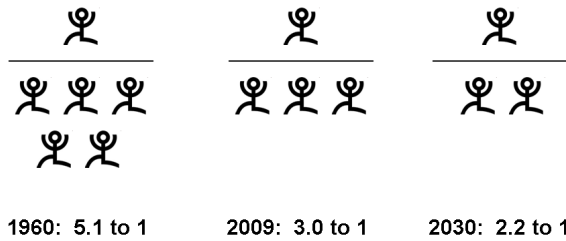


Unit 5

Percent, Ratio, and Rate



Social Security: Worker to Beneficiary Ratio



Source: Social Security Administration Trustees Report Table IV.B2
Ratio of covered workers to beneficiaries

Percent to Decimal

34% = **0.34**
 because $34 / 100 =$

- divide the percent by 100



Decimal to Percent

0.2 = **20%**
 because $0.2 \times 100 =$

0.378 = **37.8%**
 because

- multiply by 100

Handwritten notes for decimal to fraction conversion:
 - Place value labels: tenths, hundredths, thousandths with arrows pointing to digits in 0.125.
 - Calculation: $0.125 = \frac{125}{1000} \div 125 \div 125 = \frac{1}{8}$
 - Note: "Reduce fraction" written in blue.

Decimal to Fraction

-Place values help

* the place value is the denominator

* NO decimals in fractions

-Always reduce

Fraction to Decimal

-Divide top number by bottom number on a calculator

$\frac{2}{7} = 0.2857$
 $2 \div 7$

- Some fractions you can write as equivalent fractions with denominator of 100

$\frac{7}{20} = \frac{35}{100} = 0.35$
 (Note: $7 \times 5 = 35$ and $20 \times 5 = 100$)

Percent to Fraction

-Whole number put over 100

26% = $\frac{26}{100} = \frac{13}{50}$
 (Note: $26 \div 2 = 13$ and $100 \div 2 = 50$)

- NO Decimals in fractions so write equivalent fractions

12.5% =

\Rightarrow decimal $0.125 \Rightarrow$ fraction $\frac{125}{1000} = \frac{1}{8}$
 (Note: "use place value" written in blue)

$12.5\% \Rightarrow \frac{12.5}{100} \times \frac{10}{10} = \frac{125}{1000} = \frac{1}{8}$

Not Fraction

Relating Fractions, Decimals and Percent

What is percent?

Percent is a special ratio where the second term is always 100 or it is out of 100.

How do you change a percent to a decimal or fraction?

% to Decimal
÷ 100

Percent	Reduce Fraction	Decimal
18%	$\frac{18}{100} = \frac{9}{50}$	0.18
75%	$\frac{3}{4}$ 3/4	0.75
45%	$\frac{45}{100} \xrightarrow{\div 5} \frac{9}{20}$	0.45
35%	7/20 7÷20	0.35
83%	$\frac{83}{100}$	0.83
55%	$\frac{5}{9}$ 5/9	0. $\overline{55}$

$\frac{1}{9} = 0.\overline{1}$
 $\frac{2}{9} = 0.2$
 $\frac{3}{9} = \frac{1}{3} = 0.\overline{33}$

Think test results

What is the decimal value? the percentage?

$$\frac{62}{82}$$

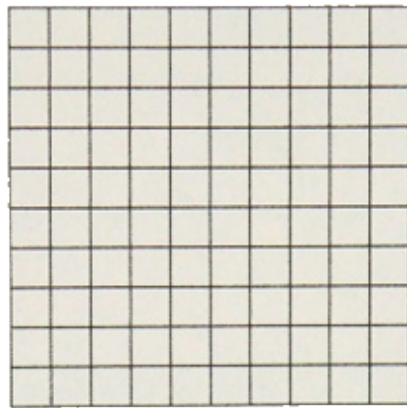
$$62 \div 82$$

0.75
decimal

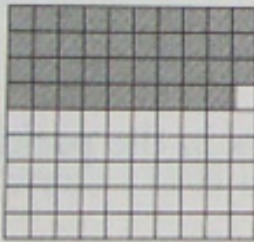
→
x100


75%

We can use a hundred chart to represent one whole or 100%. Each small square represents 1%.



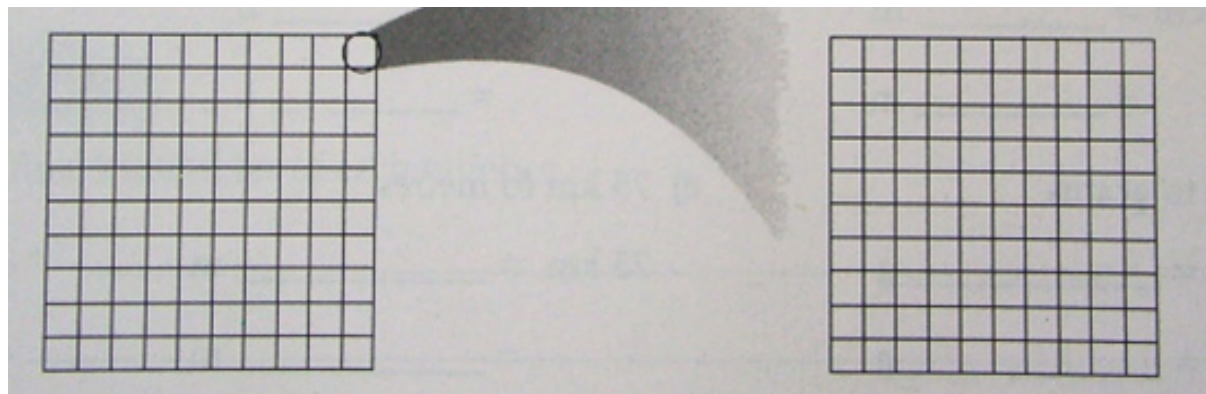
Each hundred chart represents 100%. What fraction is shaded? Write each fraction as a decimal and as a percent.

a)  **39%**

b) **80.5%** 

The image shows two examples of hundred charts. Chart (a) has 39 squares shaded gray, with the label "39%" written in red next to it. Chart (b) has 80.5 squares shaded gray, with the label "80.5%" written in blue next to it.

One small square on a hundred chart can be enlarged to show 100 squares. This is called a hundredths chart.



Each small square of a hundredths chart represents $\frac{1}{100}$ of 1%, or $\frac{1}{100}$ %, or 0.01%

Percent to decimal remember to divide by 100

Be careful not to confused a
decimal percent to a decimal

0.2% is 0.002 as a decimal

0.007% = as a decimal

Write each percent as a fraction and a decimal:

(a) 7% \rightarrow 0.07 $\frac{7}{100}$

(b) 7.75% \rightarrow 0.0775 $\frac{775}{10000} = \frac{31}{400}$

(c) $7\frac{1}{4}\%$ \rightarrow 7.25% $\xrightarrow{\div 100}$ 0.0725 $\rightarrow \frac{725}{10000} = \frac{29}{400}$

Write each fraction as a decimal and as a percent:

(a) $\frac{5}{8}$
 Fraction \rightarrow decimal
 $5 \div 8 = 0.625$ $\xrightarrow{\times 100}$ 62.5%

(b) $\frac{5}{6}$
 $0.8\bar{3}$ $\xrightarrow{\times 100}$ $8\bar{3}\%$

(c) $\frac{5}{1000} = 0.005$ $\xrightarrow{\times 100}$ 0.5%

Buffy had $23\frac{1}{2}$ out of 30 on her math test

She had $21\frac{1}{2}$ out of 40 on her second math test

On which test did Buffy do better? **1st Test**

Use calculators

1st

$$\frac{23\frac{1}{2}}{30} \Rightarrow \frac{23.5}{30} \Rightarrow 0.78 = 78\%$$

2nd

$$\frac{21\frac{1}{2}}{40} \Rightarrow \frac{21.5}{40} \Rightarrow 0.5375 = 53.75\%$$

Class/Homework

Practice Questions

% → fract → dec

Page 239 # ~~10(a,b)~~, 7(a,c)

Page 240 # ~~11~~, 9(a,c), 12(~~b~~,d), 13(a,c), 14(b,c), 16