

## Warm Up

1) Simplify the radical: **Entire  $\rightarrow$  Mixed**

$$a) \sqrt[4]{1250} = \frac{\sqrt[4]{625 \times 2}}{\sqrt[4]{625} \sqrt[4]{2}} = 5 \sqrt[4]{2}$$

$$b) \sqrt[3]{192} = \sqrt[3]{64 \times 3} = \sqrt[3]{64} \times \sqrt[3]{3}$$

2) Change the radical from mixed to entire:

$$a) 7 \sqrt[4]{2} = \sqrt[4]{7^4 \times 2} = \sqrt[4]{2401 \times 2}$$

$$b) 6 \sqrt[3]{4} = \sqrt[3]{6^3 \times 4} = \sqrt[3]{216 \times 4} = \sqrt[3]{864}$$

3) Simplify each:  $= \sqrt[4]{4802}$

$$a) (3x^6)^3 = 3^3 x^{18}$$

$$c) \frac{36x^7y^9}{12x^5y^3}$$

$$d) \left[ \frac{(12x^2)(4x^{-5})}{(16x^{12})} \right]^0$$

$$3x^2 y^6$$

$$\begin{aligned} 5^0 &= 1 \\ 6^0 &= 1 \\ 7^0 &= 1 \end{aligned} = 1$$

## Homework Solutions



Pg 218 - 219 7b, 8b, 10ace, 11egi, 12acegi, 13,14,15,17ac, 18ac



<https://www.youtube.com/watch?v=RyFr279K9TE>



Chuck Norris of Numbers

## 4.2 Irrational Numbers

### LESSON FOCUS

Identify and order irrational numbers.

### Make Connections

The formulas for the area and circumference of a circle involve  $\pi$ , which is not a rational number because it cannot be written as a quotient of integers.

What other numbers are not rational?



## TRY THIS

Work with a partner.

F. D. C.

These are rational numbers.

$$\sqrt{100} \quad \sqrt{0.25} = \frac{1}{4} \quad \sqrt[3]{8} \quad 0.5$$

$$\frac{5}{6} \quad \sqrt{\frac{9}{64}} \quad 0.8^2 \quad \sqrt[5]{-32}$$

These are not rational numbers.

$$\sqrt{0.24} \quad \sqrt[5]{100} \quad \sqrt[3]{9} \quad \sqrt{2}$$

$$\sqrt{\frac{1}{3}} \quad \sqrt[4]{12}$$

How do these rational radicals compare

to these not rational numbers

Which of these radicals are rational numbers?

Which are not rational numbers? How do you know?

$$\sqrt{1.44}$$

$$\frac{\sqrt{144}}{\sqrt{100}}$$

$$= \frac{12}{10}$$

$$= 1.2$$

$$\sqrt{\frac{64}{81}} = \frac{8}{9}$$

$$= 0.\overline{8}$$

$$\sqrt[3]{-27}$$

$$= -3$$

$$\sqrt{\frac{4}{5}}$$

$$\frac{\sqrt{4}}{\sqrt{5}} \text{ Yes}$$

$$= \text{No}$$

It is  
irrational

$$\sqrt{5}$$

$$\text{No}$$

Irrational

Write 3 other radicals that are rational numbers. Why are they rational?

Write 3 other radicals that are not rational numbers. Why are they not rational?

How are radicals that are rational numbers different from radicals that are not rational numbers?

**Rational numbers** terminate (end) or repeat

**Irrational numbers** do not terminate (end)

Radicals that are square roots of perfect squares, cube roots of perfect cubes, and so on are rational numbers. Rational numbers have decimal representations that either terminate or repeat.

?

$\sqrt{2}$

1.414213562

$\sqrt[3]{-500}$

-3.684031499

?

4.2 Irrational Numbers

When an irrational number is written as a radical, the radical is the exact value.

Examples:

$$\sqrt{2} \quad \sqrt[3]{-50} \quad \text{exact}$$

When we use the square root or cube root key on our calculators we are obtaining approximate value of irrational numbers.

$$\sqrt{2} \approx 1.4142$$

**Example 1** Classifying Numbers

Tell whether each number is rational or irrational. Explain how you know.

a)  $-\frac{3}{5}$       b)  $\sqrt{14}$       c)  $\sqrt[3]{\frac{8}{27}}$

**SOLUTION** 



CHECK YOUR UNDERSTANDING



4.2 Irrational Numbers



Natural Numbers

$\mathbb{N}$  1, 2, 3, 4, 5, ..

Whole Numbers

$\mathbb{W}$  0, 1, 2, 3, 4

Integers

$\mathbb{I}^+$  whole

Rational

$\mathbb{Q}$

Irrational

$\overline{\mathbb{Q}}$

Real

$\mathbb{R}$

**Natural Numbers :**

Ex. 1, 2, 3 etc

**Whole Numbers:** Counting numbers including zero.

Ex. 0, 1, 2, 3, etc

**Integers:** Are all positive and negative whole numbers.  
(Remember zero is neither negative or positive)

Ex: ....3,2,1,0,-1-2,-3...

**Rational Numbers:** All whole numbers, fractions, mixed  
numbers, decimals and their negatives  
The decimal must repeat or terminate also.

Ex:  $\frac{1}{3}$ , 4,  $\frac{3}{4}$

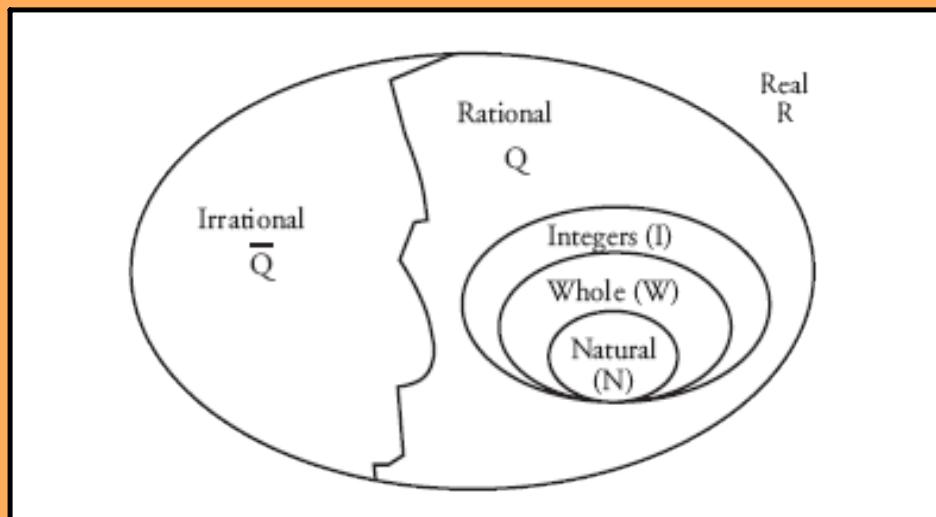
**Irrational Numbers:** Decimals that never terminate or repeat.

Ex:  $\sqrt{2}$

**Real Numbers:** All rational and irrational numbers are real  
numbers

Ex: All possible numbers

### Review of Types of Number Systems



Exercise

Complete the table

	N	W	I	Q	$\bar{Q}$	R
5	✓	✓	✓	✓	✗	✓
-2	✗	✗	✓	✓	✗	✓
$\frac{3}{4}$	✗	✗	✗	✓	✗	✓
-1.3	✗	✗	✗	✓	✗	✓
$\sqrt{7}$	✗	✗	✗	✗	✓	✓
$\sqrt{95}$	✗	✗	✗	✗	✓	✓

## Attachments

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[Day 6 Entire to mix \(Homework Solutions to Day 5 Pg 218\\_219\).notebook](#)