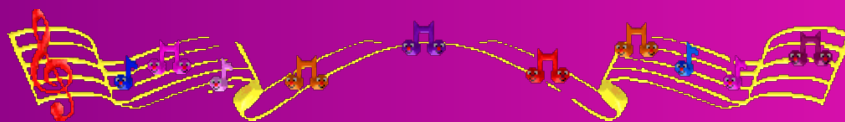


## Chapter 5

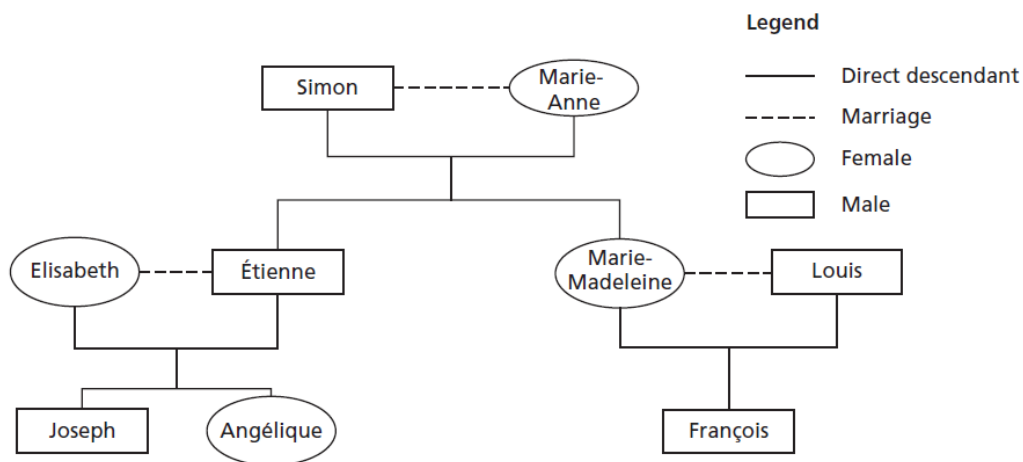
# Functions & Relations



## 5.1 Representing Relations



**How are we Related !!!!**



- How is Joseph related to Simon?
- How are Angelique and Francois related?
- How does the family tree show these relations?



# Terminology

A set is a collection of distinct objects.

## Set of Fruit

Fruit

apple

blueberry

cherry

huckleberry

## Set of Colours

Colour

red

green

blue

Sets use { }

Ordered pairs use (\_\_, \_\_)

An ***element*** of a set is one object in the set.

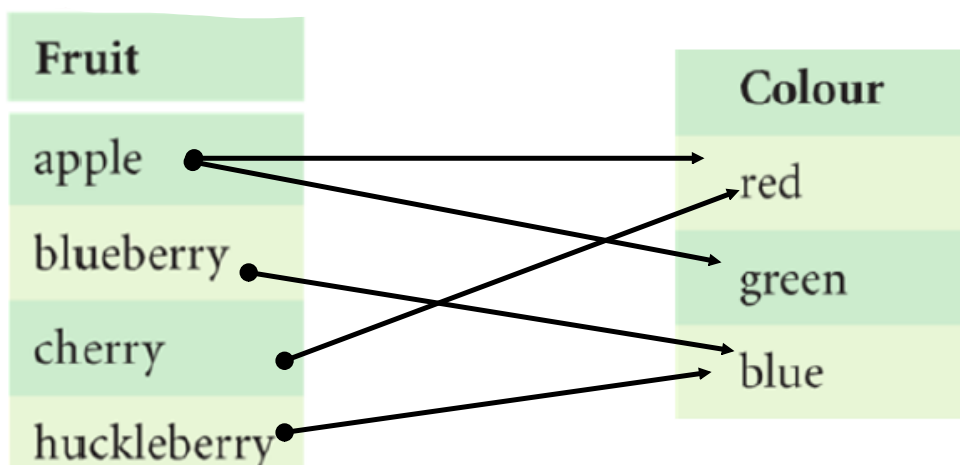


<b><u>Set of Fruit</u></b>
Fruit
apple
blueberry
cherry
huckleberry

***Apple*** is an ***element*** of the set of Fruit

# Terminology

Arrow diagram show how one set is related to another set



Sets use { }

Ordered pairs use (\_\_, \_\_)

Set of ordered pairs

{ (Apple, red), (apple, green), (Blueberry, Blue), (Cherry, red), (Huckleberry, blue)}

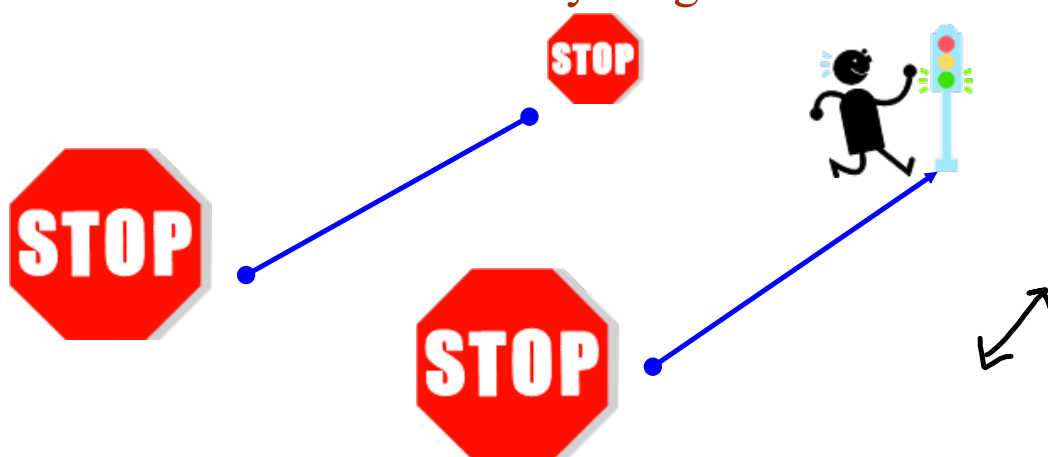
# Independent / Dependent

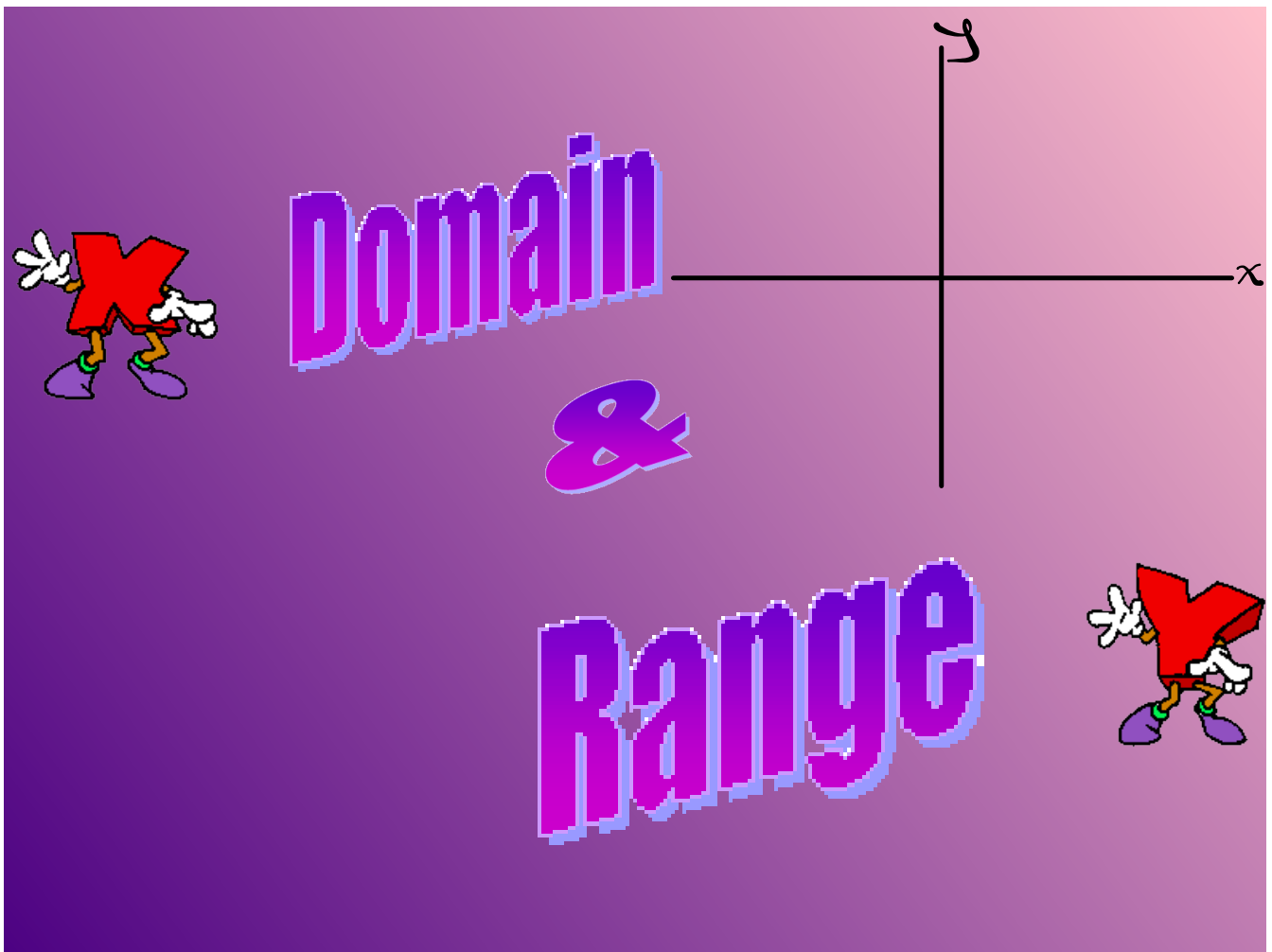
**Dependent** - a variable whose value is determined by the value of another (independent) variable.  
(y) or range ↕

**Independent** - a variable whose value is not determined by the value of another variable, and whose value determines the value of another (dependent) variable  
↔  
(x) or domain

# Limits?

There are limits to everything in life!









# Domain & Range



**Domain** - the set of first elements in a relation

**Range** - the set of second elements in a relation

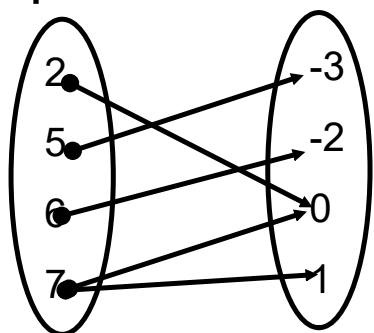
Input	Output
1	5
2	7
	9
4	
	13

$x$	$y$
Sport	Equipment
badminton	shuttlecock
badminton	racquet
hockey	puck
hockey	stick
tennis	ball
tennis	racquet
soccer	ball

First                      Second  
( Sport, Equipment )

<span style="font-size: 2em; font-weight: bold; color: multi;">Domain</span>	<p>The set of first elements:                  { badminton, hockey, tennis, soccer }</p>
<span style="font-size: 2em; font-weight: bold; color: multi;">Range</span>	<p>The set of second elements:                  { shuttlecock, racquet, puck, stick, ball }</p>

Input      Output



This is an arrow diagram. Follow the arrows to write the set of ordered pairs.

The set of ordered pairs is

$\{(2,0), (5,-3), (6,-2), (7, 0), (7, 1)\}$

# There are two types of graphs and data

## Discrete and Continuos Data

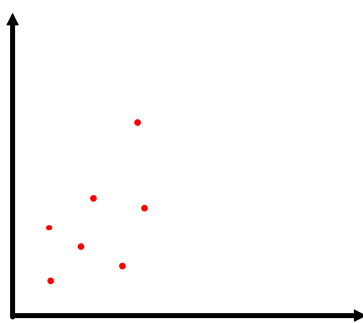
### Discrete Data

- points are not joined together with a line on the graph.
- A finite number of values exist between points
- hint ask yourself can you have part of a "x" value. If no then discrete

### Continuous Data

- points are joined together with a line on the graph.
- A infinite number of values exist between points
- hint ask yourself can you have part of a "x" value. If yes then continuous

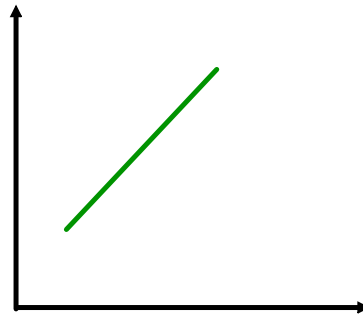
Examples)



Discrete

with dots then

$$\begin{array}{l}
 x \in \mathbb{W} \\
 \boxed{x \in \mathbb{I}} \\
 x \in \mathbb{N}
 \end{array}
 \left. \vphantom{\begin{array}{l} x \in \mathbb{W} \\ x \in \mathbb{I} \\ x \in \mathbb{N} \end{array}} \right\}
 \begin{array}{l}
 y \in \mathbb{W} \\
 \boxed{y \in \mathbb{I}} \\
 y \in \mathbb{N}
 \end{array}$$



Continuous

with line

$$\begin{array}{l}
 x \in \mathbb{R} \\
 y \in \mathbb{R}
 \end{array}$$

*Is a member of*

*Real #*

Review from Grade 6 & 8

For Word Problems Ask yourself

"Can you have part of the data on the x axis or the y axis?"

If yes ,then it is continuous.

If no, then discrete

Examples:

1) Remember the example graphing the number of people at a dance  
between 9 and 10 o'clock

You can have part of a time BUT cannot have part of a person at the  
dance. So DISCRETE

2) Graphing the temperature of a lake from 7:00 pm to 7:00 am

You can have part of a time AND you can have part of a temperature.  
So CONTINUOUS

## Linear & Non-Linear

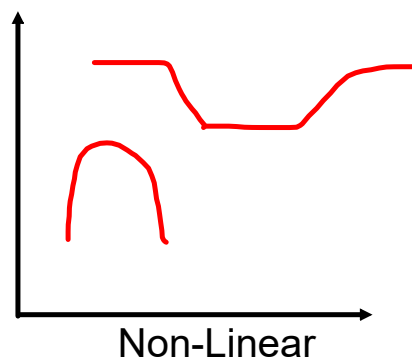
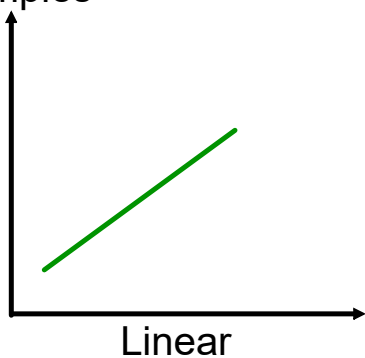
Linear graphs - the data is a single straight line  
(Doesn't have to be connected)

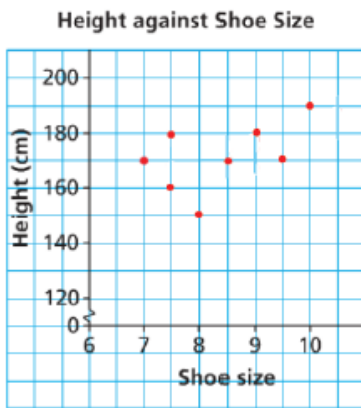


Non-Linear graphs - the data is NOT a straight line  
- It can curve or spread out with no real pattern.



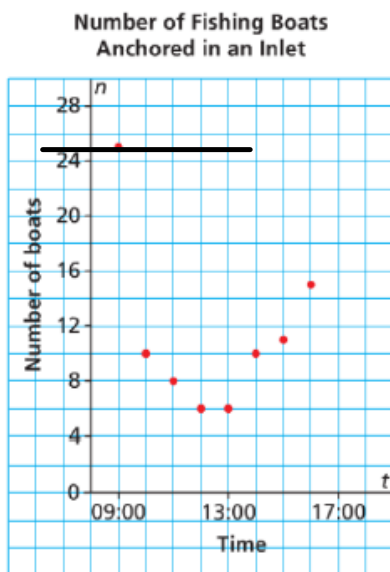
Examples





- ↔
- a) State the domain & range.  
 $D = \{7, 7.5, 8, 8.5, 9, 9.5, 10\}$   
 $R = \{150, 160, 170, 180, 190\}$
- b) Why are the points not connected? Explain.  
 discrete - (dots)

Shoes do not come in partial sizes (No 7.1 or 7.3)



a) State the domain & range.

$D \{ 9, 10, 11, 12, 13, 14, 15, 16 \}$

$R \{ 6, 8, 10, 11, 15, 25 \}$

b) Why are the points not connected? Explain

discrete  
since you  
cannot have  
part of a  
boat docked





## How do you state the Domain & Range?

When connected lines

How to write Range

$$\left\{ y \mid \boxed{\text{lowest}} \leq y \leq \boxed{\text{highest}}, y \in \boxed{\text{is a member of}} \right\}$$

*Such that* (above the vertical bar), *lowest* (below the first box), *highest* (below the second box), *is a member of* (above the set symbol), *R conn* (above the set symbol), *Z to Dis* (below the set symbol).

How to write Domain

$$\left\{ x \mid \boxed{\text{left}} \leq x \leq \boxed{\text{Right}}, x \in \boxed{\text{is a member of}} \right\}$$

*left* (below the first box), *Right* (below the second box), *is a member of* (above the set symbol).

You can use this for dots as well as using as you say  $x \in I$

How to write Range ↓

$$\{y \mid \underset{\text{low}}{-2} \leq y \leq 5, y \in I\}$$

How to write Domain ←

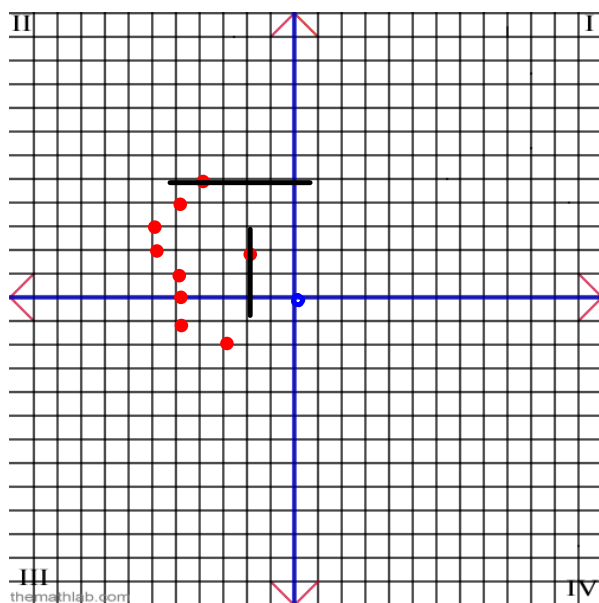
$$\{x \mid \underset{\text{left}}{-6} \leq x \leq 2, x \in I\}$$

↘ I will use this

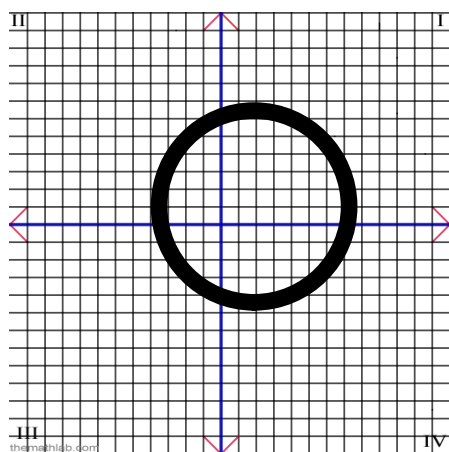
or you can list as a set

Domain  $\{-6, -5, -4, -3, -2\}$

Range:  $\{-2, -1, 0, 1, 2, 3, 4, 5\}$



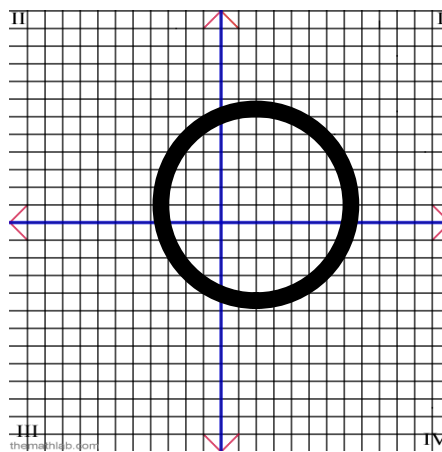
**Domain**



The **domain** represents all the values of  $x$ .

**X is the independent Variable**

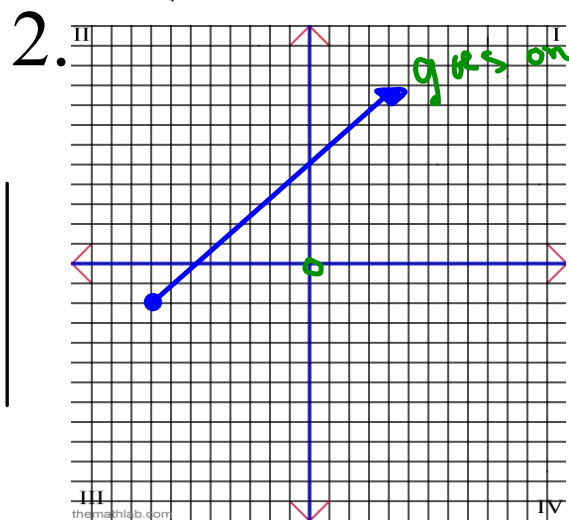
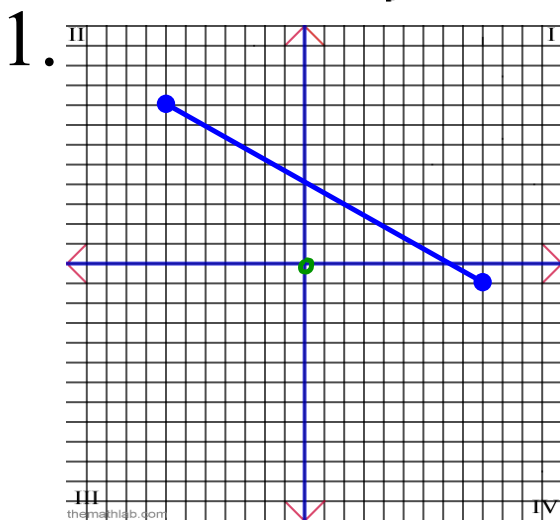
**Range**



The **range** represents all the values of  $y$ .

**Y is the dependent Variable**

# EXAMPLES!



Domain:  $\{x \mid \underline{-7} \leq x \leq \underline{9}, x \in \underline{\mathbb{R}}\}$

Domain:  $\{x \mid \underline{-8} \leq x, x \in \underline{\mathbb{R}}\}$

Range:  $\{y \mid \underline{-1} \leq y \leq \underline{8}, y \in \underline{\mathbb{R}}\}$

Range:  $\{y \mid \underline{-2} \leq y, y \in \underline{\mathbb{R}}\}$

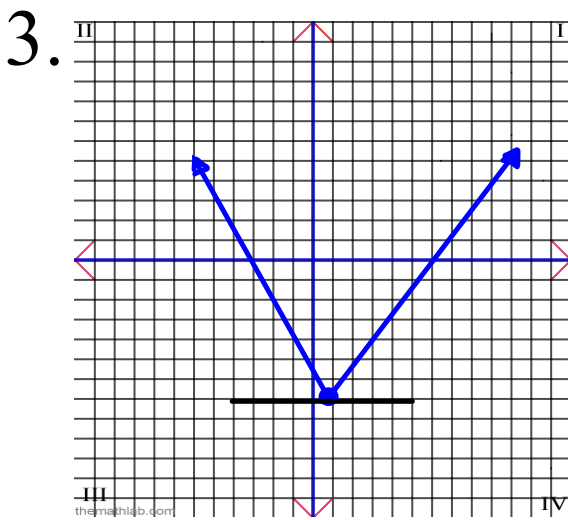
Is it continuous or discrete?

Is it continuous or discrete?

Is it linear or non linear?

Is it linear or non linear?

# EXAMPLES!

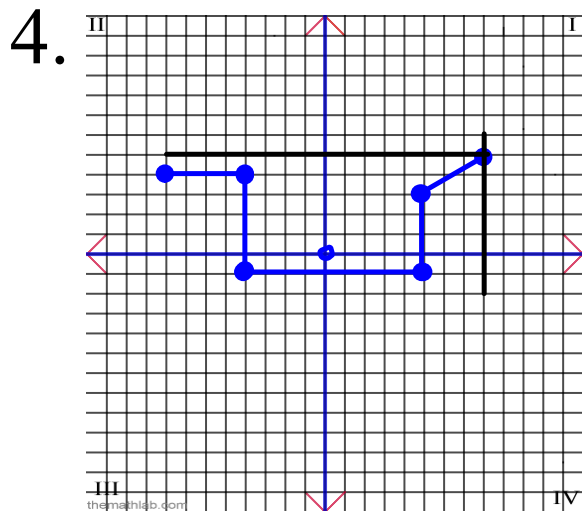


Domain:  $\{x \mid x \in \mathbb{R}\}$

Range:  $\{y \mid -7 \leq y, y \in \mathbb{R}\}$

Is it continuous or discrete?

Is it linear or non linear?



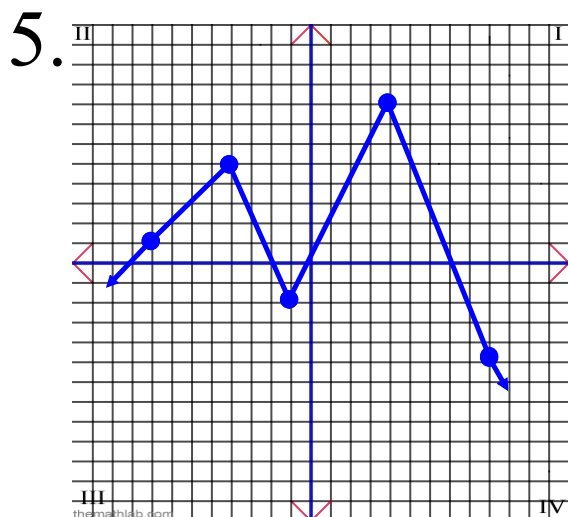
Domain:  $\{x \mid -8 \leq x \leq 8, x \in \mathbb{R}\}$

Range:  $\{y \mid -1 \leq y \leq 4, y \in \mathbb{R}\}$

Is it continuous or discrete?

Is it linear or non linear?

# EXAMPLES!



Domain:  $\{x \mid x \in \underline{R}\}$

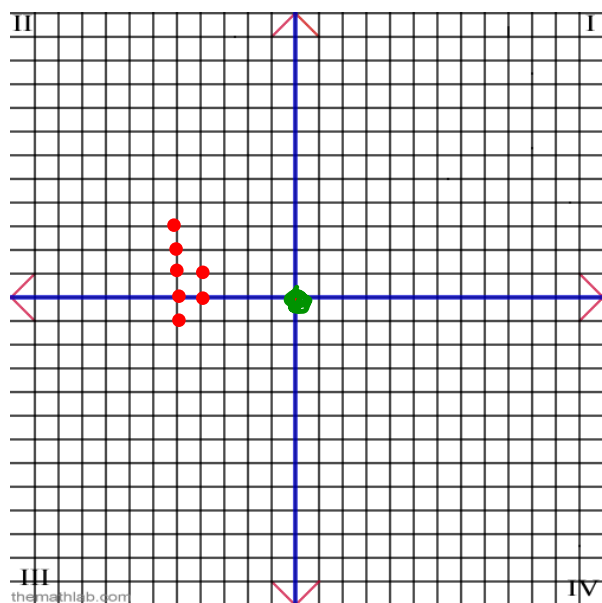
Range:  $\{y \mid y \leq \underline{8}, y \in \underline{R}\}$

Is it continuous or discrete?

Is it linear or non linear?

# EXAMPLES!

7.



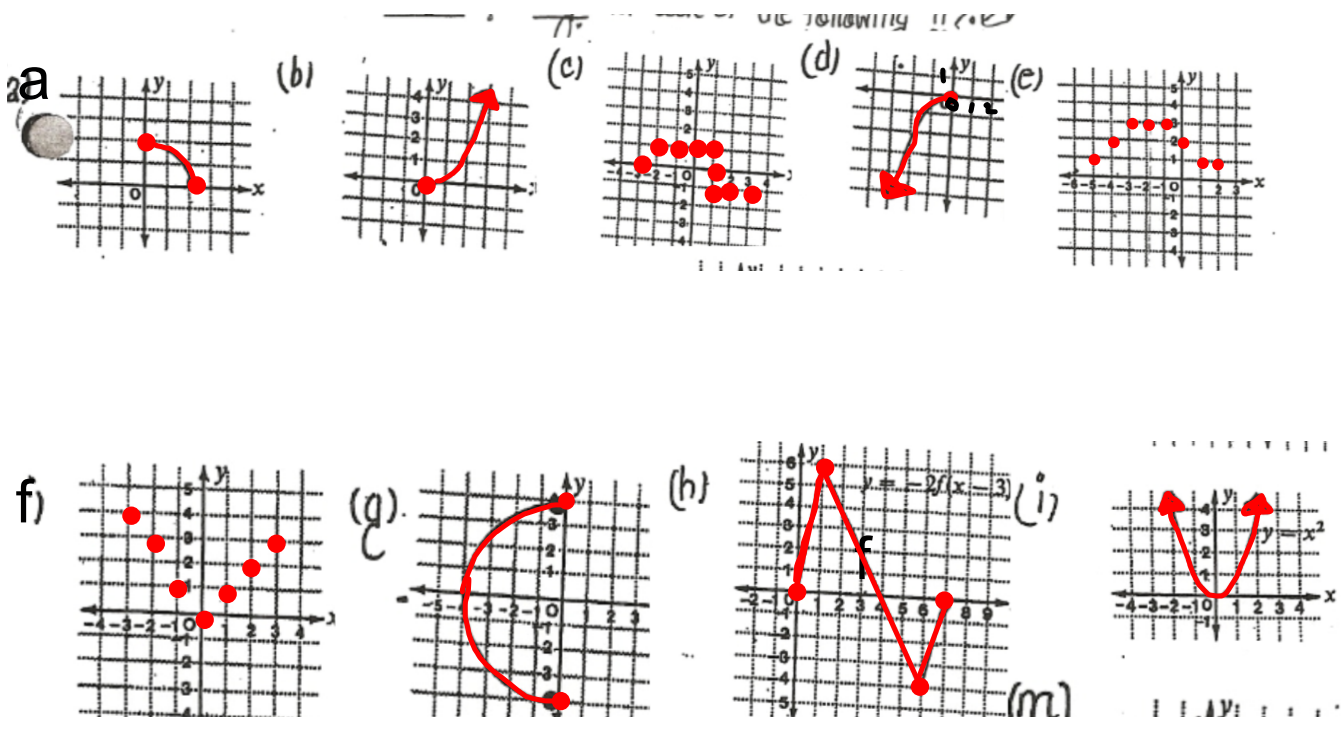
Domain:  $\{x \mid \underline{-5} \leq x \leq \underline{-4}, x \in \underline{\mathbb{I}}\}$

Range:  $\{y \mid \underline{-1} \leq y \leq \underline{3}, y \in \underline{\mathbb{I}}\}$

Is it continuous or discrete?

Is it linear or non linear?

Class/Homework Write the domain, range, is it continuous or discrete, and is linear or nonlinear.





Class/Homework Write the domain, range, is it continuous or discrete, and is linear or nonlinear.

