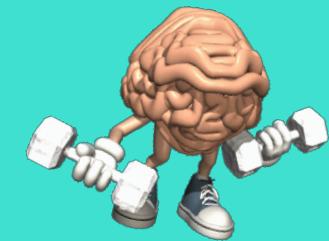




# Warm Up



1) Solve the following systems using Substitution :

a)  $3x - 4y = 19$   
 $x + 4y = 1 - 4y$

b)  $3x + y = 3$   
 $x = y - 1$

①  $x = 1 - 4y$   
 Sub into ②

$$\begin{aligned} 3x - 4y &= 19 \\ 3(1 - 4y) - 4y &= 19 \\ 3 - 12y - 4y &= 19 \\ 3 - 16y &= 19 - 3 \\ -16y &= \frac{16}{-16} \end{aligned}$$

$$y = -1$$

↓ Sub into 1

$$\begin{aligned} x &= 1 - 4y \\ &= 1 - 4(-1) \end{aligned}$$

$$x = 1 + 4$$

$$x = 5$$

$$(5, -1)$$

$$\begin{aligned} 3x + y &= 3 \\ 3(y - 1) + y &= 3 \\ 3y - 3 + y &= 3 \\ 4y - 3 &= 3 \\ 4y &= \frac{6}{4} \\ y &= \frac{3}{2} \end{aligned}$$

$$y = \frac{3}{2}$$

$$\begin{aligned} x &= y - 1 && \text{need C. D.} \\ &= \frac{3}{2} - 1 \\ &= \frac{3}{2} - \frac{2}{2} && \frac{1}{1} = \frac{2}{2} \end{aligned}$$

$$x = \frac{1}{2}$$

$$(\frac{1}{2}, \frac{3}{2})$$

$$(0.5, 1.5)$$

this is the warm up

a)  $3x - 4y = 19$   
 $x + 4y = 1$

this is the warm up

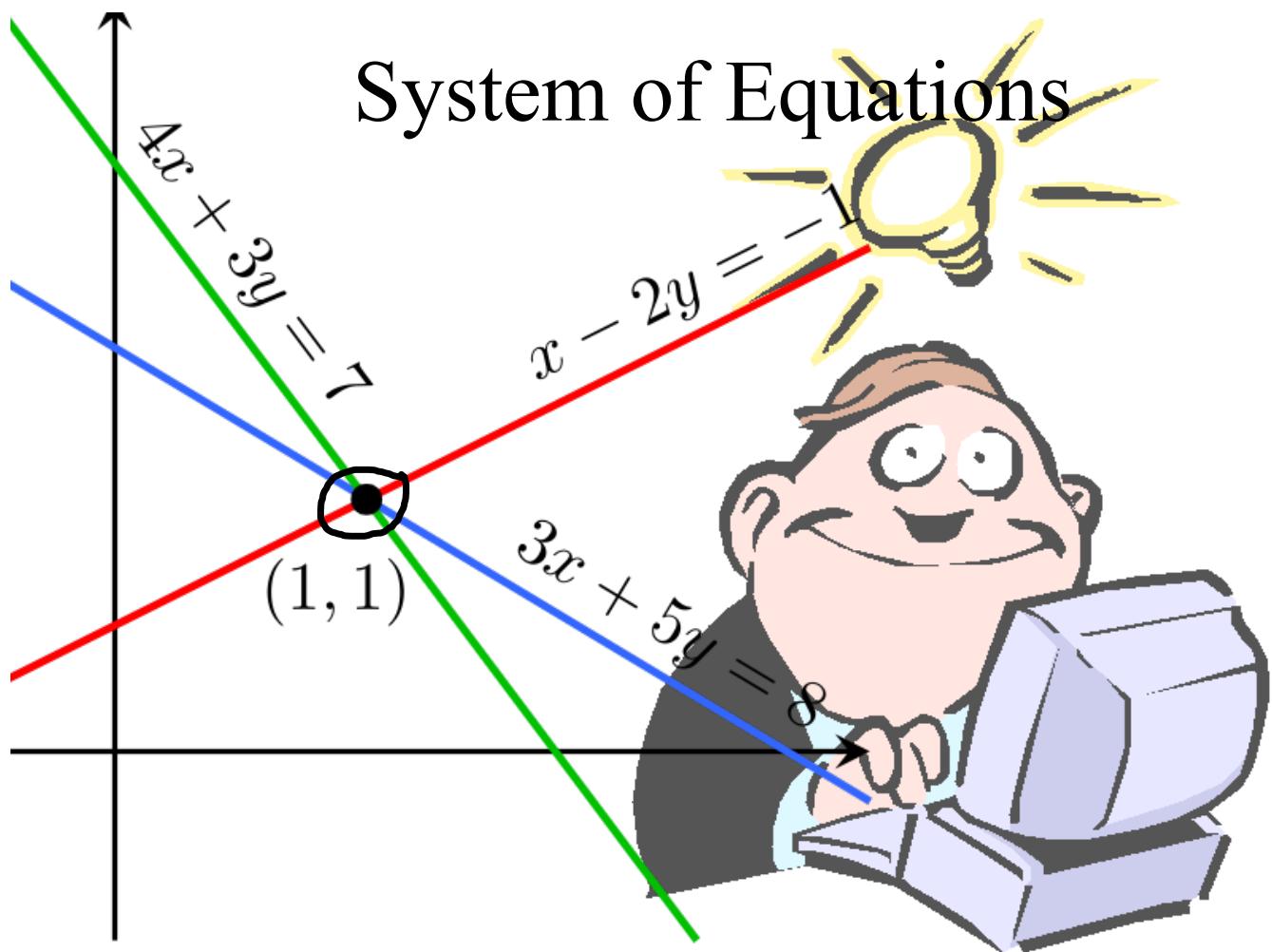
$$\text{b) } 3x + y = 3$$

$$x = y - 1$$

HW Solutions to WS



Click on link above



You try

## Elimination using Addition

Consider the system

$$\begin{array}{r} \textcircled{1} \ x - 2y = 5 \\ \textcircled{2} \ \underline{2x + 2y = 7} \\ \textcircled{1+2} \ 3x = 12 \end{array}$$

$$\frac{3x}{3} = \frac{12}{3}$$

$$x = 4$$

↓ Sub it into 1

$$\begin{array}{l} \textcircled{1} \ x - 2y = 5 \\ 4 - 2y = 5 \\ 4 - 2y = 5 - 4 \end{array}$$

$$-2y = 1$$

$$\frac{-2y}{-2} = \frac{1}{-2}$$

$$y = -\frac{1}{2}$$

$$(4, -\frac{1}{2})$$

## Elimination using Addition

Consider the system

$$\begin{array}{rcl} x - 2y & = 5 & \leftarrow \\ + 2x + 2y & = 7 & \leftarrow \\ \hline \end{array}$$

Lets add both equations  
to each other

touch

# Solution

## Elimination using Addition

Consider the system

$$\begin{array}{rcl}
 x - 2y & = 5 & \leftarrow \\
 + 2x + 2y & = 7 & \leftarrow \\
 \hline
 3x & = 12 &
 \end{array}$$

Lets add both equations to each other

solve for x

ANS: (4, y)

$$x = 4$$

Now solve for y (HOW???)

- sub the value of x into one of the equations and solve for y

$$\begin{aligned}
 x - 2y &= 5 \\
 4 - 2y &= 5 \\
 -2y &= 1
 \end{aligned}$$

$$y = \frac{-1}{2}$$

intersection point (4, - 0.5)

# Elimination using Addition

Same process as before  
You can choose to eliminate either x or y

$$\textcircled{1} \quad x + 3y = 14$$

Who would you eliminate??

$$\textcircled{2} \quad \underline{-x + 4y = 7}$$

Do you add or subtract?

$$\textcircled{1} - \textcircled{2} \quad 7y = 21$$

$$\frac{7y}{7} = \frac{21}{7}$$

$$y = 3$$

↓ sub \textcircled{1}

$$x + 3y = 14$$

$$x + 3(3) = 14$$

$$x + 9 = 14 - 9$$

$$x = 5$$

$$(5, 3)$$

Solution

## Elimination using Addition

$$\begin{array}{r} \textcircled{x} + 3y = 14 \\ -\textcircled{x} + 4y = 7 \\ \hline 7y = 21 \end{array}$$

Add this time

$$y = 3$$

$$(x, 3)$$

solve for x

$$x + 3y = 14$$

$$x + 3(3) = 14$$

$$x + 9 = 14$$

$$x = 14 - 9$$

$$x = 5$$

## You Try

Solve the system of equations

Example 1)

$$\begin{array}{rcl}
 & \downarrow & \\
 2x + y & = & 5 \\
 + 3x - y & = & 15 \\
 \hline
 5x & = & 20 \\
 \hline
 5 & & 5 \\
 \boxed{x=4} & & \\
 \downarrow \text{sub into ①} & &
 \end{array}$$

$$\begin{array}{l}
 2x + y = 5 \\
 2(4) + y = 5 \\
 8 + y = 5 - 8
 \end{array}$$

$$\begin{array}{l}
 \boxed{y = -3} \\
 (-4, -3)
 \end{array}$$

Example 2)

$$\begin{array}{rcl}
 \begin{cases} 6y + x = 11 \\ 2y - x = 5 \end{cases} & \downarrow & \\
 \begin{array}{rcl}
 \textcircled{1} & 6y + x & = 11 \\
 \textcircled{2} & 2y - x & = 5 \\
 \hline
 \textcircled{1} + \textcircled{2} & 8y & = 16 \\
 & \frac{8}{8} & \frac{16}{8} \\
 \boxed{y = 2} & & \\
 \downarrow \text{sub into ①} & &
 \end{array} & &
 \end{array}$$

$$\begin{array}{l}
 6y + x = 11 \\
 6(2) + x = 11 \\
 12 + x = 11 - 12
 \end{array}$$

$$\begin{array}{l}
 \boxed{x = -1} \\
 (-1, 2)
 \end{array}$$

## Elimination Using Subtraction

---

$$\begin{array}{r}
 6x + 11y = -5 \\
 - (6x + 9y = -3) \\
 \hline
 2y
 \end{array}$$

Careful you are subtraction all of the second  
(switch all signs on the second equation)

Sub into ①

$$\begin{aligned}
 6x + 11y &= -5 \\
 6x + 11(-1) &= -5 \\
 6x - 11 &= -5 + 11
 \end{aligned}$$

$$\frac{6x}{6} = \frac{6}{6}$$

$$x = 1$$

$$\begin{array}{r}
 6x + 11y = -5 \\
 -6x - 9y = +3 \\
 \hline
 2y = -2 \\
 y = -1
 \end{array}$$

May want to  
change signs and  
add

$$(1, -1)$$

**Same****Elimination Using Subtraction**

Careful you are subtraction all of the second  
(switch all signs on t second equation)

$$\begin{aligned} & \textcircled{6x} + 11y = -5 \\ & -(6x + 9y) = -3 \end{aligned}$$



**Solution****Elimination Using Subtraction**

Careful you are subtraction all of the second  
(switch all signs on the second equation)

$$\begin{array}{r} 6x + 11y = -5 \\ -6x - 9y = +3 \\ \hline 2y = -2 \end{array}$$

$$y = -1$$

solve for x

$$\begin{aligned} 6x + 11y &= -5 \\ 6x + 11(-1) &= -5 \\ 6x - 11 &= -5 \\ 6x &= -5 + 11 \\ 6x &= 6 \\ x &= 1 \end{aligned}$$

Intersection (1, -1)

**You Try**

Use subtraction to eliminate

$$\begin{array}{rcl} \text{a)} & 7x + 7y = 0 & 7x + 7y = 0 \\ & - (7x - y = 2) & \cancel{-7x} \cancel{+y} = \cancel{-2y} \\ & \textcircled{1} - \textcircled{2} & \end{array}$$

$$\frac{8y}{8} = \frac{-24}{8}$$

$$y = -3$$

↓ sub ①

$$\begin{array}{l} 7x + 7y = 0 \\ 7x + 7(-3) = 0 \\ 7x + 21 = 0 - 21 \end{array}$$

$$\frac{7x}{7} = \frac{-21}{7}$$

$$x = 3$$

$$(3, -3)$$

$$\begin{array}{l} \text{b)} 7x + 6y = -10 \\ 9x + 6y = -30 \end{array}$$

Math 10 (Numbers Relations &amp; Functions)

Name \_\_\_\_\_

## Elimination

Date \_\_\_\_\_

Solve each system by elimination.

$$\begin{array}{l} \text{1) } 2x + 8y = 8 \\ -3x - 8y = -4 \end{array}$$

**Add**

$$\begin{array}{l} \text{2) } -x + 4y = 7 \\ x + 4y = 25 \end{array}$$

**Add**

$$\begin{array}{l} \text{3) } -9x + 8y = 15 \\ -9x + 6y = 27 \end{array}$$

**Subtr**

$$\begin{array}{l} \text{4) } -x - 5y = -3 \\ -x + 3y = 13 \end{array}$$

**Subtr**

$$\begin{array}{l} \text{5) } -5x + 2y = 9 \\ 6x - 2y = -8 \end{array}$$

**Add**

$$\begin{array}{l} \text{6) } 5x + 5y = 30 \\ 5x + 2y = 12 \end{array}$$

**Subtr**

$$\begin{array}{l} \text{7) } -10x + 8y = -28 \\ 9x + 4y = 14 \end{array}$$

$$\begin{array}{l} \text{8) } -6x + y = -15 \\ -12x - 3y = -15 \end{array}$$

$$\begin{array}{l} \text{9) } -5x + 10y = -10 \\ -7x - 5y = -14 \end{array}$$

$$\begin{array}{l} \text{10) } -5x + 10y = 5 \\ 10x - 4y = 6 \end{array}$$

$$\begin{array}{l} \text{11) } 7x - 2y = 24 \\ 3x + 9y = 30 \end{array}$$

$$\begin{array}{l} \text{12) } -3x - 2y = 2 \\ -5x - 3y = 6 \end{array}$$

$$\begin{array}{l} \text{13) } 3x - 6y = 30 \\ -10x - 9y = -13 \end{array}$$

$$\begin{array}{l} \text{14) } 7x - 10y = 0 \\ -9x - 4y = 0 \end{array}$$

$$\begin{array}{l} \text{15) } -10x + 7y = 12 \\ -3x + 6y = -12 \end{array}$$

$$\begin{array}{l} \text{16) } -3x + 4y = 2 \\ -5x + 3y = 29 \end{array}$$

$$\begin{array}{l} \text{17) } -10x - 6y = -14 \\ 8x + 5y = 11 \end{array}$$

$$\begin{array}{l} \text{18) } -3x - 2y = 8 \\ -8x - 7y = 18 \end{array}$$

$$\begin{aligned}1) \quad & 2x + 8y = 8 \\& -3x - 8y = -4 \\& (-4, 2)\end{aligned}$$

$$\begin{aligned}2) \quad & -x + 4y = 7 \\& x + 4y = 25 \\& (9, 4)\end{aligned}$$

$$\begin{aligned}3) \quad -9x + 8y &= 15 \\-9x + 6y &= 27 \\(-7, -6)\end{aligned}$$

$$\begin{aligned}4) \quad -x - 5y &= -3 \\-x + 3y &= 13 \\(-7, 2)\end{aligned}$$

$$\begin{aligned} 5) \quad -5x + 2y &= 9 \\ 6x - 2y &= -8 \\ (1, 7) \end{aligned}$$

$$\begin{aligned} 6) \quad 5x + 5y &= 30 \\ 5x + 2y &= 12 \\ (0, 6) \end{aligned}$$

$$\begin{aligned} 7) \quad -10x + 8y &= -28 \\ 9x + 4y &= 14 \\ (2, -1) \end{aligned}$$

$$\begin{aligned} 8) \quad -6x + y &= -15 \\ -12x - 3y &= -15 \\ (2, -3) \end{aligned}$$

$$\begin{aligned} 9) \quad -5x + 10y &= -10 \\ -7x - 5y &= -14 \end{aligned}$$

(2, 0)

$$\begin{aligned} 10) \quad -5x + 10y &= 5 \\ 10x - 4y &= 6 \end{aligned}$$

(1, 1)

$$\begin{aligned}11) \quad & 7x - 2y = 24 \\& 3x + 9y = 30 \\& (4, 2)\end{aligned}$$

$$\begin{aligned}12) \quad & -3x - 2y = 2 \\& -5x - 3y = 6 \\& (-6, 8)\end{aligned}$$

$$\begin{aligned}13) \quad & 3x - 6y = 30 \\& -10x - 9y = -13 \\& (4, -3)\end{aligned}$$

$$\begin{aligned}14) \quad & 7x - 10y = 0 \\& -9x - 4y = 0 \\& (0, 0)\end{aligned}$$

$$\begin{aligned}15) \quad -10x + 7y &= 12 \\ -3x + 6y &= -12 \\ (-4, -4) &\end{aligned}$$

$$\begin{aligned}16) \quad -3x + 4y &= 2 \\ -5x + 3y &= 29 \\ (-10, -7) &\end{aligned}$$

$$\begin{aligned}17) \quad -10x - 6y &= -14 \\8x + 5y &= 11 \\(2, -1)\end{aligned}$$

$$\begin{aligned}18) \quad -3x - 2y &= 8 \\-8x - 7y &= 18 \\(-4, 2)\end{aligned}$$

## Homework:

Math 10B

Name\_\_\_\_\_

System of Equations: Elimination (Add &amp; Sub)

Date\_\_\_\_\_

Solve each system by elimination.

1)  $8x - 8y = 0$   
 $-5x + 8y = -3$

2)  $6x - 4y = 6$   
 $-8x + 4y = 0$

3)  $-3x + 8y = -15$   
 $9x - 8y = -3$

4)  $x + 3y = 18$   
 $3x - 3y = -6$

5)  $-x + 5y = -28$   
 $x + 3y = -28$

6)  $-5x + 3y = 10$   
 $5x - 5y = 10$

7)  $-4x + 5y = 25$   
 $-4x + 6y = 22$

8)  $-3x + 5y = 12$   
 $-5x + 5y = 0$

11)  $5x - y = 19$   
 $-9x - y = -9$

12)  $-2x + y = 0$   
 $-6x + y = 20$

13)  $10x = 18 + 8y$   
 $-8y = -5x - 27$

14)  $8y + 13 = 3x$   
 $-8y = 9x + 25$

15)  $4 + x = -2y$   
 $16 + 8y - x = 0$

16)  $-12 + 8x = 6y$   
 $-5y - 10 = 4x$

**Homework:**

Math 10B

Name \_\_\_\_\_

System of Equations: Elimination (Add &amp; Sub)

Date \_\_\_\_\_

Solve each system by elimination.

1)  $8x - 8y = 0$   
 $-5x + 8y = -3$

2)  $6x - 4y = 6$   
 $-8x + 4y = 0$

 $(-3, -6)$  add

3)  $-3x + 8y = -15$   
 $9x - 8y = -3$

4)  $x + 3y = 18$   
 $3x - 3y = -6$

 $(3, 5)$  add

5)  $-x + 5y = -28$   
 $x + 3y = -28$

6)  $-5x + 3y = 10$   
 $5x - 5y = 10$

 $(-8, -10)$  add

7)  $-4x + 5y = 25$   
 $-4x + 6y = 22$

8)  $-3x + 5y = 12$   
 $-5x + 5y = 0$

 $(6, 6)$  sub

9)  $-4x - 7y = -15$   
 $-4x - 9y = -17$

10)  $-5x - 3y = 7$   
 $-2x - 3y = -8$

 $(-5, 6)$  sub

11)  $5x - y = 19$   
 $-9x - y = -9$

12)  $-2x + y = 0$   
 $-6x + y = 20$

 $(-5, -10)$  sub

13)  $10x = 18 + 8y$   
 $-8y = -5x - 27$

14)  $8y + 13 = 3x$   
 $-8y = 9x + 25$

 $(-1, -2)$  sub

15)  ~~$4 + x = -2y$~~   
 ~~$16 + 8y - x = 0$~~

16)  ~~$-12 + 8x = 6y$~~   
 ~~$-5y - 10 = 4x$~~

 ~~$(0, -2)$~~

$$\begin{array}{r}
 2) \quad 6x - 4y = 6 \quad \textcircled{1} \\
 + \quad -8x + 4y = 0 \quad \textcircled{2} \\
 \hline
 -2x + 0 = 6 \\
 -2x = 6 \\
 x = \frac{6}{-2}
 \end{array}$$

$$\boxed{x = -3}$$

$$\begin{aligned}
 6x - 4y &= 6 \\
 6(-3) - 4y &= 6 \\
 -18 - 4y &= 6 \\
 -4y &= 6 + 18 \\
 -4y &= 24
 \end{aligned}$$

$$y = \frac{24}{-4}$$

$$\boxed{y = -6}$$

$$\begin{array}{r}
 2) \quad 6x - 4y = 6 \quad \textcircled{1} \\
 + \quad -8x + 4y = 0 \quad \textcircled{2} \\
 \hline
 -2x + 0 = 6 \\
 -2x = 6 \\
 x = \frac{6}{-2}
 \end{array}$$

$$\boxed{x = -3}$$

$$\begin{aligned}
 6x - 4y &= 6 \\
 6(-3) - 4y &= 6 \\
 -18 - 4y &= 6 \\
 -4y &= 6 + 18 \\
 -4y &= 24
 \end{aligned}$$

$$y = \frac{24}{-4}$$

$$\boxed{y = -6}$$

$$\begin{array}{r}
 8) \quad -3x + 5y = 12 \quad \textcircled{1} \\
 -(-5x + 5y = 0) \quad \textcircled{2} \\
 \hline
 (-3x + 5x) + 0 = 12 - 0
 \end{array}$$

$$2x = 12$$

$$x = \frac{12}{2}$$

$$\boxed{x = 6}$$

$$-3x + 5y = 12$$

$$-3(6) + 5y = 12$$

$$-18 + 5y = 12$$

$$5y = 12 + 18$$

$$5y = 30$$

$$\boxed{y = 6}$$

$$\begin{aligned}8) \quad & -3x + 5y = 12 \\& - (-5x + 5y = 0)\end{aligned}$$

$$\begin{array}{r}8) \quad -3x + 5y = 12 \\+ \quad 5x - 5y = 0 \\ \hline 2x \quad = 12\end{array}$$

$$x = 6$$

$$\begin{array}{r} 10) \quad -5x - 3y = 7 \\ \underline{-(-2x - 3y = -8)} \end{array}$$

$$(-5x + 2x) - 3y + 3y = 7 - 8$$

$$-3x = 15$$

$$x = \frac{15}{-3}$$

$$x = -5$$

$$-5x - 3y = 7$$

$$-5(-5) - 3y = 7$$

$$25 - 3y = 7$$

$$-3y = 7 - 25$$

$$-3y = -18$$

$$y = \frac{-18}{-3}$$

$$y = +6$$

# Elimination using Multiplication

Consider the system

$$\begin{aligned}x + 2y &= 6 \\3x + 3y &= -6\end{aligned}$$

How are they related?

What could we do to equation 1 to make the "x" equal?

answer



# Elimination using Multiplication

Consider the system

$$\begin{aligned}x + 2y &= 6 \\3x + 3y &= -6\end{aligned}$$

How are they related?

What could we do to equation 1 to make the "x" equal?

multiply equation 1 by 3



# Elimination using Multiplication

Consider the system

$$3x + 6y = 18$$

$$3x + 3y = -6$$

Now subtract the equations



# Elimination using Multiplication

Consider the system

$$3x + 6y = 18$$

$$\underline{-3x - 3y = +6}$$

Now subtract the equations

Answer



# Elimination using Multiplication

Consider the system

$$\begin{array}{r} 3x + 6y = 18 \\ -3x - 3y = +6 \\ \hline 3y = 24 \end{array}$$

Now subtract the equations

$$y = 8$$

Sub into equation 1 (original) or the above

$$\begin{aligned} x + 2y &= 6 \\ x + 2(8) &= 6 \\ x + 16 &= 6 \\ x &= 6 - 16 \\ x &= -10 \end{aligned}$$

$$(-10, 6)$$

You Try

1)

$$x + 2y = 5$$

$$2x + 6y = 12$$

ANS:

2)

$$\begin{aligned}x + 2y &= 4 \\x - 4y &= 16\end{aligned}$$

ANS:



## Attachments

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solutions to Day 3 WS PDF Version.pdf