

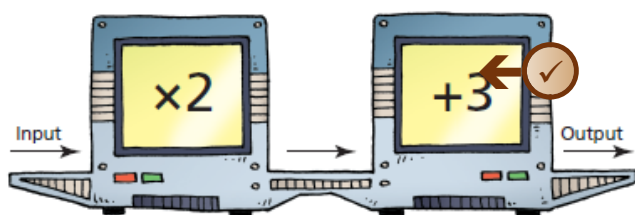
5.2 Properties of Functions



LESSON FOCUS

Develop the concept of a function.

Make Connections



Input	Output
1	5
2	7
3	9
4	11
5	13

What is the rule for the Input/Output machine above?

Which numbers would complete this table for the machine?

Remember

Independent / Dependent

Dependent - a variable whose value is determined by the value of another (independent) variable.

Independent - a variable whose value is not determined by the value of another variable, and whose value determines the value of another (dependent) variable

Complete the chart for $y = -2x + 5$

Independent x	dependent y
0	5
1	3
2	1
3	-1

Slope (with arrow pointing to the slope of the line)

Handwritten notes: Red arrows point from x=0 to x=1 and x=1 to x=2. Blue arrows point from y=5 to y=3, y=3 to y=1, and y=1 to y=-1, each labeled with "-2".

Complete the chart for $y = \frac{18x}{6}$

hint → 6
x should count by 6

x	y
0	
6	
12	

Same as $y = 3x + 4$

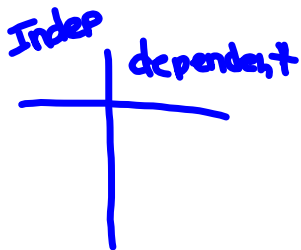
Write an equation for the chart

Independent Variable

- Hours do not depend on the person's pay.

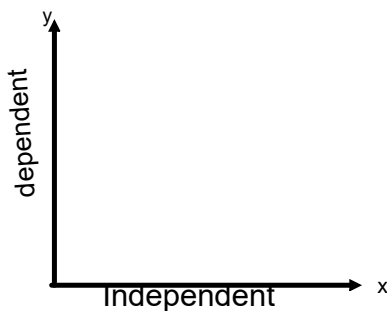
Dependent Variable

- A person's pay often depends on the number of hours worked.



Hours Worked, h	Gross Pay, P (\$)
1	12
2	24
3	36
4	48
5	60

$12x + 0$
 $P = 12h$



When graphing always

Try This!!

Domain

$\{1, 2, 3, 4, 5\}$

Range

$\{1.27, 2.54, 3.81, 5.08, 6.35, 7.62\}$

Independent	Dependent
Number of Marbles, n	Mass of Marbles, m (g)
1	1.27
2	2.54
3	3.81
4	5.08
5	6.35
6	7.62

- State the domain & Range.
- Is this relation a function? (Can't Repeat Domain) **Yes**
- State the dependent and independent variables.
- Write the function notation.

no repeats
then a function

Solution:

a) **Domain:** $\{ 1, 2, 3, 4, 5 \}$
Range: $\{ 1.75, 3.50, 5.25, 7.00, 8.75 \}$

b) **Function**

c) **Independent - number of tickets**
Dependent - Cost

d) **$C(n) = 1.75 n$**

Recall from last day



Domain & Range



Domain - the set of first elements in a relation

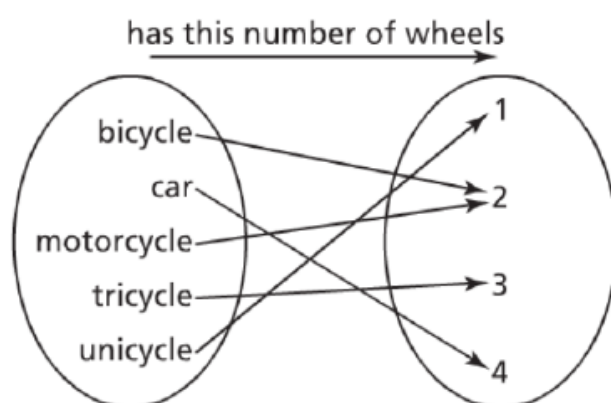
Range - the set of second elements in a relation

Indep Domain dep Range $y = 2x + 3$

Input	Output
0	3
1	5
2	7
3	9
4	11
5	13

Handwritten notes: $+1 \downarrow$ and $\downarrow +2$ are written next to the first two rows of the table.

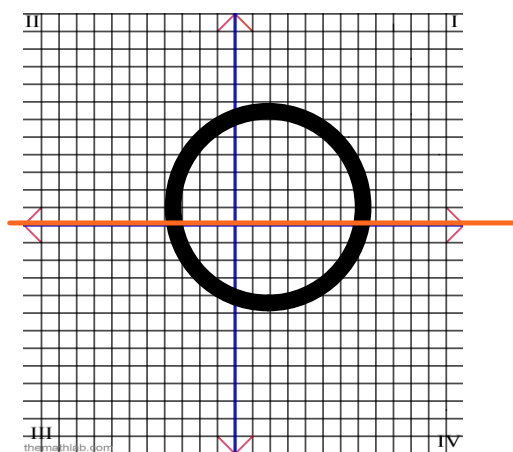
Recall from last day



Domain	The first set of elements: {bicycle, car, motorcycle, tricycle, unicycle}
Range	The second set of elements: {1, 2, 3, 4}

Recall from last day

Domain

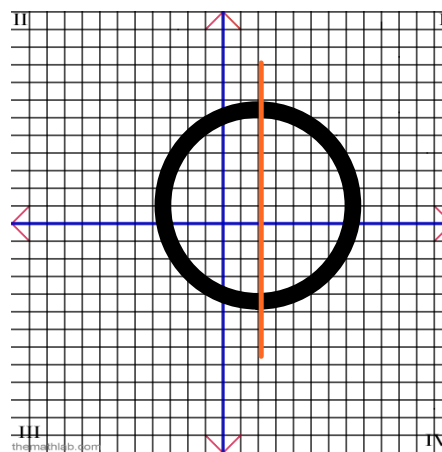


The **domain** represents all the values of x.

X is the independent Variable

$$\{x \mid _ \leq x \leq _, x \in _ \}$$

Range



The **range** represents all the values of y.

Y is the dependent Variable



How do you state the range?

$$\{y \mid y \leq 5, y \in \mathbb{R}\}$$

$$\{y \mid -5 \leq y \leq 8, y \in \mathbb{I}\}$$

MATH 10

FUNCTIONS

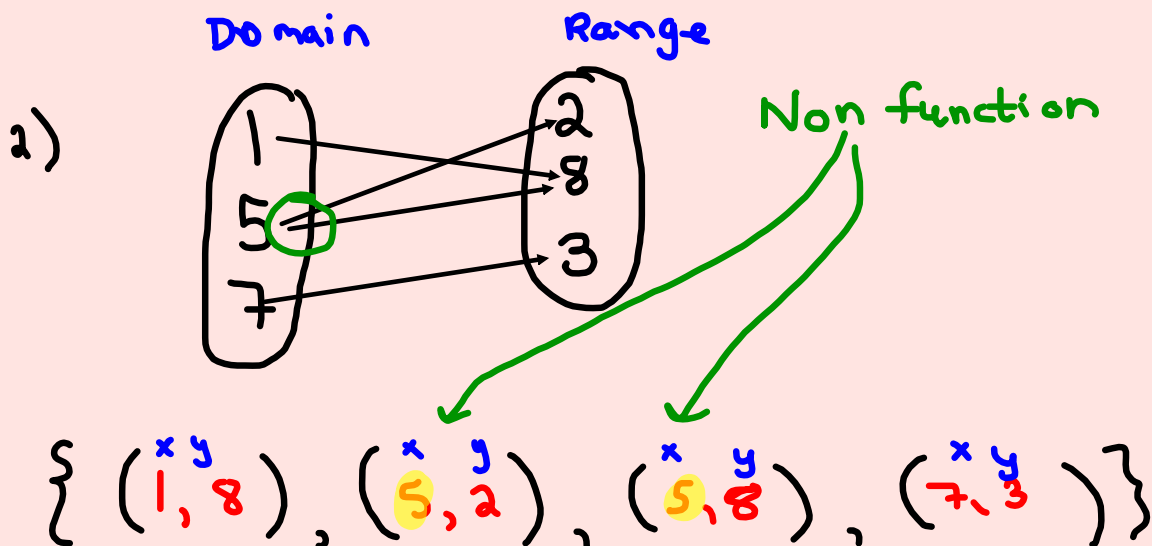
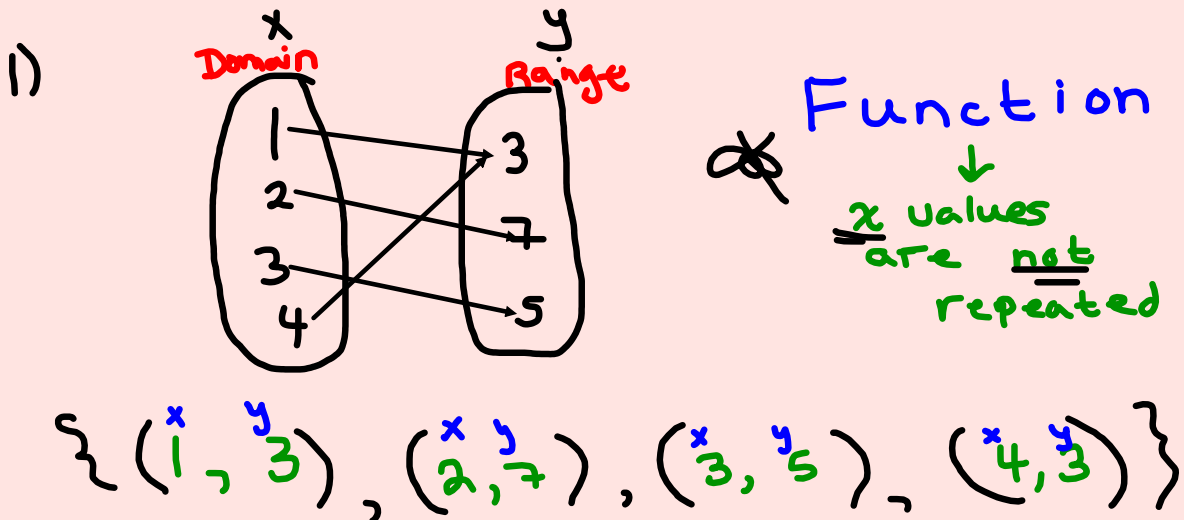
1min



Relations VS Functions

- a **relation** is where a pattern/relationship exists between the independent variable (x) and the dependent variable (y).

* a **function** is a special relationship where...
 "each x has one and only one y value".



Function or Nonfunction

Function:

A relation where each element in the first set is associated with one and only one element in the second set.

Functions

- How can I tell from a set of points/table?

"an x value has more than one y value"

- a function is a relation in which no two ordered pairs have the same first coordinate.

x	y
3	5
7	11
8	15
9	22

No x repeated

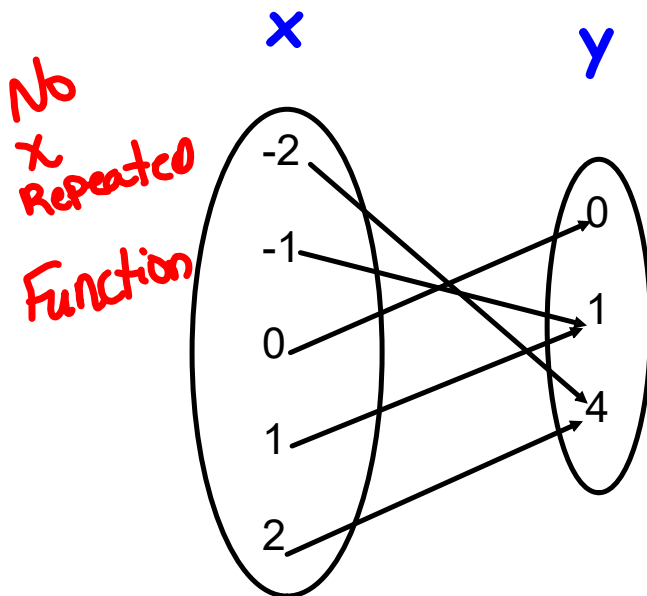
Function or Not a function
that is the question?



Arrow Diagrams

Function:

For every first element there is one and only one second element. (Only one arrow starts from each element of the domain.)



Function or Not a function
that is the question?



$(-2, 4)$, $(-1, 1)$ $(0, 0)$ $(1, 1)$ $(2, 4)$



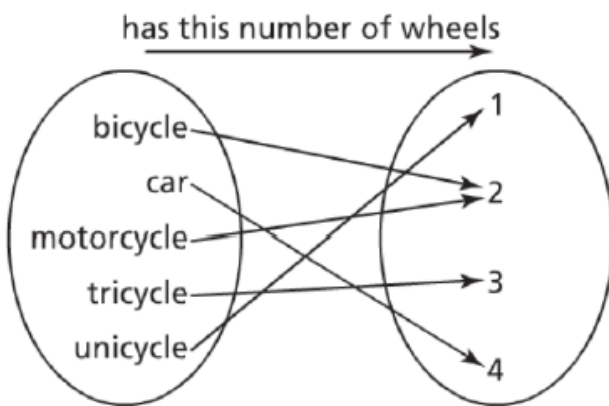
x	y
Sport	Equipment
badminton	shuttlecock
badminton	racquet
hockey	puck
hockey	stick
tennis	ball
tennis	racquet
soccer	ball

Repeat

Not a function

Function or Not a function
that is the question?





No repeats
in x
So function

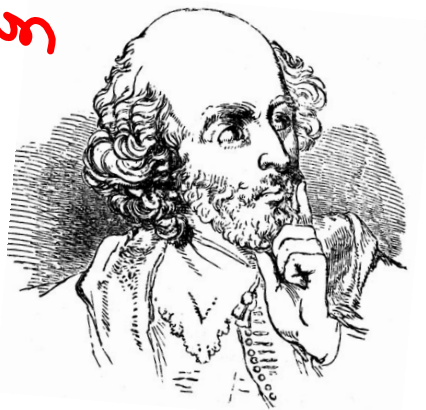
Function or Not a function
that is the question?

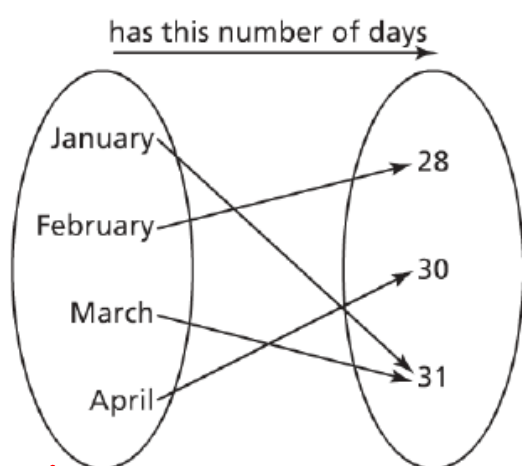


$\{ (2, 5), (3, 7), (4, 2), (2, 6), (8, 0) \}$

Repeats
of
 $x=2$
So Not
a function

Function or Not a function
that is the question?





No repeat
in x
so
function

Function or Not a function
that is the question?



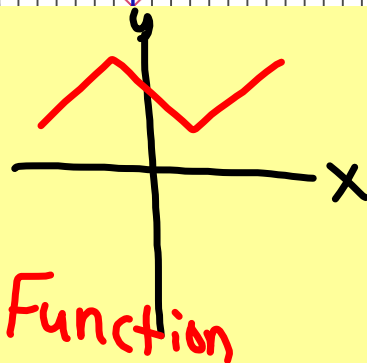
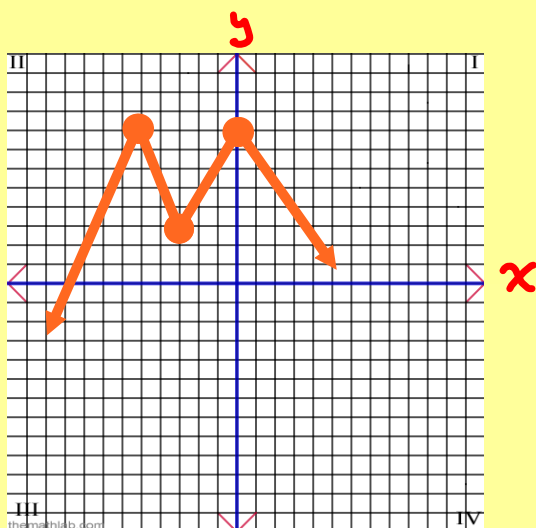
Function or Nonfunction



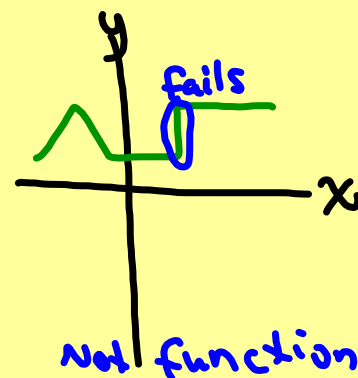
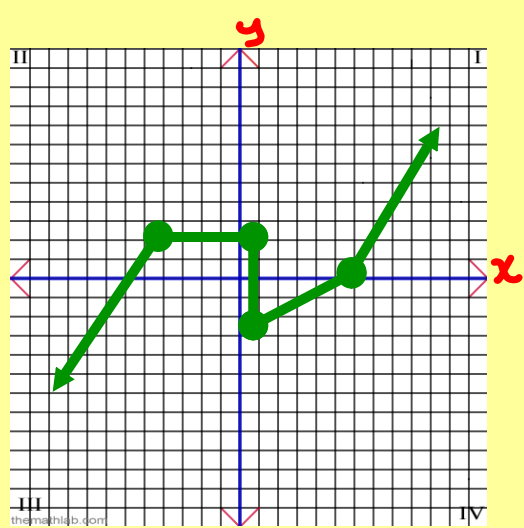
** To determine whether or not a graph is a function or nonfunction, we use what is called the vertical line test!!

** If the line crosses the graph more than once at any particular location, then it is not a function.

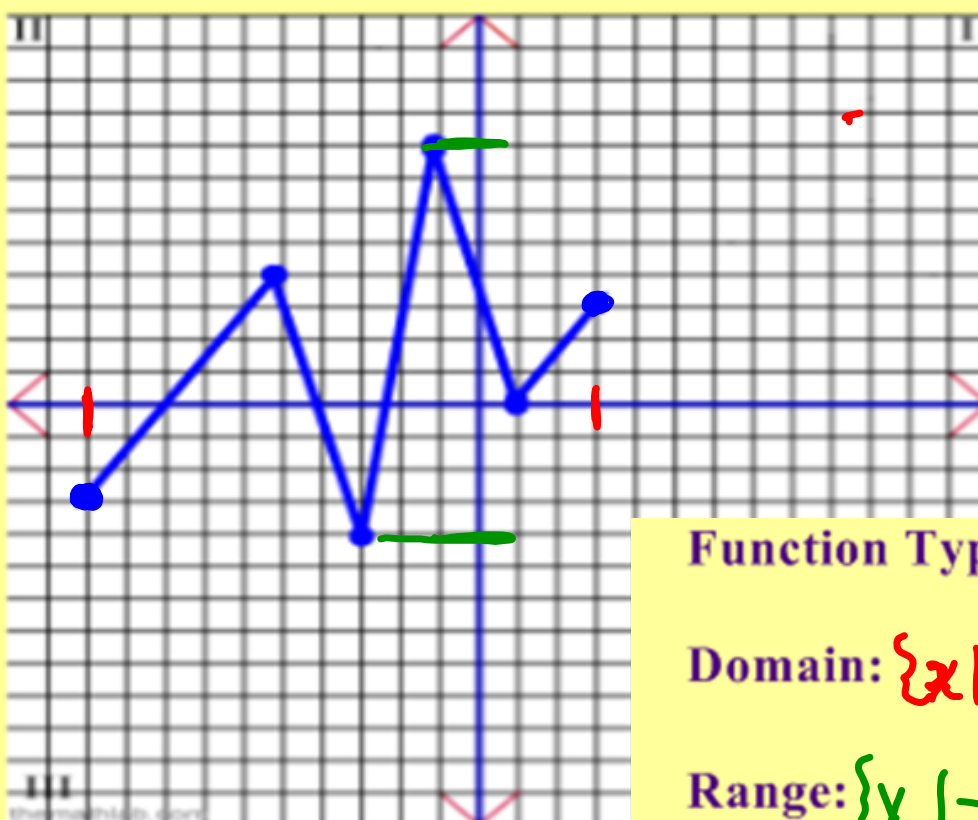
Function



Nonfunction



**** State whether the graph is a function or nonfunction, as well as stating the domain & range!!**

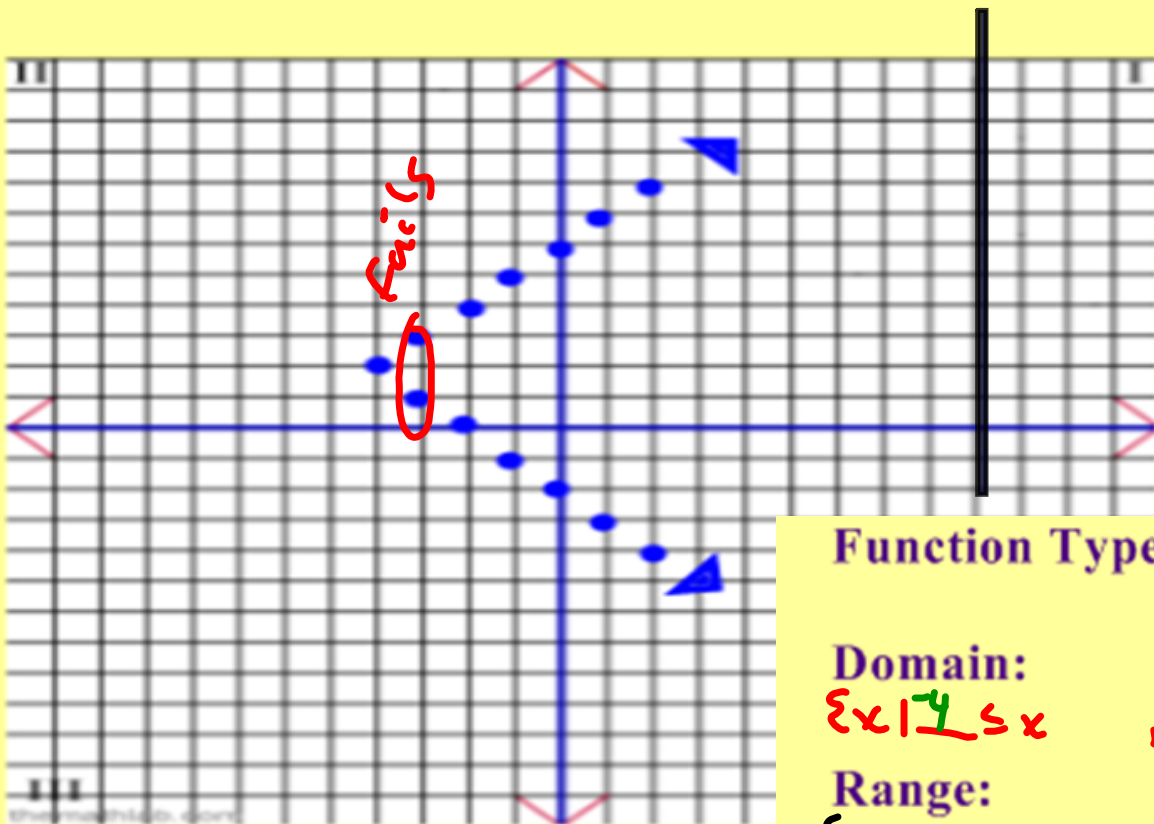


Function Type: **Function**

Domain: $\{x \mid -3 \leq x \leq 2, x \in \mathbb{R}\}$

Range: $\{y \mid -4 \leq y \leq 8, y \in \mathbb{R}\}$

* State whether the graph is a function or nonfunction, as well as stating the domain & range!!



Non-function

Function Type:

Domain:

$\{x \mid -4 \leq x$

$, x \leq 4\}$

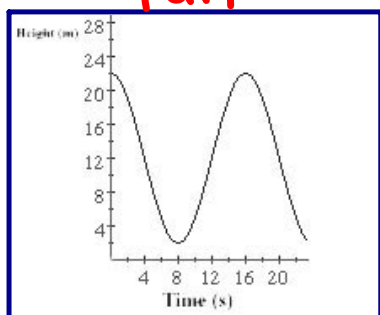
Range:

$\{y \mid$

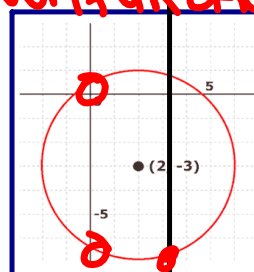
$, y \leq 4\}$

Use the Vertical Line Test to see if the graph is a function

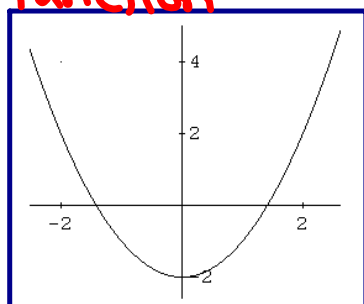
Fun



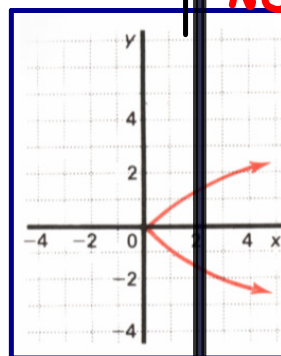
Non function



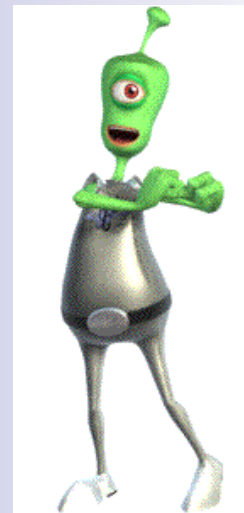
Function



Non function



Graphs
are so EASY



Homework

Page 270: Questions: 4,5,8, and Page 294: Questions: 4(a,b),7

$$\{x \mid _ \leq x \leq _, x \in _ \}$$
$$\{y \mid _ \leq y \leq _, y \in _ \}$$