

Solution to Mid Unit



Answers to Chapter 3 (Factors & Products)

- | | | | |
|------------------------------------|----------------------------------|----------------------------|--------------------|
| 1) $(k-10)(k-3)$ | 2) $(k-1)(k-8)$ | 3) $(x-1)(x+5)$ | 4) $(n-5)(n-2)$ |
| 5) $(x-10)(x-6)$ | 6) $(n+5)(n+7)$ | 7) $(x-7)(x-6)$ | 8) $(p+10)(p+3)$ |
| 9) $(2n-9)(n-3)$ | 10) $(7n+5)(n+8)$ | 11) $(7n-10)(n+8)$ | 12) $(7b-6)(b+3)$ |
| 13) $(3x+1)(x-9)$ | 14) $(3n-10)(n+3)$ | 15) $4(7k-5)(k+7)$ | 16) $4\sqrt{7v-9}$ |
| 17) $10y^4(8-x^2y^2+y)$ | 18) $7x(xy+7x-6)$ | 19) $4x^3(-3y^6-10xy^2+7)$ | |
| 20) $3(m^4n-8n^2-6)$ | 21) $5m^2n^2(m^3-4mn-1)$ | 22) $7b^3(-4+9ab+2a)$ | |
| 23) $9ac(-4a^5bc^3-3bc^2+4c^2-12)$ | 24) $6p^4(-11q^2r+2p^3+11pr-11)$ | | |
| 25) $56b^2+49b-7$ | 26) $56b^2-120b+64$ | 27) $16n^2+4n-30$ | 28) $64x^2+56x+6$ |
| 29) $40a^3-4a^2+8a-12$ | 30) $14p^3+64p^2+18p-56$ | | |

3.6 Polynomials of the Form $ax^2 + bx + c$



Worksheet: GCF, Simple Trinomials & Hard Trinomials
Questions: 1-12

Math 10

Name _____

GCF, Simple Trinomials, Hard Trinomials

Date _____

Choose a factoring Method and factor each completely:

1) $-9n^5 + 6n^3$

2) $36r^6 + 54r - 45$

3) $-40 + 4b^2 - 32b^4$

4) $4xy^2 + 20x^2y + 16xy$

5) $x^2 + 13x + 42$

6) $x^2 + 13x + 36$

7) $k^2 + k - 12$

8) $a^2 + 4a - 45$

9) $2p^2 + 11p - 63$

10) $3n^2 + 11n - 20$

11) $4n^2 - 4n - 15$

12) $6n^2 - 29n + 20$

$$1) -9n^5 + 6n^3$$
$$3n^3(-3n^2 + 2)$$

$$2) 36r^6 + 54r - 45$$
$$9(4r^6 + 6r - 5)$$

$$3) -40 + 4b^2 - 32b^4$$
$$4(-10 + b^2 - 8b^4)$$

$$4) 4xy^2 + 20x^2y + 16xy$$
$$4xy(y + 5x + 4)$$

$$5) x^2 + 13x + 42$$
$$(x + 6)(x + 7)$$

$$6) x^2 + 13x + 36$$
$$(x + 9)(x + 4)$$

$$7) k^2 + k - 12$$
$$(k + 4)(k - 3)$$

$$8) a^2 + 4a - 45$$
$$(a - 5)(a + 9)$$

$$9) 2p^2 + 11p - 63$$
$$(2p - 7)(p + 9)$$

$$10) 3n^2 + 11n - 20$$
$$(3n - 4)(n + 5)$$

$$11) 4n^2 - 4n - 15$$
$$(2n + 3)(2n - 5)$$

$$12) 6n^2 - 29n + 20$$
$$(n - 4)(6n - 5)$$

3.8 Factoring Special Polynomials

Difference of Squares

- two terms that are perfect squares.
- must be a difference
- factor like this...

$$a^2 - b^2 = (a + b)(a - b)$$

EXAMPLES...

$$1) \quad (2x)^2 - (7)^2$$

$$(2x+7)(2x-7)$$

check

$$4x^2 - 14x + 14x - 49$$

$$4x^2 - 49$$

$$3) \quad 81z^4 - 625$$

$$(9z^2)^2 - (25)^2$$

$$(9z^2+25)(9z^2-25)$$

$$2) \quad (4x)^2 - (3y)^2$$

$$(4x+3y)(4x-3y)$$

$$4) \quad 49w^2 - 4s^2$$

$$(7w)^2 - (2s)^2$$

$$(7w+2s)(7w-2s)$$

Perfect Square Trinomials

- three terms: the first and last are perfect squares.
- factors like this...

check

$$\begin{aligned} (x-2)^2 &= (x-2)(x-2) \\ &= x^2 - 2x - 2x + 4 \\ &= x^2 - 4x + 4 \end{aligned}$$

perfect square #

$2(-)(2)$

$$a^2 + 2ab + b^2 = (a + b)^2$$

OR

$$a^2 - 2ab + b^2 = (a - b)^2$$

- recognize them and you save yourself the decomposition steps!!!

EXAMPLES...

1) $25x^2 - 10x + 1$

$(5x)^2$ $2x(5x)$ $(1)^2 \leftarrow \text{Notice}$

$$(5x - 1)^2$$

2) $9x^2 + 24x + 16$

$(3x)^2$ $2(3x)(4)$ $(4)^2$

Double of 3+4

$$(3x + 4)^2$$

Decomposition Still works

$$\begin{aligned} &25x^2 - 10x + 1 \quad \begin{array}{l} \text{mult} \quad \text{add} \\ +25 \quad -10 \end{array} \\ &\underline{25x^2 - 5x} \quad \underline{-5x + 1} \quad \begin{array}{l} 1 \times 25 \\ -5 \times 5 \end{array} \\ &5x(5x-1) - 1(5x-1) \\ &\underline{(5x-1)} \quad \underline{(5x-1)} \\ &(5x-1)^2 \end{aligned}$$

Factor using Perfect Squares Method

$$\begin{array}{cc} (5x)^2 & (12)^2 \\ \uparrow & \uparrow \\ 25x^2 - 120x + 144 \end{array}$$

$$(5x - 12)^2$$

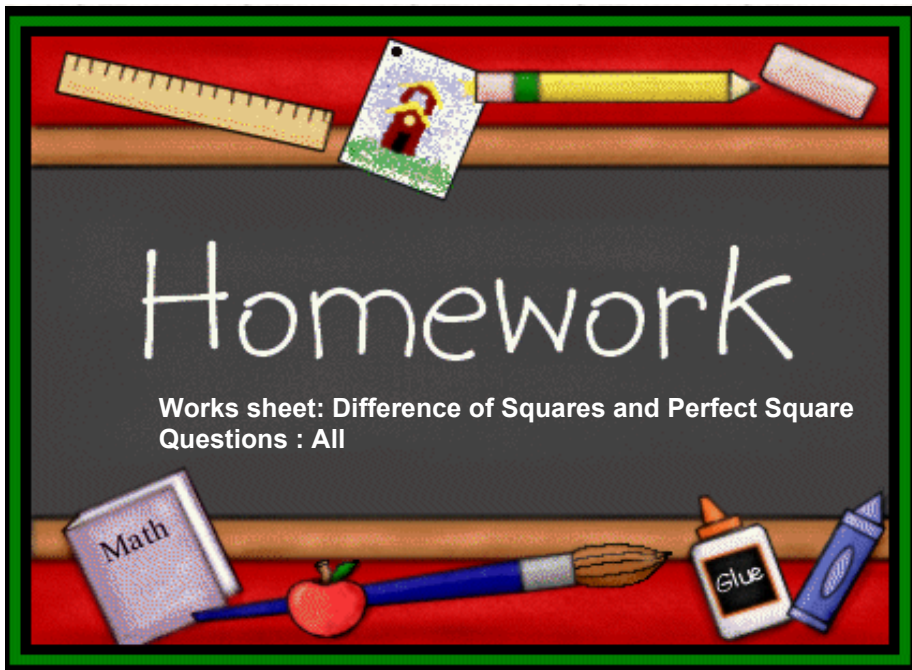
$$\begin{array}{cc} (9x)^2 & (10)^2 \\ \uparrow & \uparrow \\ 81x^2 - 180x + 100 \end{array}$$

$$(9x - 10)^2$$

$$\begin{array}{cc} (7x)^2 & (6)^2 \\ \uparrow & \uparrow \\ 49x^2 + 84x + 36 \end{array}$$

$$(7x + 6)^2$$

$$36x^2 + 132x + 121$$



Math 10

Name _____

Factoring: Difference of Squares and Perfect Squares

Date _____

Factor each completely.

1) $n^2 - 9$

$$(n)^2 - (3)^2$$
$$(n-3)(n+3)$$

3) $k^2 - 4$

5) $x^2 - 25$

7) $u^2 - 16v^2$ $(u - 4v)(u + 4v)$

9) $4x^2 - y^2$
 $(2x - y)(2x + y)$

11) $9m^2 + 12m + 4$
 $(3m + 2)^2$

13) $25x^2 - 20x + 4$

15) $9b^2 - 24b + 16$

17) $9x^2 - 6xy + y^2$ $(3x - y)^2$

19) $x^2 - 8xy + 16y^2$

2) $25a^2 - 9$ $(5a)^2 - (3)^2$ $(5a + 3)(5a - 3)$

4) $16x^2 - 9$ $(4x)^2 - (3)^2$ $(4x - 3)(4x + 3)$

6) $25x^2 - 16y^2$
 $(5x - 4y)(5x + 4y)$

8) $u^2 - 9v^2$
 $(u - 3v)(u + 3v)$

10) $a^2 - 25b^2$
 $(a - 5b)(a + 5b)$

12) $16r^2 + 8r + 1$

14) $16n^2 + 40n + 25$

16) $16m^2 - 24mn + 9n^2$

18) $25x^2 + 10xy + y^2$

20) $9x^2 + 24xy + 16y^2$

Chapter 3 (Factors & Products) Review.pdf