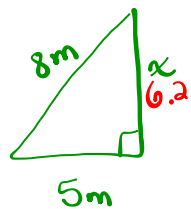
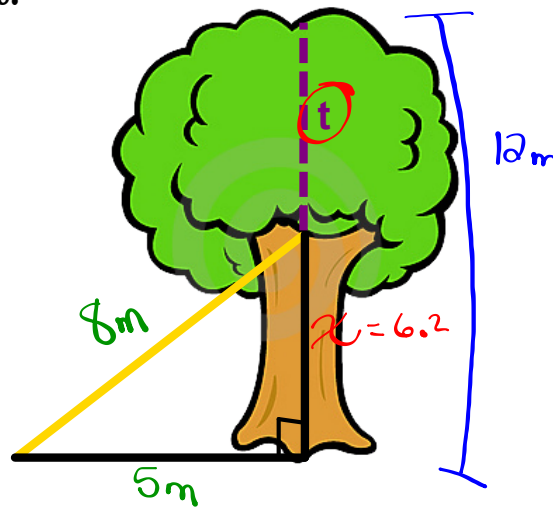


# Warm Up

To support the tree, a guy wire 8 m long is attached to the trunk and then secured in the ground 5 m from the base of the tree. The tree is 12 m in height. Find "t" to the nearest tenth of a metre.



$$c^2 = a^2 + b^2$$

$$a^2 = c^2 - b^2$$

$$a^2 = c^2 - b^2$$

$$= 8^2 - 5^2$$

$$a^2 = 64 - 25$$

$$a^2 = 39$$

$$\sqrt{a^2} = \sqrt{39}$$

$$a = 6.2$$

$$t = 12 - 6.2$$

$$t = 5.8$$

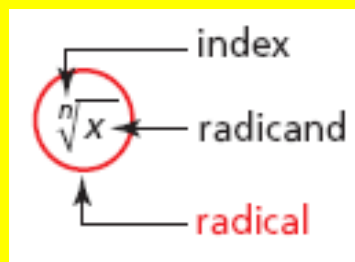
$$t \text{ is } 5.8 \text{ m}$$



# What do you know???

$$\sqrt{36} = 6$$

$$\sqrt[3]{64} = 4$$



Exponent Button  
 $x^y$  or  $y^x$

Root button

$$\sqrt[4]{64} = 2.8284 \dots$$

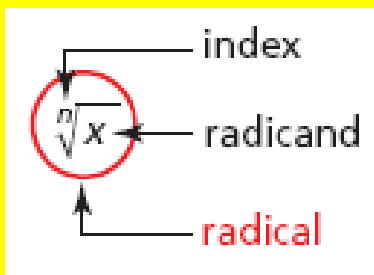


# What do you know???

$$\sqrt[2]{\frac{144}{196}} = \frac{\sqrt{144}}{\sqrt{196}} = \frac{12}{14} \begin{matrix} \div 2 \\ \div 2 \end{matrix} \rightarrow \boxed{\frac{6}{7}}$$

Reduce

$$\sqrt[3]{\frac{125}{1000}} = \frac{\sqrt[3]{125}}{\sqrt[3]{1000}} = \frac{5}{10} \begin{matrix} \div 5 \\ \div 5 \end{matrix} = \frac{1}{2}$$





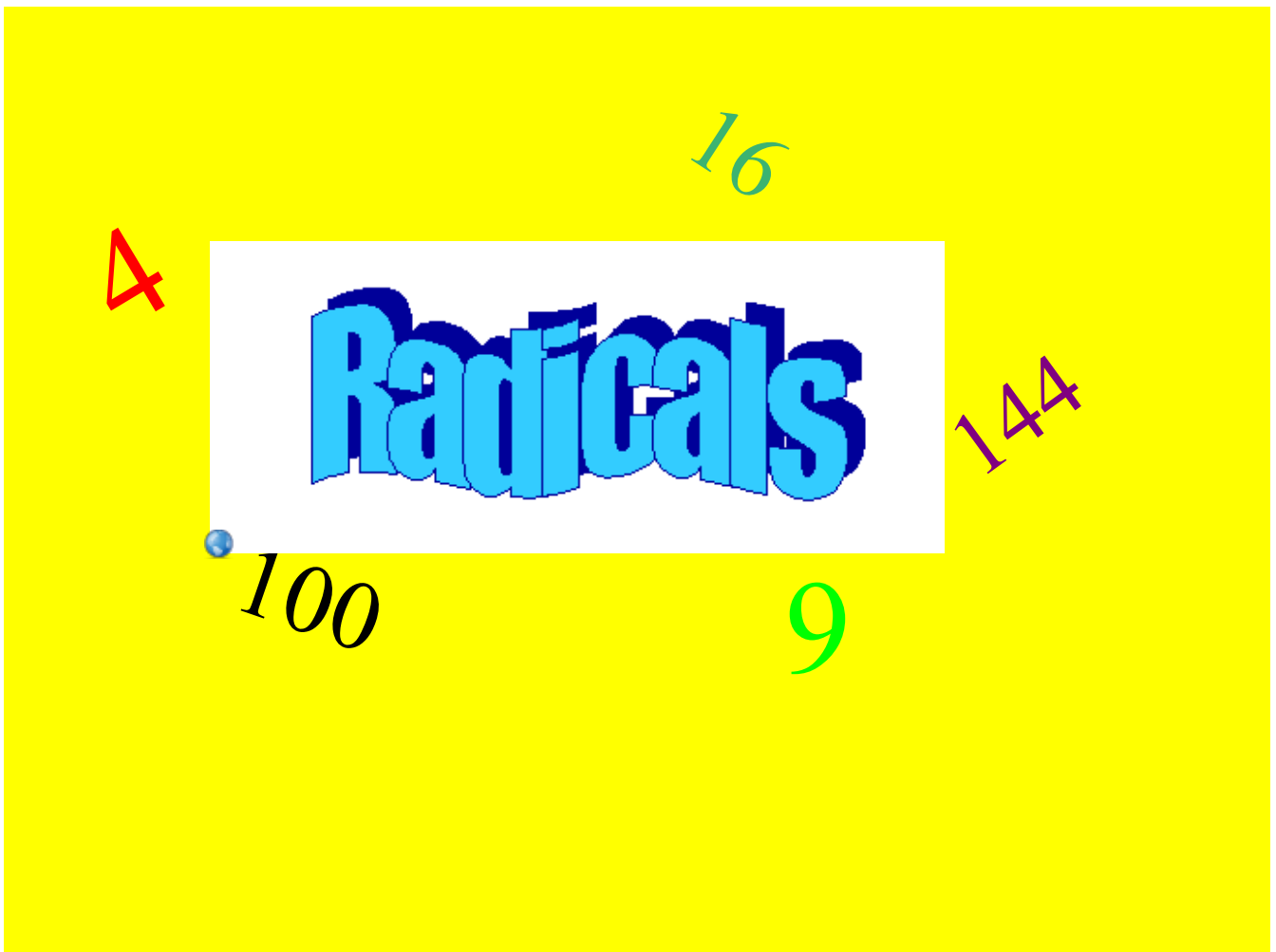
**TRY THIS**      **Have already**

Determine the value of each radical.

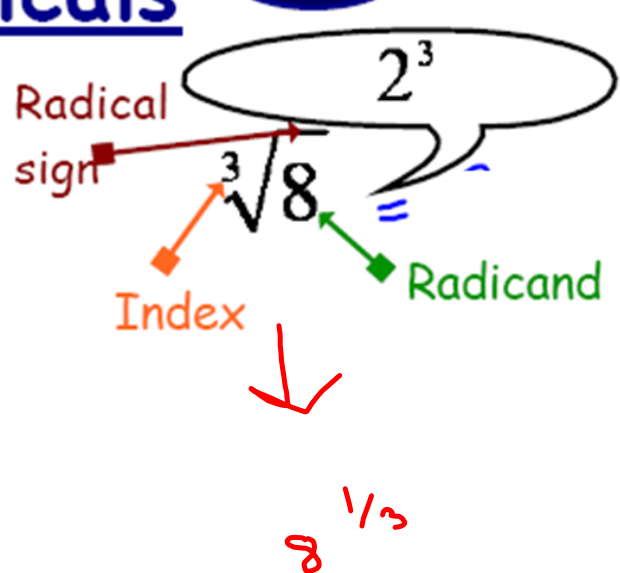
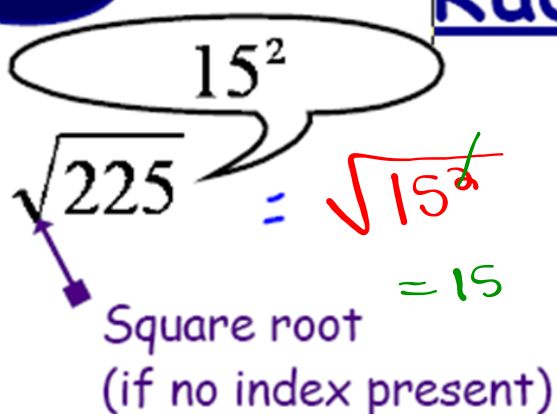
Radical	Value	Is the Value Exact or Approximate?
$\sqrt{16}$	4	Ex
$\sqrt{27}$	5.1	App
$\sqrt{\frac{16}{81}}$	$\frac{\sqrt{16}}{\sqrt{81}} = \frac{4}{9}$	Ex
$\sqrt{0.64}$	$\frac{\sqrt{64}}{\sqrt{100}} = \frac{8}{10} = 0.8$	Exact
$\sqrt[3]{16}$	2.3...	App
$\sqrt[3]{27}$	3	Ex
$\sqrt[3]{\frac{16}{18}}$	$\frac{\sqrt[3]{16}}{\sqrt[3]{18}}$ Round	App

Use fractions to help

Use cube numbers list to help



# Radicals



# Radicals

Write a fraction that is equivalent to:

$$\frac{3}{4} \quad \frac{6}{8} \quad \frac{9}{12} \quad \frac{12}{16}$$

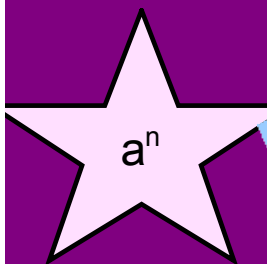
Just as with fractions, Radicals expressions have equivalent expressions:

$$\sqrt{144} \leftarrow \begin{array}{l} \sqrt{16 \cdot 9} \\ = \sqrt{16} \cdot \sqrt{9} \\ = 4 \cdot 3 \\ = 12 \end{array} \text{ or } \begin{array}{l} \sqrt{16 \cdot 9} = \sqrt{144} \\ = 12 \end{array}$$

Same works if we change the "index":

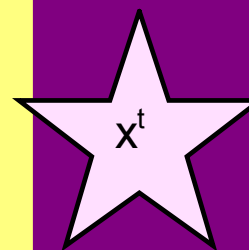
$$\sqrt[3]{8 \cdot 27} = \begin{array}{l} \text{Separate} \\ \sqrt[3]{8} \cdot \sqrt[3]{27} \\ = \sqrt[2]{8} \cdot 3 \\ = 6 \end{array} \text{ or } \begin{array}{l} \sqrt[3]{8 \cdot 27} = \sqrt[3]{216} \\ = 6 \end{array}$$

*look in perfect cube list*



# POWERS

From last day



$$1^0 = 1$$

$$1^1 = 1$$

$$1^2 = 1$$

$$1^3 = 1$$

$$1^4 = 1$$

$$1^5 = 1$$

$$2^0 = 1$$

$$2^1 = 2$$

$$2^2 = 4$$

$$2^3 = 8$$

$$2^4 = 16$$

$$2^5 = 32$$

$$3^0 = 1$$

$$3^1 = 3$$

$$3^2 = 9$$

$$3^3 = 27$$

$$3^4 = 81$$

$$3^5 = 243$$

$$4^0 = 1$$

$$4^1 = 4$$

$$4^2 = 16$$

$$4^3 = 64$$

$$4^4 = 256$$

$$4^5 = 1024$$

$$5^0 = 1$$

$$5^1 = 5$$

$$5^2 = 25$$

$$5^3 = 125$$

$$5^4 = 625$$

$$5^5 = 3125$$

$$6^0 = 1$$

$$6^1 = 6$$

$$6^2 = 36$$

$$6^3 = 216$$

$$6^4 = 1296$$

$$6^5 = 7776$$

$$7^0 = 1$$

$$7^1 = 7$$

$$7^2 = 49$$

$$7^3 = 343$$

$$7^4 = 2401$$

$$7^5 = 16807$$

$$8^0 = 1$$

$$8^1 = 8$$

$$8^2 = 64$$

$$8^3 = 512$$

$$8^4 = 4096$$

$$8^5 = 32768$$

$$9^0 = 1$$

$$9^1 = 9$$

$$9^2 = 81$$

$$9^3 = 729$$

$$9^4 = 6561$$

$$9^5 = 59049$$

$$10^0 = 1$$

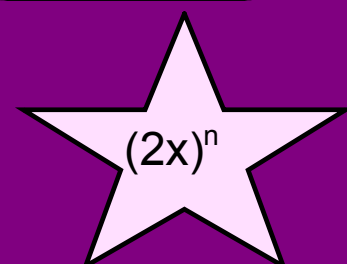
$$10^1 = 10$$

$$10^2 = 100$$

$$10^3 = 1000$$

$$10^4 = 10000$$

$$10^5 = 100000$$





# Reducing Radicals

## Multiplication Property of Radicals

$$\sqrt[n]{ab} = \sqrt[n]{a} \cdot \sqrt[n]{b},$$

where  $n$  is a natural number, and  $a$  and  $b$  are real numbers

Same works if we change the "index":

$$\begin{aligned}\sqrt[3]{8 \cdot 27} &= \sqrt[3]{8} \cdot \sqrt[3]{27} \\ &= 2 \cdot 3 \\ &= 6\end{aligned}$$

or

$$\begin{aligned}\sqrt[3]{8 \cdot 27} &= \sqrt[3]{216} \\ &= 6\end{aligned}$$

NEED in front of you perfect squares, cubes

Evaluate each radical. Justify you answer

a)  $\sqrt{64} = 8$       b)  $\sqrt[4]{81} = 3$       c)  $\sqrt[3]{27} = 3$

Rewrite

$$= \sqrt{16 \cdot 4}$$
$$= \sqrt{16} \cdot \sqrt{4}$$
$$= 4 \cdot 2$$
$$= 8$$

$\quad \quad \quad =$

Estimate to one decimal

$\sqrt[3]{9}$

$\sqrt[3]{8}$        $\sqrt[3]{27}$

$\Downarrow$        $\Downarrow$

    2      3

$\approx 2.2$

cal 2.08

b)  $\sqrt[5]{1562}$

$\sqrt[5]{1024}$        $\sqrt[5]{3125}$

$\Downarrow$        $\Downarrow$

    4      5

$4.2$

$$1^4 = 1$$

$$2^4 = 16$$

$$3^4 = 81$$

$$4^4 = 256$$

$$5^4 = 625$$

$$6^4 = 1296$$

$$7^4 = 2401$$

$$8^4 = 4096$$

⋮

$$1^5 = 1$$

$$2^5 = 32$$

$$3^5 = 243$$

$$4^5 = 1024$$

$$5^5 = 3125$$

$$6^5 = 7776$$

$$7^5 = 16807$$

$$8^5 = 32768$$

Remember

**Rational numbers** are numbers that can be written as a fraction or is a decimal that repeats or terminates. Ex)  $\sqrt[4]{\frac{1296}{10000}}$  Ex)  $\sqrt[3]{\frac{8}{27}}$

**Irrational numbers** are numbers that cannot be written as a fraction and its decimal neither terminates or repeats.  $\sqrt{28}$

## Class Work/Homework

Page 206 # ~~1 to #6~~# 2 a c d e f  
3 c d f

$$2a) \sqrt{36} = 6$$
$$\sqrt{4} \cdot \sqrt{9}$$
$$2 \cdot 3$$
$$6$$

$$\sqrt[4]{10000} = 10$$

$$\sqrt[4]{625} \cdot \sqrt[4]{4}$$
$$5 \cdot 2$$
$$10$$

**STOP**