

GCF

When Comparing 2 or More Numbers....

GCF - Greatest Common Factor

Is the largest COMMON number that will divide into each

- you can list the factors or use prime factorization trees

Prime Factorization

Ex) GCF (6,12) =

12

6

12 =

Underline the common primes (then multiply them and that give you the GCF)

LCM

When Comparing 2 or More Numbers....

LCM - Lowest Common Multiple

Is the largest COMMON multiple

- you can list the multiples of each number and circle the common multiple that fall on all list Prime Factorization

or

use prime factorization trees

- use maximum # of primes in each list

WATCH The video for description

<https://www.khanacademy.org/math/algebra2/rational-expressions-equations-and-functions/adding-and-subtracting-rational-expressions/v/least-common-multiple-exercise>



Prime Factorization

18

12

Ex) GCF (18,12) = ?

Both have
so take largest
power of each

1)) Find the

- a) GCF (24, 40) b) GCF (84, 60) c) GCF (36, 90, 126)

1)) Find the

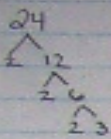
- a) LCM (15,40) b) LCM (12,15) c) LCM (9, 14, 63)

Factor Worksheet

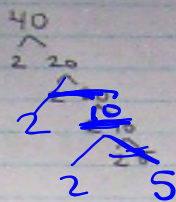
GCF \Rightarrow Circle ^{all} common primes (even repeats) (multiple)

LCM \Rightarrow List prime & used then take the maximum exponent used
 1
 (multiple)

1) GCF(24, 40)



$$24 = \underbrace{2 \times 2 \times 2}_{2^3} \times 3$$



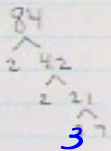
$$40 = 2 \times 2 \times 2 \times 5 = 2^3 \times 5$$

\rightarrow Look at common amount of primes must appear in both

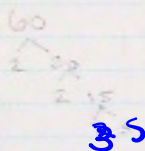
$$\begin{aligned} \text{GCF}(24, 40) &= 2 \times 2 \times 2 \\ &= 2^3 \leftarrow \text{appears in both} \\ &= 8 \end{aligned}$$

$$\begin{aligned} \text{LCM}(24, 40) &= 2^3 \times 3 \times 5 \\ &= \overbrace{8}^{\text{primes seen}} \times 3 \times 5 \\ &= 120 \end{aligned}$$

2) GCF(84, 60)



$$84 \Rightarrow 2 \times 2 \times 3 \times 7$$

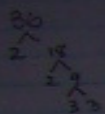


$$60 \Rightarrow 2 \times 2 \times 3 \times 5$$

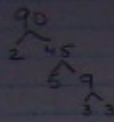
$$\begin{aligned} \text{GCF}(84, 60) &= 2 \times 2 \times 3 \\ &= 4 \times 3 \\ &= 12 \end{aligned}$$

$$\begin{aligned} \text{LCM}(84, 60) &= 2^2 \times 3 \times 5 \times 7 \\ &= 4 \times 3 \times 5 \times 7 \\ &= 12 \times 5 \times 7 \\ &= 420 \end{aligned}$$

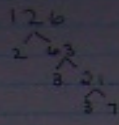
c) GCF (36, 90, 126)



$$36 = 2 \times 2 \times 3 \times 3 \\ = 2^2 \times 3^2$$



$$90 = 2 \times 3 \times 3 \times 5 \\ = 2^1 \times 3^2 \times 5^1$$

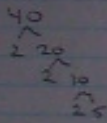


$$126 = 2 \times 3 \times 3 \times 7 \\ = 2^1 \times 3^2 \times 7^1$$

$$\begin{aligned} \text{GCF}(36, 90, 126) &= 2 \times 3^2 \\ &= 2 \times 9 \\ &= 18 \end{aligned}$$

$$\begin{aligned} \text{LCM}(36, 90, 126) &= 2^2 \times 3^2 \times 5^1 \times 7^1 \\ &= 2 \times 9 \times 5 \times 7 \\ &= 630 \end{aligned}$$

d) LCM (15, 40)



$$15 = 3 \times 5$$

$$40 = 2 \times 2 \times 2 \times 5 \\ = 2^3 \times 5$$

$$\begin{aligned} \text{LCM}(15, 40) &= 2^3 \times 3^1 \times 5^1 \\ &= 8 \times 3 \times 5 \\ &= 120 \end{aligned}$$

$$\text{GCF}(15, 40) = 5$$

2) b) LCM (12, 15)

$$\begin{array}{c} 12 \\ \swarrow \searrow \\ 2 \quad 6 \\ \quad \swarrow \searrow \\ \quad 2 \quad 3 \end{array}$$

$$\begin{array}{c} 15 \\ \swarrow \searrow \\ 3 \quad 5 \end{array}$$

$$12 = 2 \times 2 \times 3 \\ = 2^2 \times 3$$

$$15 = 3 \times 5$$

$$\begin{aligned} \text{LCM}(12, 15) &= 2^2 \times 3^1 \times 5^1 \\ &= 4 \times 3 \times 5 \\ &= 60 \end{aligned}$$

$$\text{GCF}(12, 15) = 3$$

c) LCM(9, 14, 63)

$$\begin{array}{c} 9 \\ \swarrow \searrow \\ 3 \quad 3 \end{array}$$

$$\begin{array}{c} 14 \\ \swarrow \searrow \\ 2 \quad 7 \end{array}$$

$$\begin{array}{c} 63 \\ \swarrow \searrow \\ 3 \quad 21 \\ \quad \swarrow \searrow \\ \quad 3 \quad 7 \end{array}$$

$$9 = 3 \times 3 \\ = 3^2$$

$$14 = 2 \times 7$$

$$63 = 3 \times 3 \times 7 \\ = 3^2 \times 7$$

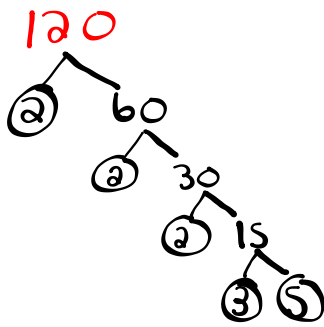
$$\begin{aligned} \text{LCM}(9, 14, 63) &= 2^1 \times 3^2 \times 7^1 \\ &= 2 \times 9 \times 7 \\ &= 126 \end{aligned}$$

$$\text{GCF}(9, 14, 63) = \text{None}$$

Warm Up

Sept. 28, 2017

Find the GCF (120, 960, 1400)



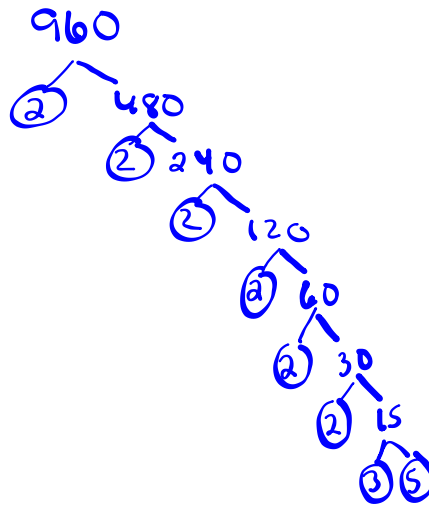
$$120 = 2 \times 2 \times 2 \times 3 \times 5$$

$$= 2^3 \times 3^1 \times 5^1$$

$$\text{GCF}(120, 960, 1400)$$

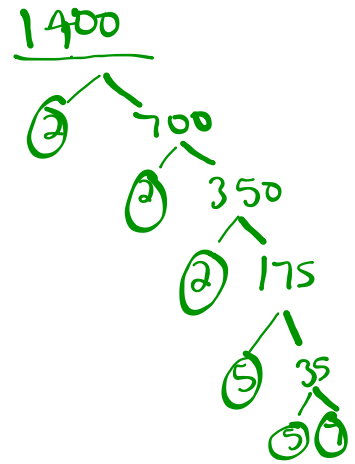
$$= 2^3 \times 5^1$$

$$= 8 \times 5$$



$$960 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 5$$

$$= 2^6 \times 3 \times 5$$



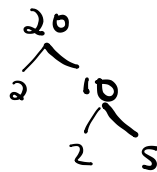
$$1400 = 2 \times 2 \times 2 \times 5 \times 5 \times 7$$

$$= 2^3 \times 5^2 \times 7$$

Find the LCM (15, 20, 24, 27)

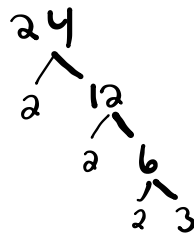


$$15 = 3 \times 5$$



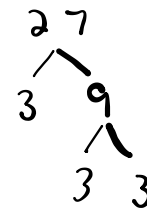
$$20 = 2 \times 2 \times 5$$

$$= 2^2 \times 5$$



$$24 = 2 \times 2 \times 2 \times 3$$

$$= 2^3 \times 3$$



$$27 = 3 \times 3 \times 3$$

$$= 3^3$$

$$\text{GCF}(15, 20, 24, 27) = \text{None}$$

$$\text{LCM}(15, 20, 24, 27) = 2^3 \times 3^3 \times 5^1$$

$$= 8 \times 27 \times 5$$

$$= 1080$$

Video On GCF & LCM

 <https://www.youtube.com/watch?v=NFHEH2rzSJo>

$$\begin{array}{r} 18 \\ 24 \\ \hline \text{GCF} \\ \hline 6 \end{array} \quad \begin{array}{r} 24 \\ \hline \end{array}$$

$$\begin{array}{l} \text{LCM} \\ 18 \rightarrow \\ 24 \rightarrow \end{array}$$

h

GCF =

Box/Ladder Method

2	18	24
3	9	12
	3	4

$$\text{GCF} = 2 \times 3 = 6$$

$$\begin{aligned} \text{LCM} &= 2 \times 3 \times 3 \times 4 \\ &= 72 \end{aligned}$$

Homework

Exercises page 140

A

3 a, b, c
 4
 5 b, c

B

a, c
 6
 7
 8
 9 a, c
 10 a, c, e
 11
 12
~~13~~
 14
 15 a, d
 16 a
 17
 18
 20

Box → Ladder
 Factor tree

4 abc
 5 bc
 6 ac
 8 ab
 9 ac
 10 ace
 15 ad
 16 a

C

21 22