

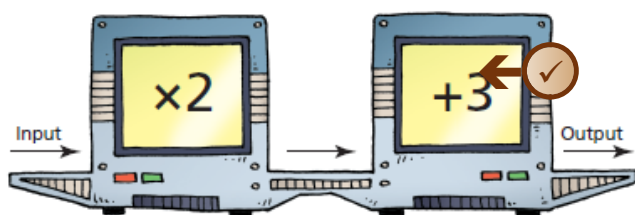
## 5.2 Properties of Functions



### LESSON FOCUS

Develop the concept of a function.

### Make Connections



Input	Output
1	5
2	7
3	9
4	11
5	13

What is the rule for the Input/Output machine above?

Which numbers would complete this table for the machine?

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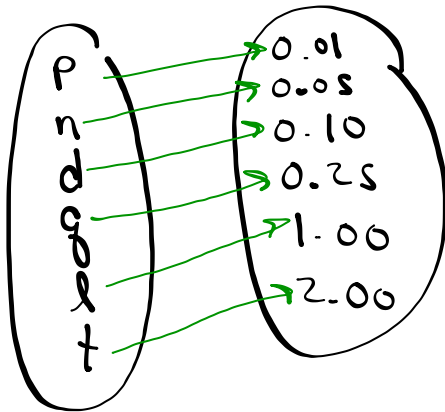
3 i)

x	y
Coin	Value
penny	0.01
nickel	0.05
dime	0.10
quarter	0.25
loonie	1.00
toonie	2.00

i) ordered pair coin first then value 2<sup>nd</sup>.  
Comparing the coin to its value

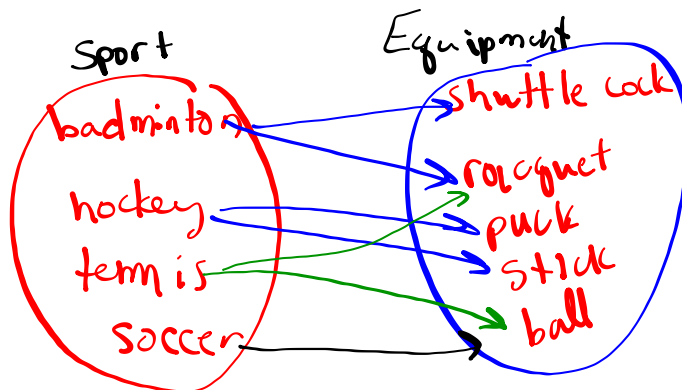
(x, y)

ii) { (penny, 0.01), (nickel, 0.05), (dime, 0.10), (quarter, 0.25), (loonie, 1.00), (toonie, 2.00) }



3b) i) Compare Sports to the equipment that they use  
Ordered pair Sports first, then equipment second.

ii) { (bad, shuttlecock), (badminton, racket), (hockey, stick), (tennis, ball), (tennis, racket), (soccer, ball) }



# <sup>x</sup>Independent / <sup>y</sup>Dependent

$$y = 3x + 1$$

**Dependent**  
<sup>y</sup>

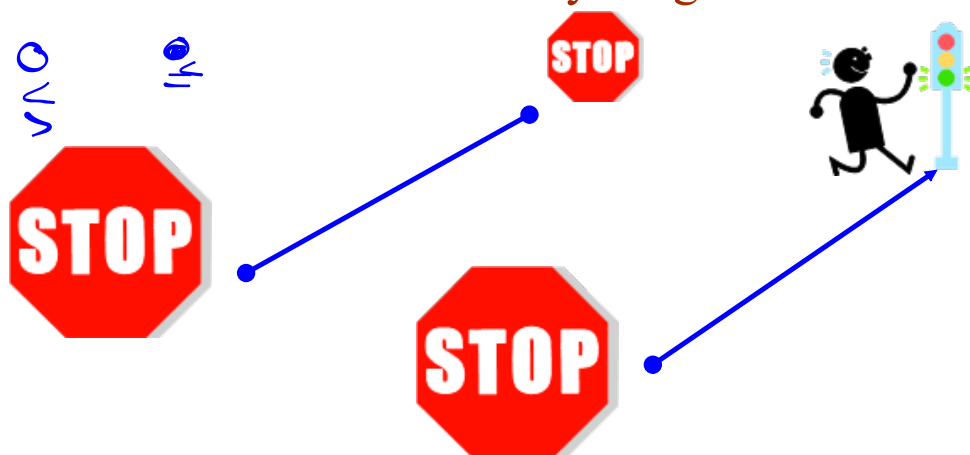
- a variable whose value is determined by the value of another (independent) variable.

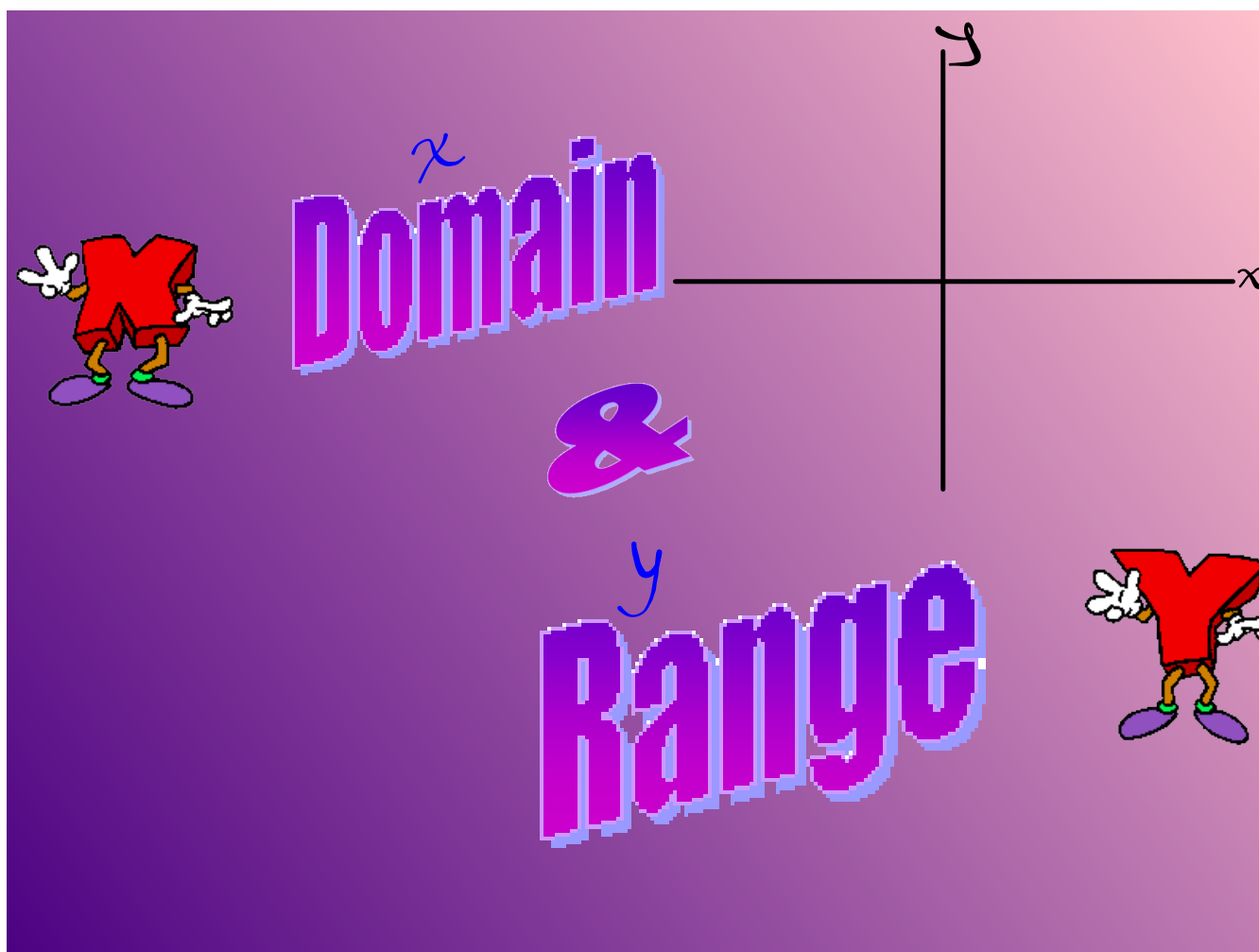
**Independent**  
<sup>x</sup>

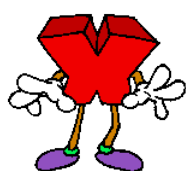
- a variable whose value is not determined by the value of another variable, and whose value determines the value of another (dependent) variable

# Limits?

There are limits to everything in life!





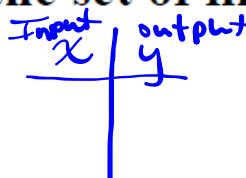


# Domain & Range



**Domain**

- the set of first elements in a relation



**Range**

- the set of second elements in a relation

$$y = 2x + 3$$

Input	Output
0	3
1	5
2	7
3	9
4	11
5	13

Handwritten annotations: A horizontal arrow points to the output value 3. A vertical bracket on the right side of the table spans from the output 5 to 9, with a handwritten '+2' next to it. Another vertical bracket is drawn below the 7 and 9 outputs.

# Domain and Range

Dr. Math says...



" The **domain** of a function is the set of all the stuff you can plug into the function. "

" The **range** of a function is the set of all the stuff you can get out of the function. "

Sport	Equipment
badminton	shuttlecock
badminton	racquet
hockey	puck
hockey	stick
tennis	ball
tennis	racquet
soccer	ball

domain  
**First**

Range  
**Second**

( **Sport, Equipment** )

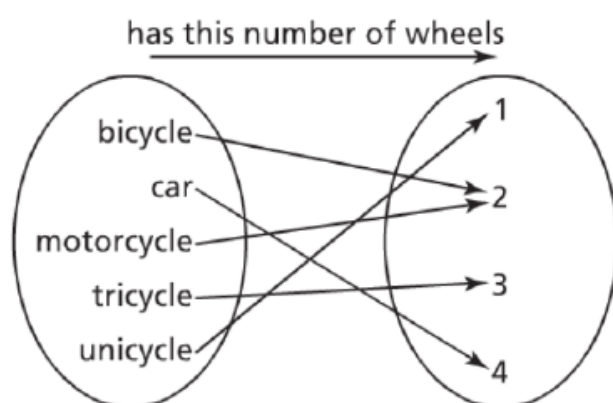
**Domain**

The set of first elements:  
{ badminton, hockey, tennis, soccer }

**Range**

The set of second elements:  
{ shuttlecock, racquet, puck, stick, ball }

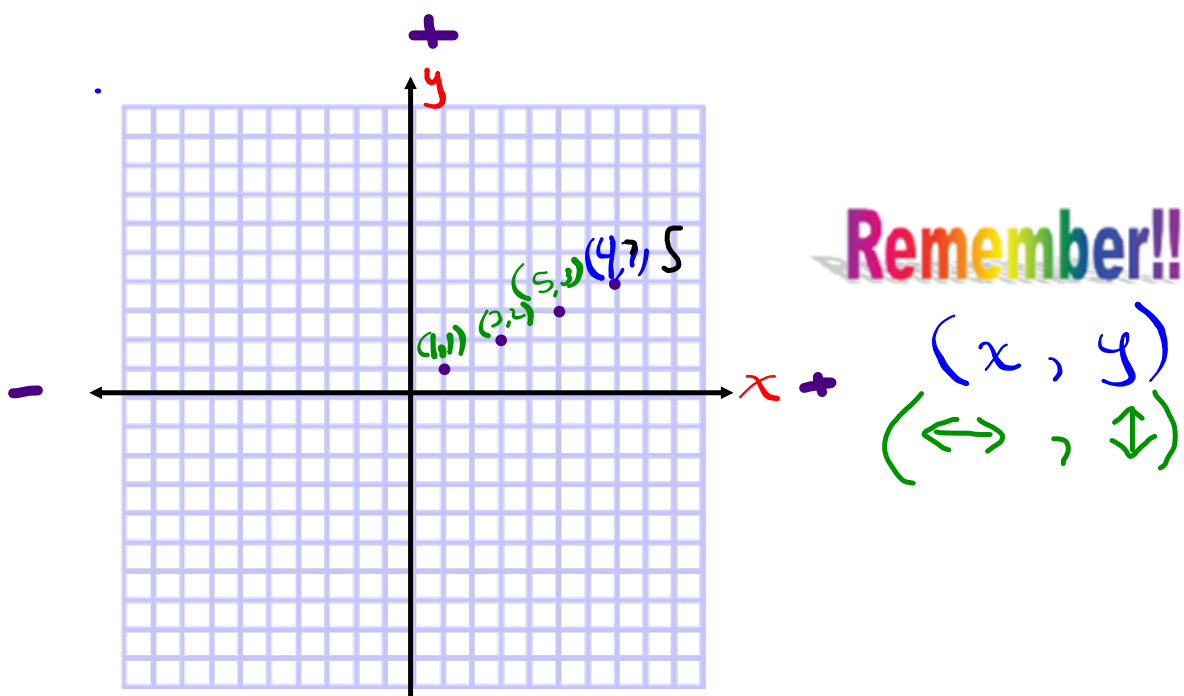


**Domain**

The first set of elements:  
{bicycle, car, motorcycle, tricycle, unicycle}

**Range**

The second set of elements:  
{1, 2, 3, 4}



Ordered Pairs: —

$$\left\{ \begin{array}{c} \text{1st} \quad \text{2nd} \quad \text{1st} \quad \text{2nd} \quad \text{1st} \quad \text{2nd} \quad \text{1st} \quad \text{2nd} \quad \text{1st} \quad \text{2nd} \\ \backslash \quad / \quad \backslash \quad / \quad \backslash \quad / \quad \backslash \quad / \quad \backslash \quad / \\ (1,1), (3,2), (5,3), (7,4), (9,5) \end{array} \right\}$$

**Domain**

The set of first elements:  $\{1, 3, 5, 7, 9\}$

**Range**

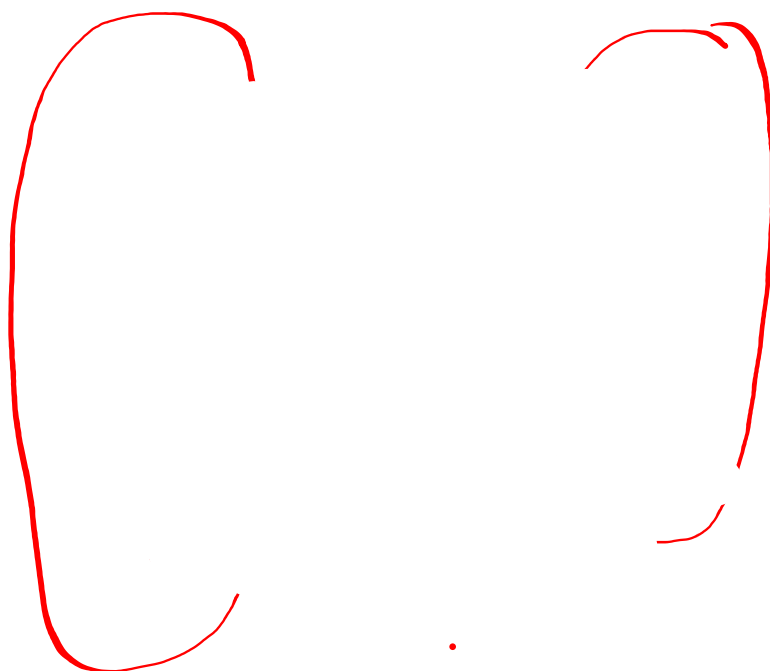
The set of second elements:  $\{1, 2, 3, 4, 5\}$

$$\{(2, 2), (1, 2), (-3, 5), (-2, 1), (5, 8)\}$$

State Domain & Range

$$\text{Domain} : \{-3, -2, 1, 2, 5\}$$

$$\text{Range} : \{1, 2, 5, 8\}$$





How do you state the range?

When connected lines

$$\{y \mid y \leq 5, y \in \mathbb{R}\}$$

$$\{y \mid -5 \leq y \leq 8, y \in \mathbb{I}\}$$

Important Study

How to write Range

$$\{y \mid \square \leq y \leq \square, y \in \square\}$$

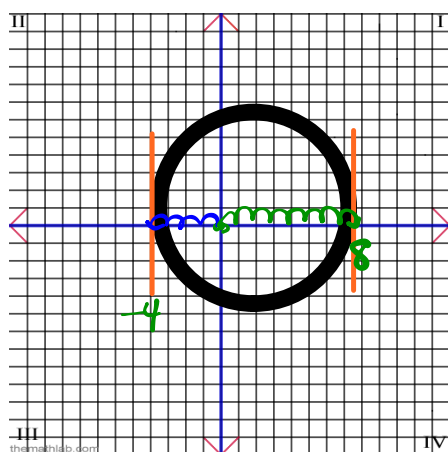
Line  $\Rightarrow$  "R"  
Dots "I"

How to write Domain

$$\{x \mid \square \leq x \leq \square, x \in \square\}$$

# Domain

Wide



The **domain** represents all the values of x.

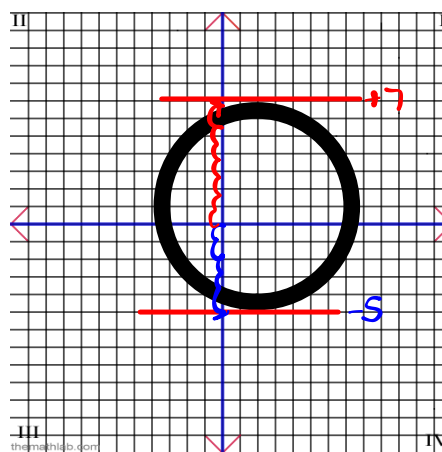
**X is the independent Variable**

$$\left\{ x \mid \underset{\text{left}}{-4} \leq x \leq \underset{\text{right}}{8}, x \in \mathbb{R} \right\}$$

connected  $\mathbb{R}$   
dots  $\Rightarrow \mathbb{I}$

$$\left\{ y \mid \underset{\text{lowest}}{-5} \leq y \leq \underset{\text{highest}}{+7}, y \in \mathbb{R} \right\}$$

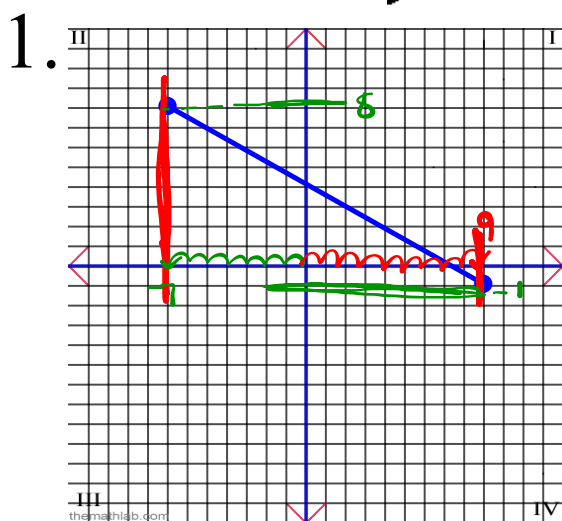
# Range



The **range** represents all the values of y.

**Y is the dependent Variable**

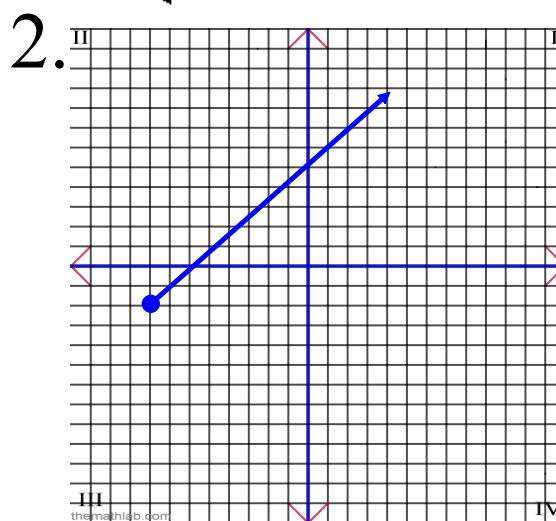
# EXAMPLES!



$$\{x \mid \underline{-7} \leq x \leq \underline{9}, x \in \underline{\mathbb{R}}\}$$

width ← connected line

$$\{y \mid \underline{-1} \leq y \leq \underline{8}, y \in \underline{\mathbb{R}}\}$$



## Attachments

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Domain & Range 1.doc