

MC

1. **A**
2. **C**
3. **C**
4. **B**
5. **B**
6. **B**
7. **A**

Short Answer

1. Simplify each expression and state any non-permissible values.

a. $\frac{x^2 - 2x}{x + 1} \times \frac{x^2 - 1}{x^2 + x - 6}$

$$\frac{\cancel{x}(x-2)}{\cancel{x}+1} \times \frac{(x-1)\cancel{(x+1)}}{(x+3)\cancel{(x-2)}}$$

$$\frac{x(x-1)}{x+3} \quad x \neq -1, -3, 2$$

b. $\frac{4x-1}{x^2+7x+12} \div \frac{2x-1}{x^2+x-12}$

$$\frac{4x-1}{(x+3)(x+4)} \div \frac{(2x-1)}{(x+4)(x-3)}$$

$$\frac{(4x-1)}{(x+3)\cancel{(x+4)}} \times \frac{\cancel{(x+4)}(x-3)}{(2x-1)}$$

$$\frac{(4x-1)(x-3)}{(x+3)(2x-1)} \quad x \neq -3, -4, \frac{1}{2}, 3$$

c. $\frac{2x^2+x-1}{6x^2-x-2} \times \frac{2x^2+3x+1}{2x^2+5x-3} \div \frac{x^2+2x+1}{x+3}$

$$\frac{(2x-1)\cancel{(x+1)}}{(2x+1)(x-2)} \times \frac{(2x+1)\cancel{(x+1)}}{(2x-1)\cancel{(x+3)}} \div \frac{(x+1)\cancel{(x+1)}}{x+3}$$

$$x \neq -\frac{1}{2}, 2, \frac{1}{2}, 3, -1$$

$$\frac{\cancel{(2x-1)}\cancel{(x+1)}}{(2x+1)(x-2)} \times \frac{\cancel{(2x+1)}\cancel{(x+1)}}{\cancel{(2x-1)}\cancel{(x+3)}} \times \frac{\cancel{(x+3)}}{\cancel{(x+1)}\cancel{(x+1)}}$$

$$\frac{1}{x-2}$$

2. Simplify each expression and state any non-permissible values.

a. $\frac{x}{x^2-3x-4} - \frac{4}{x+1}$

$$\frac{x}{(x-4)(x+1)} - \frac{4}{(x+1)}$$

$$\frac{x - 4(x-4)}{(x-4)(x+1)}$$

$$\frac{x - 4x + 16}{(x-4)(x+1)}$$

$$\frac{-3x + 16}{(x-4)(x+1)}$$

$x \neq 4, -1$

b. $\frac{3x+1}{2x^2-2} + \frac{2x+2}{2x^2-8x+6}$

$$\frac{3x+1}{2(x^2-1)} + \frac{2(x+1)}{2(x^2-4x+3)}$$

$$\frac{3x+1}{2(x-1)(x+1)} + \frac{2(x+1)}{2(x-3)(x-1)}$$

$$\frac{(3x+1)(x-3) + 2(x+1)(x+1)}{2(x-1)(x+1)(x-3)}$$

$x \neq 1, -1, 3$

$$\frac{(3x^2 - 8x - 3) + 2(x^2 + 2x + 1)}{2(x-1)(x+1)(x-3)}$$

$$\frac{3x^2 - 8x - 3 + 2x^2 + 4x + 2}{2(x-1)(x+1)(x-3)} \Rightarrow \frac{5x^2 - 4x - 1}{2(x-1)(x+1)(x-3)}$$

c. $\frac{5}{x^2-1} - \frac{2}{x^2+4x+3} + \frac{3}{x^2+2x-3}$

$$\frac{5}{(x-1)(x+1)} - \frac{2}{(x+3)(x+1)} + \frac{3}{(x+3)(x-1)}$$

$$\frac{5(x+3) - 2(x-1) + 3(x+1)}{(x-1)(x+1)(x+3)}$$

$$\frac{5x + 15 - 2x + 2 + 3x + 3}{(x-1)(x+1)(x+3)}$$

$$\frac{6x + 20}{(x-1)(x+1)(x+3)} \quad x \neq 1, -1, 3$$

3. Solve and check.

a. $\frac{5}{x-1} + \frac{2}{x+1} = -6$

$\frac{5}{\cancel{x-1}} + \frac{2}{\cancel{x+1}} = -6 \frac{(x-1)(x+1)}{(x-1)(x+1)}$

$5(x+1) + 2(x-1) = -6(x-1)(x+1)$

$5x+5+2x-2 = -6(x^2-1)$

$7x+3 = -6x^2+6$

$6x^2+7x-3=0$

QE or Factor

$(3x-1)(2x+3) = 0$

$x = \frac{1}{3}, -\frac{3}{2}$

$\frac{-7 \pm \sqrt{121}}{12}$

$\frac{-7 \pm 11}{12}$

$\frac{4}{12} = \frac{1}{3}$ $\frac{-18}{12} = -\frac{3}{2}$

b. $1 + \frac{2x}{x+4} = \frac{3}{x-1}$

$1 + \frac{2x}{\cancel{x+4}} = \frac{3}{\cancel{x-1}}$

$1(x+4)(x-1) + 2x(x-1) = 3(x+4)$

$x^2+3x-4 + 2x^2-2x = 3x+12$

$3x^2+x-4 = 3x+12$

$3x^2-2x-16=0$

QE

or

factor

$(3x-8)(x+2) = 0$

$x = \frac{8}{3}, -2$

$\frac{2 \pm \sqrt{196}}{6}$

6

$\frac{2 \pm 14}{6}$

$\frac{16}{6} = \frac{8}{3}$

$\frac{-12}{6} = -2$

$$1. \frac{3}{x+2} + \frac{3}{x+2} + \frac{2}{x-3} + \frac{2}{x-3} = 5$$

$$3(x-3) + 3(x-3) + 2(x+2) + 2(x+2) = 5(x+2)(x-3)$$

$$3x-9+3x-9+2x+4+2x+4 = 5(x^2-x-6)$$

$$10x-10 = 5x^2-5x-30$$

$$0 = 5x^2-15x-20$$

$$0 = 5(x^2-3x-4)$$

$$5(x-4)(x+3)$$

$$x = \textcircled{4} \text{ or } -3 \leftarrow \text{inadmissible}$$

2.

	D	S	T
Ed \Rightarrow Van	1200	$x-5$	$\frac{1200}{x-5}$
Van \Rightarrow Ed	1200	x	$\frac{1200}{x}$
			31

75 km/h going
85 km/h return

$$\frac{1200}{x-5} + \frac{1200}{x} = 31$$

$$1200x + 1200(x-5) = 31x(x-5)$$

$$1200x + 1200x - 6000 = 31x^2 - 155x$$

$$0 = 31x^2 - 2555x + 6000$$

$$\frac{2555 \pm \sqrt{5784025}}{62}$$

$$\frac{2555 \pm 2405}{62} \begin{cases} 80 \\ 2.42... \end{cases}$$

3. $\frac{x}{x-12}$

$\frac{1}{x} + \frac{1}{x-12} = \frac{5}{16}$ (with $16x(x-12)$ above each fraction)

$16(x-12) + 16x = 5x(x-12)$

$16x - 192 + 16x = 5x^2 - 60x$

$0 = 5x^2 - 92x + 192$

$\frac{92 \pm \sqrt{4624}}{10}$

$\frac{92 \pm 68}{10} < \begin{matrix} 16 \\ 2.4 \end{matrix}$

$(16, 4)$

$(2.4, -9.6)$

4. $\frac{10x^2 + 3x - 1}{5x - 1}$

b) $2(5) + 1 = 11m$

$= \frac{(5x-1)(2x+1)}{(5x-1)}$

$w = 2x+1$