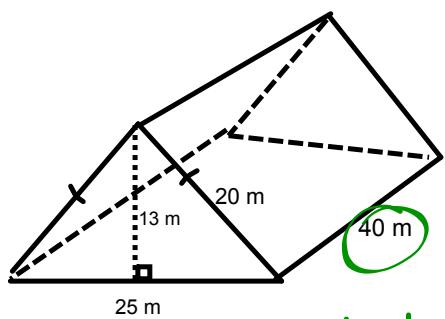




Find the volume



Warm Up Grade 8

May 30, 2017



Step 2

$$\begin{aligned} V &= A_{\text{base}} \times H \\ &= 162.5 \text{ m}^2 \times 40 \text{ m} \\ V &= 6500 \text{ m}^3 \end{aligned}$$

$$\begin{aligned} \text{Step 1} \quad A_{\text{base}\Delta} &= \frac{b \times h}{2} \\ &= \frac{25 \text{ m} \times 13 \text{ m}}{2} \\ &= \frac{325 \text{ m}^2}{2} \\ &= 162.5 \text{ m}^2 \end{aligned}$$

pg 205

1. If a rectangular prism is cut in half, each of the triangular prism will be the same and each will be half the volume of the rectangular prism.
2. In a triangular prism, the only face that can be used as the base is the triangle.

3a) Vol of Rect Prism = 450cm^3

Volume of Each
Triangular Prism

$$\begin{aligned} &= \frac{450}{2} \\ &= 225\text{cm}^3 \end{aligned}$$

b) Vol of Rect Prism = 624cm^3

Vol of each
Triangular Prism

$$\begin{aligned} &= \frac{624}{2} \\ &= 312\text{cm}^3 \end{aligned}$$

**Homework
Solutions**

$$A_{\text{base}} = 9.2 \text{ cm}^2 \quad h = 2.3 \text{ cm}$$

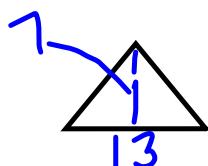
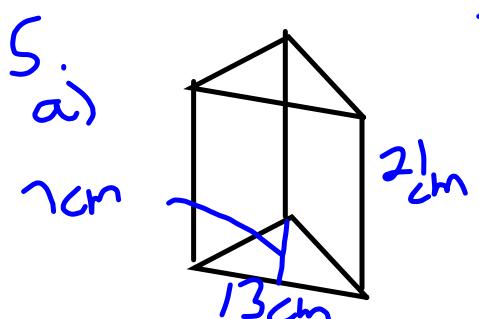
$$\begin{array}{r} 9.2 \\ \times 2.3 \\ \hline 276 \\ 184 \\ \hline 21.16 \end{array}$$

$$b) A_{\text{base}} = 43.5 \text{ cm}^2 \quad h = 5 \text{ cm}$$

$$\begin{aligned} V_{\text{ol}} &= A_{\text{base}} \times h \\ &= 43.5 \times 5 \\ &= 217.5 \text{ cm}^3 \end{aligned}$$

$$c) A_{\text{base}} = 3 \text{ m}^2 \quad h = 15 \text{ m}$$

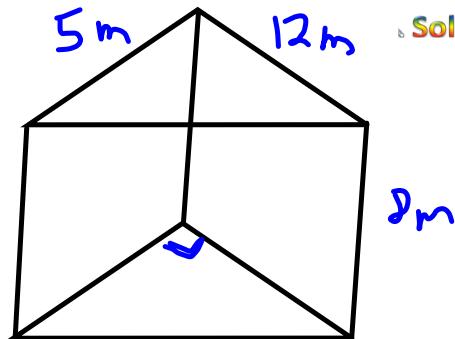
$$\begin{aligned} V_{\text{ol}} &= A_{\text{base}} \times h \\ &= 3 \times 15 \\ &= 45 \text{ m}^3 \end{aligned}$$



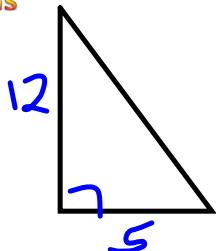
$$\begin{aligned} A_{\text{base}} &= \frac{b \times h}{2} \\ &= \frac{13 \times 7}{2} \\ &= 45.5 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} V_{\text{ol}} &= A_{\text{base}} \times h \\ &= 45.5 \times 21 \\ &= 955.5 \text{ cm}^3 \end{aligned}$$

b)



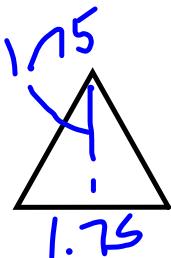
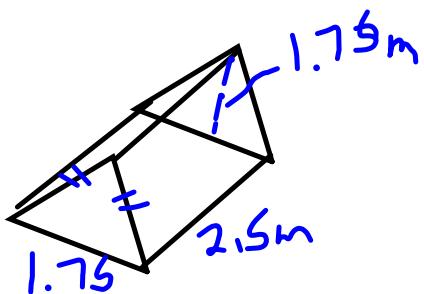
Homework
Solutions



$$\begin{aligned} A_{\text{base}} &= \frac{bxh}{2} \\ &= \frac{12 \times 5}{2} \\ &= \frac{60}{2} \\ &= 30 \text{ m}^2 \end{aligned}$$

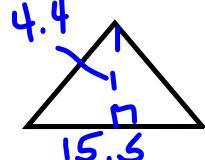
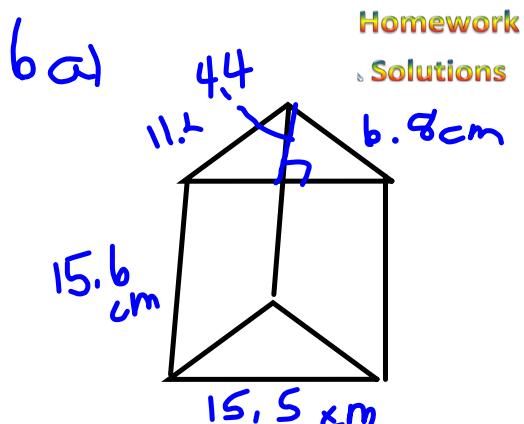
$$\begin{aligned} \text{Vol} &= \text{Base} \times h \\ &= 30 \times 8 \\ &= 240 \text{ m}^3 \end{aligned}$$

c)



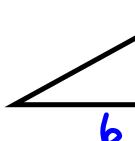
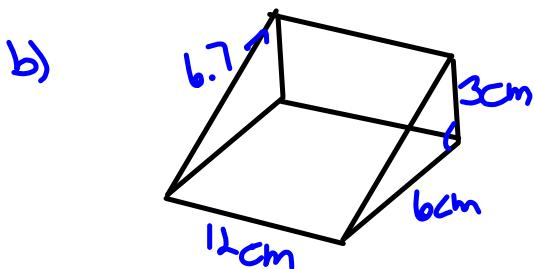
$$\begin{aligned} A_b &= \frac{bxh}{2} \\ &= \frac{1.75 \times 1.75}{2} \\ &= \frac{3.0625}{2} \\ &= 1.53125 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Vol} &= \text{Base} \times h \\ &= 1.53125 \times 2.5 \\ &= 3.828125 \text{ m}^3 \\ &\text{or } 3.8 \text{ m}^3 \end{aligned}$$



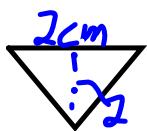
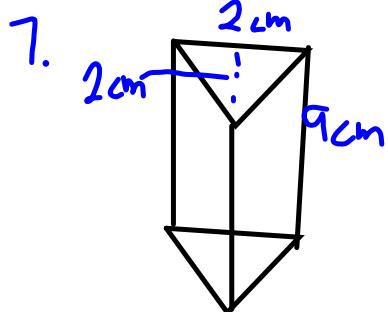
$$\begin{aligned}
 A_{\text{base}} &= \frac{b \times h}{2} \\
 &= \frac{15.5 \times 4}{2} \\
 &= \frac{68.2}{2} \\
 &= 34.1 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Vol} &< A_{\text{base}} \times h \\
 &= 34.1 \times 15.6 \\
 &= 531.96 \text{ cm}^3
 \end{aligned}$$



$$\begin{aligned}
 A_3 &= \frac{b \times h}{2} \\
 &= \frac{6 \times 3}{2} \\
 &= \frac{18}{2} \\
 &= 9 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Vol} &= A_{\text{base}} \times h \\
 &= 9 \times 12 \\
 &= 108 \text{ cm}^3
 \end{aligned}$$



Homework
Solutions

$$\begin{aligned}
 A_b &= \frac{b \times h}{2} \\
 &= \frac{2 \times 2}{2} \\
 &= \frac{4}{2} \\
 &= 2 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Vol} &= A_b \times h \\
 &= 2 \times 9 \\
 &= 18 \text{ cm}^3
 \end{aligned}$$

8. $\text{Vol} = 30 \text{ cm}^3$

$$A_{\text{base}} = 4 \text{ cm}^2$$

$$\begin{aligned}
 h &= \frac{30}{4} \\
 &= 7.5 \text{ cm}
 \end{aligned}$$

$$\text{Vol} = A_{\text{base}} \times H$$

$$\frac{30}{4} = \frac{4}{4} H$$

$$7.5 = H$$

$$9. \ . \ Vol = A_b \times h$$

[Homework](#)
[Solutions](#)

a) $S = \underline{\quad} \times \underline{\quad}$

$$A_b = 1\text{cm}^2, h = 5\text{cm}$$

$$A_b = 2\text{cm}^2, h = 2.5\text{cm}$$

b) $9\text{m}^3 = \underline{\quad} \times \underline{\quad}$

$$A_b = 1\text{m}^2, h = 9\text{m}$$

$$A_b = 3\text{m}^2, h = 3\text{m}$$

$$A_b < 9\text{m}^2, h = 1\text{m}$$

c) $8\text{m}^3 = \underline{\quad} \times \underline{\quad}$

$$A_b = 1\text{m}^2, h = 8\text{m}$$

$$A_b = 2\text{m}^2, h = 4\text{m}$$

$$A_b = 4\text{m}^2, h = 2\text{m}$$

$$A_b = 8\text{m}^2, h = 1\text{m}$$

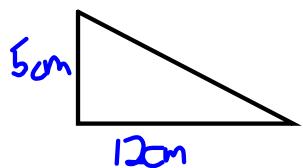
d) $18\text{cm}^3 = \underline{\quad} \times \underline{\quad}$

$$A_b = 2\text{cm}^2, A = 9\text{cm}$$

$$A_b = 3\text{cm}^2, A = 6\text{cm}$$

b) To find all possibilities, list the factors.

10. Sketch

[Homework](#)[Solutions](#)

$$\begin{aligned} A_b &= \frac{b \times h}{2} \\ &= \frac{12 \times 5}{2} \\ &= \frac{60}{2} \\ &= 30 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} V_{ol} &= A_b \times h \\ &= 30 \times 4 \\ &= 120 \text{ cm}^3 \end{aligned}$$

b) $\frac{120}{20} = 6$ people will be served cheese.

11. $V_{ol} = A_{base} \times h$

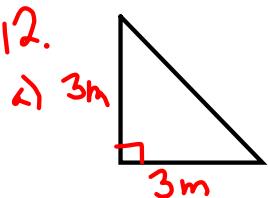
$$50 = A_{base} \times 5$$

$$10 \times 5$$

[Homework](#)[Solutions](#)

so A_{base} (or triangular face) is 10 m^2

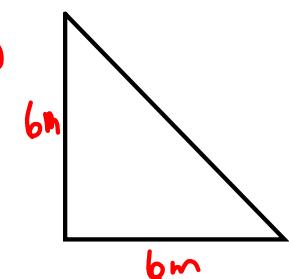
12.



$$\begin{aligned} A_b &= \frac{b \times h}{2} \\ &= \frac{3 \times 3}{2} \\ &= \frac{9}{2} \\ &= 4.5 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} V_{ol} &= A_{base} \times h \\ &= 4.5 \times 0.25 \\ &= 1.125 \text{ m}^3 \end{aligned}$$

b)



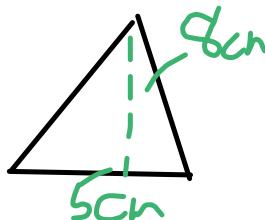
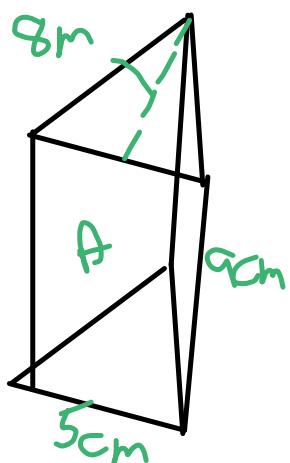
$$\begin{aligned} A &= \frac{b \times h}{2} \\ &= \frac{6 \times 6}{2} \\ &= \frac{36}{2} \\ &= 18 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} V_{ol} &= A_b \times h \\ &= 18 \times 0.25 \\ &= 4.5 \text{ m}^3 \end{aligned}$$

Jackie needs 4 times as much concrete

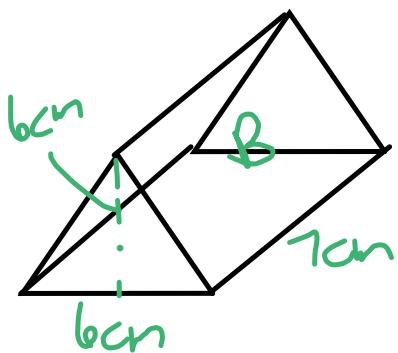
13. a) Prediction
Prism A

b)



$$\begin{aligned}A_b &= \frac{b \times h}{2} \\&= \frac{8 \times 5}{2} \\&= \frac{40}{2} \\&= 20 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}V &= A_b \times h \\&= 20 \times 9 \\&= 180 \text{ cm}^3\end{aligned}$$



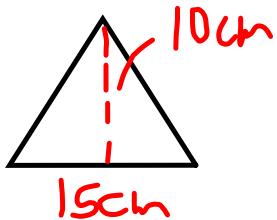
$$\begin{aligned}A_b &= \frac{b \times h}{2} \\&= \frac{6 \times 6}{2} \\&< \frac{36}{2} \\&= 18 \text{ cm}^2\end{aligned}$$

$$\begin{aligned}V &= A_b \times h \\&= 18 \times 7 \\&= 126 \text{ cm}^3\end{aligned}$$

Prediction was correct

c) If Prism B had a height of 10 cm it would have the same volume as A.

14 Sketch



$$\begin{aligned} A_b &= \frac{b \times h}{2} \\ &= \frac{15 \times 10}{2} \\ &= \frac{150}{2} \\ &= 75 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} V_{ol} &= A_b \times h \\ &= 75 \times 30 \\ &= 2250 \text{ cm}^3 \end{aligned}$$

b) Contains 1350 ml of water
depth = ?

$$1350 \text{ ml} = 1350 \text{ cm}^3$$

$$\begin{aligned} V_{ol} &= A_{base} \times h \\ 1350 &= 75 \times h \end{aligned}$$

$$\frac{1350}{75} = 18$$

The depth would be
18 cm

c) $\frac{1350}{2250} = 0.6$ or 60% water

$$15. \text{ Volume} = 198 \text{ cm}^3$$

$$A_{\text{base}} = 18$$

$$\text{Vol} = A_{\text{base}} \times h$$

$$198 = 18 \times h$$

$$\frac{198}{18} = h$$

$$11 = h$$



$$18 = \frac{b \times h}{2}$$

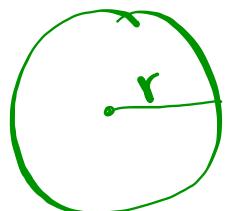
$$3b = b \times h$$

Base of \triangle , Height of \triangle , Height of Prism

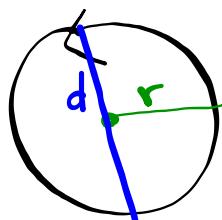
1
2
3
4
5
9

3b
18
12
9
6
4

:



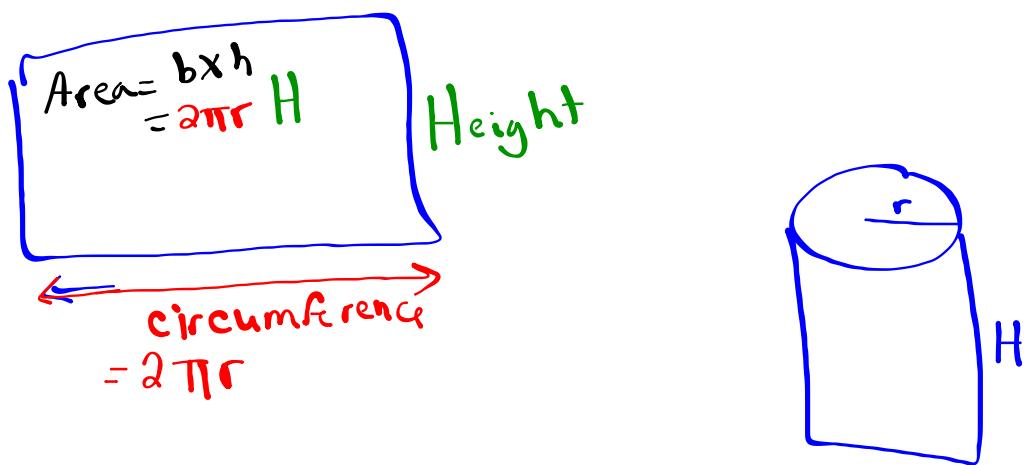
$$\text{Area}_O = \pi r^2$$



$$\text{Circumference}_O = \pi d$$

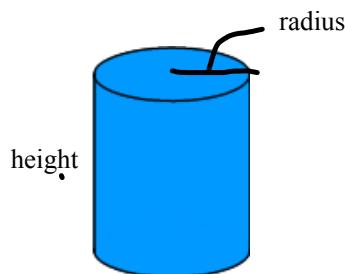
or
 $2\pi r$

$$\begin{aligned}\text{Total SA}_{\text{cyl}} &= 2 \text{ Area of circle} + \boxed{\text{Rec}} \\ &= 2 \pi r^2 + 2\pi r H\end{aligned}$$



Surface Area of a Cylinder

When finding the surface area of a cylinder, you still have to find the area of the faces then add them. However, what are the shapes of the faces?



The top and bottom are both Circles

If you unroll the curved face of the cylinder, you will get a rectangle

One side of the rectangle is the height of the cylinder,
and
the other side of the rectangle is the circumference of the circle

Step 1) Find the area of the circle

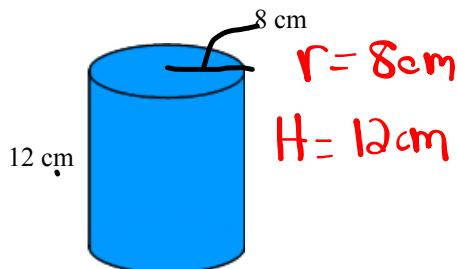
Step 2) Find the circumference of the circle

Step 3) Find the area of the rectangle $A = bh$

$$= \text{circumference} \times h$$

Step 4) Find the Total SA = 2Circles + Rectangle

Total SA of cyl = $2\pi r^2 + 2\pi rh$



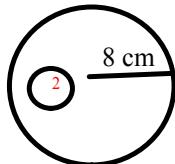
Step 1) Find the area of the circle

Step 2) Find the circumference of the circle

Step 3) Find the area of the rectangle $A = b \times h$
= circumference \times h

Step 4) Find the Total SA = 2Circles + Rectangle

Top and Bottom



Step 1)

$$\text{Area} = \pi r^2$$

$$= 3.14(8\text{cm})^2$$

$$= 3.14 \times 64\text{cm}^2$$

$$= 200.96\text{cm}^2$$

Curved Face



Step 2)

$$\begin{aligned} \text{Circumference} &= 2\pi r \times H \\ &= 2(3.14)(8\text{cm}) \times (12) \end{aligned}$$

$$602.88\text{cm}^2$$

Step 3) Area =

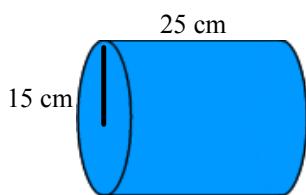
Step 4)

$$\begin{aligned} \text{Surface Area} &= \underline{\text{2 circles}} + \underline{\text{Rec}} \\ &= 2(200.96\text{cm}^2) + 602.88\text{cm}^2 \\ &= 401.92\text{cm}^2 + 602.88\text{cm}^2 \\ &= 1004.8\text{cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Total SA}_{\text{cyl.}} &= 2\pi r^2 + 2\pi r H \\ &= 2(3.14)(8\text{cm})^2 + 2(3.14)(8\text{cm})(12\text{cm}) \\ &= \underbrace{2(3.14)(64\text{cm}^2)}_{\text{multi}} + \underbrace{2(3.14)(8\text{cm})(12\text{cm})}_{\text{multiply}} \\ &= 401.92\text{cm}^2 + 602.88\text{cm}^2 \\ &= 1004.8\text{cm}^2 \end{aligned}$$

Must Follow
BEDMAS

Find the surface area



$$r = \boxed{15 \text{ cm}}$$

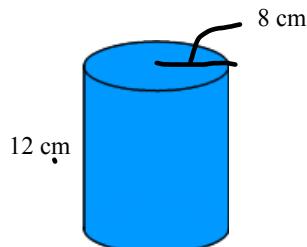
$$H = \boxed{25 \text{ cm}}$$

Your Turn

$$\begin{aligned}
 \text{Total SA}_{\text{cyl}} &= 2\pi r^2 + 2\pi r H \\
 &= 2(3.14)(15 \text{ cm})^2 + 2(3.14)(15 \text{ cm})(25 \text{ cm}) \\
 &= \underbrace{2(3.14)(225 \text{ cm}^2)}_{= 1413 \text{ cm}^2} + \underbrace{2(3.14)(15 \text{ cm})(25 \text{ cm})}_{= 2355 \text{ cm}^2} \\
 &= 3768 \text{ cm}^2
 \end{aligned}$$

Surface Area of a Cylinder

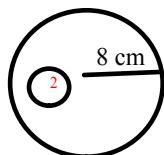
When finding the surface area of a cylinder, you still have to find the area of the faces then add them. However, what are the shapes of the faces?



The top and bottom are both circles.

If you unroll the curved face of the cylinder, you will get a rectangle. One side of the rectangle is the height of the cylinder, and the other side of the rectangle is the circumference of the circle

Top and Bottom



$$\begin{aligned} \text{Area} &= \pi r^2 \\ &= 3.14 \times 8^2 \\ &= 3.14 \times 64 \\ &= 200.96 \text{ cm}^2 \end{aligned}$$

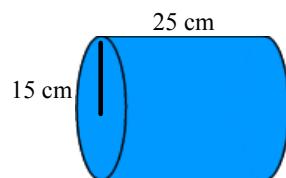
Curved Face



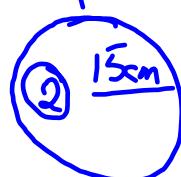
$$\begin{aligned} \text{Circumference} &= \pi \times d \\ &= 3.14 \times 16 \\ &= 50.24 \text{ cm} \end{aligned}$$

$$\begin{aligned} \text{Area} &= l \times w \\ &= 50.24 \times 12 \\ &= 602.88 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Surface Area} &= 2 \times 200.96 + 602.88 \\ &= 401.92 + 602.88 \\ &= 1004.8 \text{ cm}^2 \end{aligned}$$

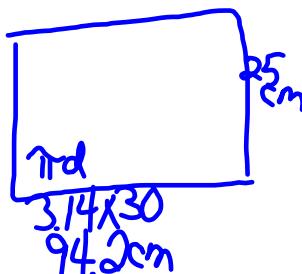


Top and Bottom



$$\begin{aligned} A &= \pi r^2 \\ &= 3.14 \times 15^2 \\ &= 3.14 \times 225 \\ &= 706.5 \text{ cm}^2 \end{aligned}$$

Curved Face



$$\begin{aligned} A &= l \times w \\ &= 3.14 \times 30 \\ &= 94.2 \text{ cm} \end{aligned}$$

$$SA = 2 \times 706.5 + 94.2$$

$$\begin{aligned} &= 1413 + 2355 \\ &= 3768 \text{ cm}^2 \end{aligned}$$

Class/Homework

$$r = \frac{1}{2}d$$

$$\text{Ex) } d = 4 \\ r = 2$$

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~~#16~~

4 q b

6 a b c

$$\begin{aligned} \text{Total SA}_{\text{cyl}} &= 2\pi r^2 + 2\pi rh \\ &2(3.14)()^2 + 2(3.14)()() \end{aligned}$$