



# System of Equations

**Numbers on Trial**

**CSI:**  
CRIME SCENE INVESTIGATION

If the suspect is a number identified as "y" and  $y = 2x - 8$  and  $x = 6y - 7$ , who is the suspect?

Music By  
**JOHN M. KEARNE**

*Handwritten notes in green ink:*  
Such y  
Deny

The image is a promotional poster for the TV show CSI: Crime Scene Investigation. It features the main cast members' faces at the top. The title 'CSI: CRIME SCENE INVESTIGATION' is prominently displayed in the center. Below the title, there is a yellow text block containing a math problem. The background includes a magnifying glass over a 'LAS VEGAS' sign and a computer keyboard. Green handwritten text is overlaid on the image.

If the suspect is a number identified as "y"

and

$y = 2x - 8$  and  $x = 6y - 7$ , who is the suspect?

$$y = 2(x) - 8$$

$$= 2(6y - 7) - 8$$

$$y = 12y - 14 - 8$$

$$y = 12y - 22$$

$$-11y = -22$$

$$\frac{-11y}{-11} = \frac{-22}{-11}$$

$$y = 2$$

$$x = 6y - 7$$

$$= 6(2) - 7$$

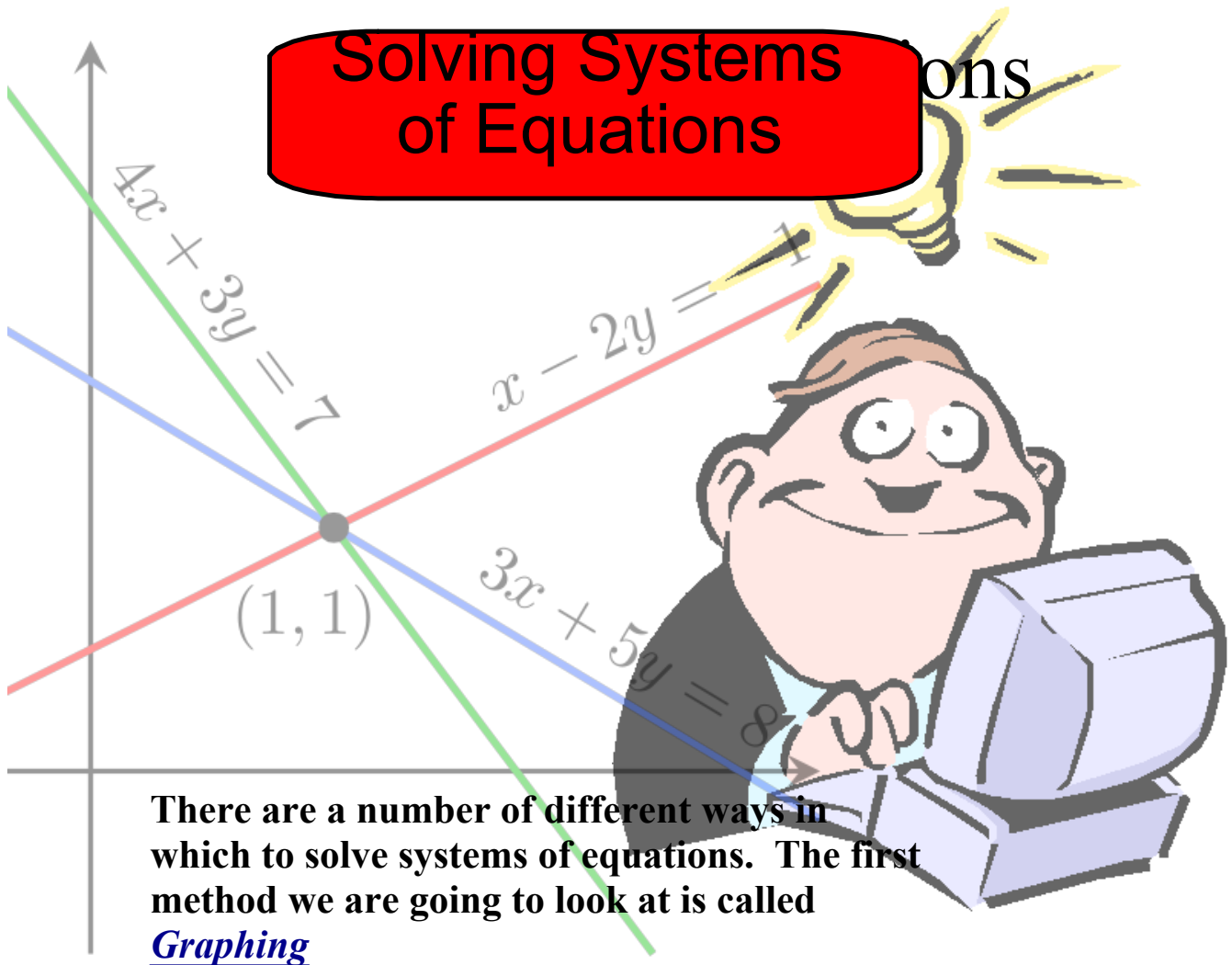
$$= 12 - 7$$

$$x = 5$$

$$(x, y)$$

$$(5, 2)$$

## Solving Systems of Equations



There are a number of different ways in which to solve systems of equations. The first method we are going to look at is called Graphing

The solution of a linear system can be estimated by graphing both equations on the same grid. If the two lines intersect, the coordinates  $(x, y)$  of the point of intersection are the solution of the linear system.

$$3x + 2y = -12 \quad \textcircled{1}$$

$$-2x + y = 1 \quad \textcircled{2}$$

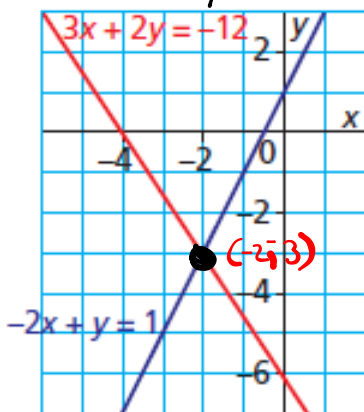
$$y = 2x + 1 \quad \textcircled{2}$$

$m = 2 \quad b = 1$

$$\frac{2y}{2} = \frac{-3x - 12}{2}$$

$$y = -\frac{3}{2}x - 6$$

$$m = -\frac{3}{2} \quad b = -6$$



We can use the graphs to estimate the solution of the linear system.

The set of points that satisfy equation ① lie on its graph.

The set of points that satisfy equation ② lie on its graph.

The set of points that satisfy both equations lie where the two graphs intersect.

From the graphs, the point of intersection appears to be  $(-2, -3)$ .

$$\begin{matrix} x & , & y \\ (-2) & , & (-3) \end{matrix}$$

Check LHS to RHS in Both Equation

$$\textcircled{1} \quad \begin{matrix} \text{LHS} & \text{RHS} \\ 3x + 2y = & -12 \end{matrix}$$

$$3(x) + 2(y)$$

$$3(-2) + 2(-3)$$

$$-6 + -6$$

$-12 \leftarrow$  Same  
So Works

Read off graph

$$\textcircled{2} \quad \begin{matrix} \text{LHS} & \text{RHS} \\ -2x + y = & 1 \end{matrix}$$

$$-2(x) + (y)$$

$$-2(-2) + (-3)$$

$$4 + -3$$

$1 \leftarrow$  Same  
So Works

**Example 1** Solving a Linear System by Graphing

Solve this linear system.

$$\textcircled{1} \quad x + y = 8$$

$$\textcircled{2} \quad 3x - 2y = 14$$

**SOLUTION**

$$x + y = 8 \quad \textcircled{1}$$

$$3x - 2y = 14 \quad \textcircled{2}$$

Determine the  $x$ -intercept and  $y$ -intercept of the graph of equation  $\textcircled{1}$ . Both the  $x$ - and  $y$ -intercepts are 8.

Write equation  $\textcircled{2}$  in slope-intercept form.

$$3x - 2y = 14$$

$$-2y = -3x + 14 \quad \text{Divide by } -2 \text{ to solve for } y.$$

$$y = \frac{3}{2}x - 7$$

The slope of the graph of equation  $\textcircled{2}$  is  $\frac{3}{2}$ , and its  $y$ -intercept is  $-7$ .

(Solution continues.)



Solve this linear system.

$$\textcircled{1} \quad x + y = 8 \rightarrow$$

$$y = -\frac{1}{1}x + 8$$

$$\textcircled{2} \quad 3x - 2y = 14$$

$$\frac{-2y}{-2} = \frac{-3x + 14}{-2}$$

$$y = \frac{3}{2}x - 7$$

$$y = mx + b$$

$$m = -\frac{1}{1} \quad b = +8$$

$$m = \frac{3}{2} \quad b = -7$$

Step 1) Find the x and y intercept for equation 1 or put in slope intercept form then graph it

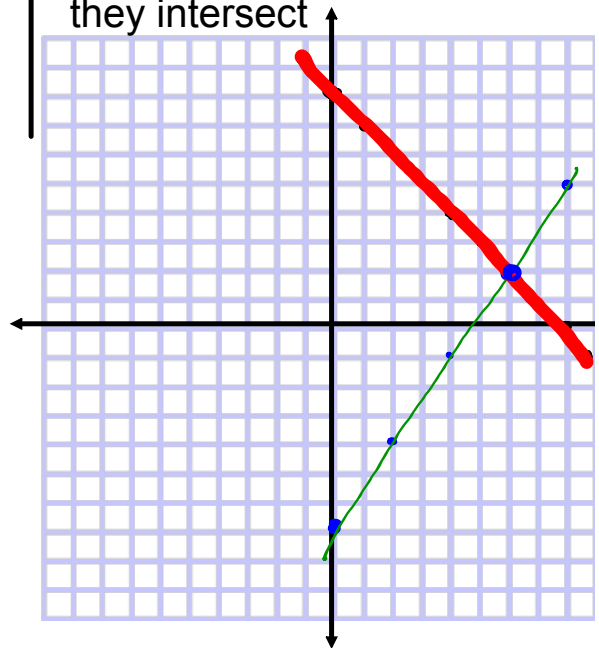
Step 2) For equation 2, solve for slope intercept form (Then Graph it)

line 1  $m = \frac{-1 \text{ rise}}{1 \text{ run}} \quad b = +8$

line 2  $m = \frac{3 \text{ rise}}{2 \text{ run}} \quad b = -7$

Point of intersection  
(6, 2)

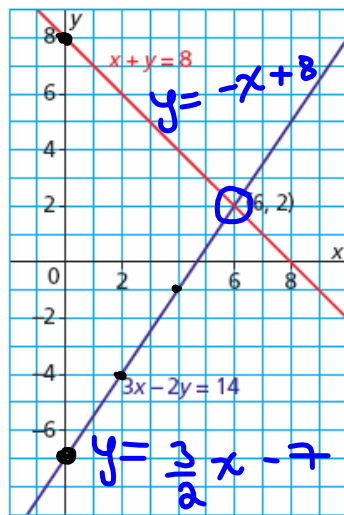
Once both are graphed read off the graph where they intersect



**Example 1** Solving a Linear System by Graphing

Graph each line.

The point of intersection appears to be (6, 2).



(Solution continues.)

Check it (6, 2)

LHS = RHS for both

$$\begin{array}{r}
 x + y = 8 \\
 \downarrow \quad \downarrow \\
 6 + 2 \\
 \hline
 8 \\
 \leftarrow \\
 \text{Same} \\
 \checkmark
 \end{array}$$

on next page

$$\begin{array}{r}
 3x - 2y = 14 \\
 \downarrow \quad \downarrow \\
 3(6) - 2(2) \\
 \hline
 18 - 4 \\
 \hline
 14 \\
 \leftarrow \\
 \text{Same} \\
 \checkmark
 \end{array}$$





**Example 1** Solving a Linear System by Graphing

Verify the solution. In each equation,  
substitute:  $x = 6$  and  $y = 2$

$$x + y = 8$$

$$\begin{aligned} \text{L. S.} &= x + y \\ &= 6 + 2 \\ &= 8 \\ &= \text{R.S.} \end{aligned}$$

$$3x - 2y = 14$$

$$\begin{aligned} \text{L.S.} &= 3x - 2y \\ &= 3(6) - 2(2) \\ &= 18 - 4 \\ &= 14 \\ &= \text{R.S.} \end{aligned}$$


For each equation, the left side is equal to the right side.  
So,  $x = 6$  and  $y = 2$  is the solution of the linear system.



1. Solve this linear system.

①  $2x + 3y = 3$

②  $x - y = 4$



$y = mx + b$  for Both

Using graphing method

①  $2x + 3y = 3$

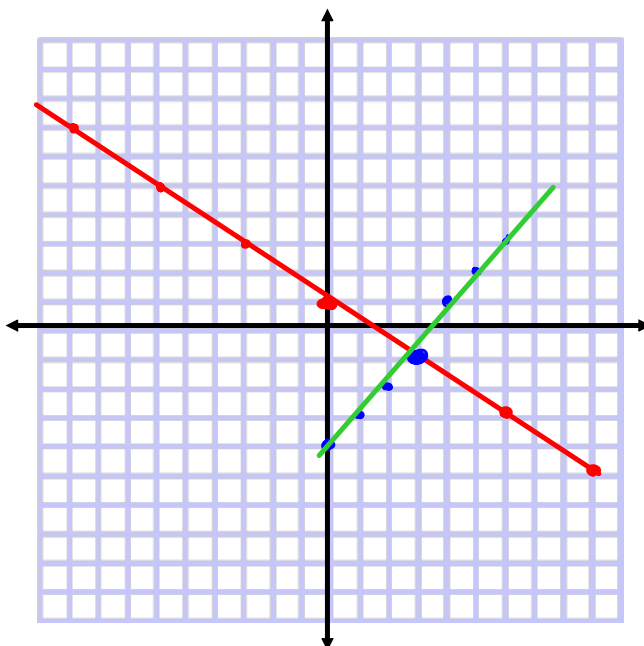
$\frac{3y}{3} = \frac{-2x + 3}{3}$

$y = -\frac{2}{3}x + 1$

$m = -\frac{2}{3}$  rise  
run

$b = +1$

Plot y-intercept  
then use  $m = -\frac{2}{3}$  rise  
to graph this line



②  $x - y = 4$

$\frac{-y}{-1} = \frac{-x + 4}{-1}$

$y = 1x - 4$

$m = \frac{1}{1}$   $b = -4$

Point of intersection  
 $(3, -1)$

Check

①  $2x + 3y = 3$

$2(3) + 3(-1)$   
 $6 + -3$   
 $3 \leftarrow \text{same}$

②  $x - y = 4$

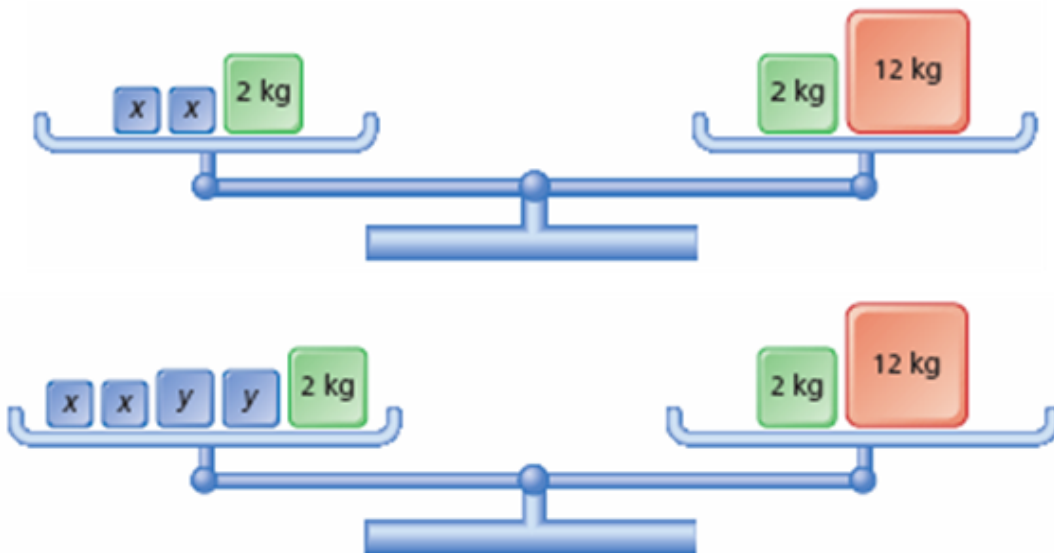
$(3) - (-1)$   
 $3 + (+1)$   
 $4 \leftarrow \text{same}$

Method 2: Substitution

I like this one better

## 7.4 Using a Substitution Strategy to Solve a System of Linear Equations

Save for tomorrow



## Solving Systems of Equations



There are a number of different ways in which to solve systems of equations. The second method we are going to look at is called *substitution*.



When we refer to solving a system of equations, we want to solve for a numerical value for one variable



**Rules for Substitution as a method for solving a system of equations.**

- **There must be the same number of equations as variables.**

- If there are two variables, there must be two equations; three variables, three equations, etc.

- **One of the equations can easily be substituted into the other equation to solve for one variable**

Steps when solving systems of equations using substitution

$$\textcircled{1} \quad -8x + y = 0$$

$$\textcircled{2} \quad x + 2y + 17 = 0$$

Doesn't  
matter  
which you  
start with

Step 1: Isolate one of the variables with the coefficient 1.

Step 2: Substitute into the other equation.

Step 3: Solve for the variable Using step 1's equation

You try with Substitution

Solve the following systems of equations using substitution

$$y - 3x = 5$$

$$y + x = 3$$