

# Chapter 6: Linear Functions

[http://www.youtube.com/watch?v=tMhF-1ew\\_bM&feature=related](http://www.youtube.com/watch?v=tMhF-1ew_bM&feature=related)



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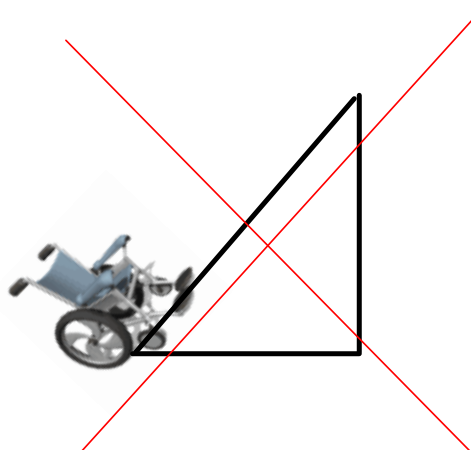
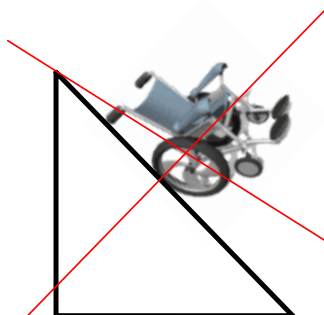
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A wheelchair ramp should not exceed a slope of 0.125.



8



Building stairs  
should  
not exceed  
a slope of  
0.83

6





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# Calculating slope!

*See a graph*

Same as rate of change

$$\text{slope} = \frac{\text{rise}}{\text{run}}$$

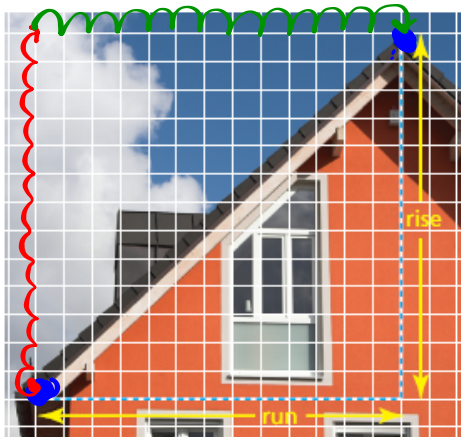


Some roofs are steeper than others. Steeper roofs are more expensive to shingle.  
The steepness of a roof is measured by calculating its **slope**.

$$\text{Slope} = \frac{\text{rise}}{\text{run}}$$

The **rise** is the vertical distance from the bottom of the edge of the roof to the top.  
The **run** is the corresponding horizontal distance.  
For each roof, we count units to determine the rise and the run.

Roof A



For Roof A

$$\text{Slope} = \frac{\text{rise}}{\text{run}}$$

$$\text{Slope} = ?$$

$$\frac{+13}{+13} = +1$$

Slope  
intercept  
Equation

$$y = mx + b$$

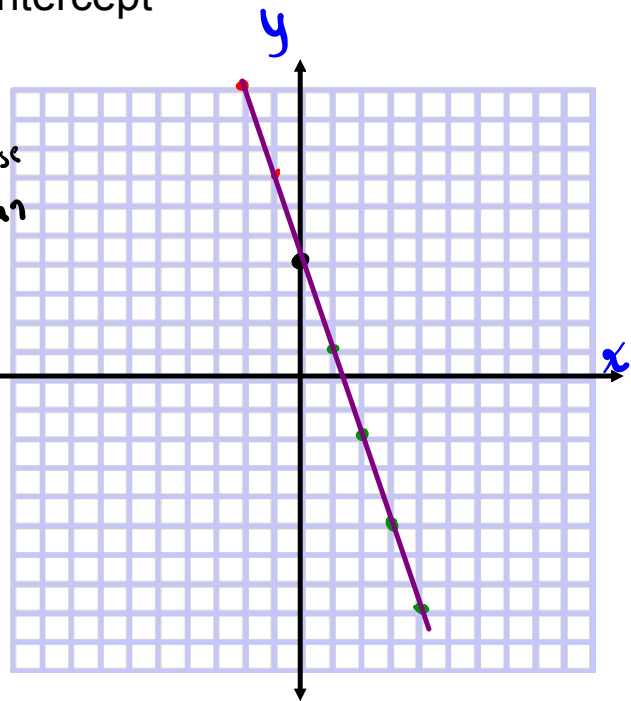
↑ slope      ↑ y-intercept

Ex)  $y = mx + b$   
 $y = -3x + 4$

$m = -3$  same as  $\frac{-3}{1}$  or  $\frac{+3}{-1}$  rise/run

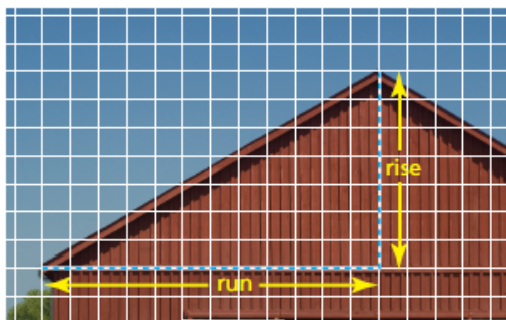
y-intercept =  $+4$  point on y-axis

Sketch using these two pieces of information





Roof B



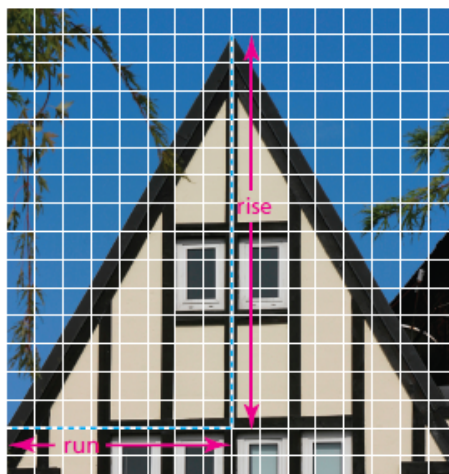
For Roof B

$$\text{Slope} = \frac{\text{rise}}{\text{run}}$$

$$\text{Slope} = \frac{7}{12}$$

$$\text{Slope} = 0.58\bar{3}$$

Roof C



For Roof C

$$\text{Slope} = \frac{\text{rise}}{\text{run}}$$

$$\text{Slope} = \frac{14}{8}$$

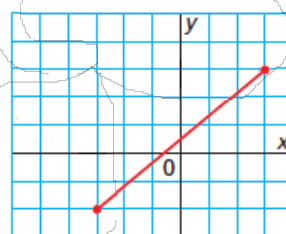
$$\text{Slope} = 1.75$$

Roof C is the steepest because its slope is the greatest.  
Roof B is the least steep because its slope is the least.

The slope of a line segment on a coordinate grid is the measure of its rate of change. From Chapter 5, recall that:

$$\text{Rate of change} = \frac{\text{change in dependent variable}}{\text{change in independent variable}}$$

$$\text{Rate of change} = \frac{\text{change in } y}{\text{change in } x} \quad \frac{\Delta y}{\Delta x} \quad \frac{\text{rise}}{\text{run}}$$



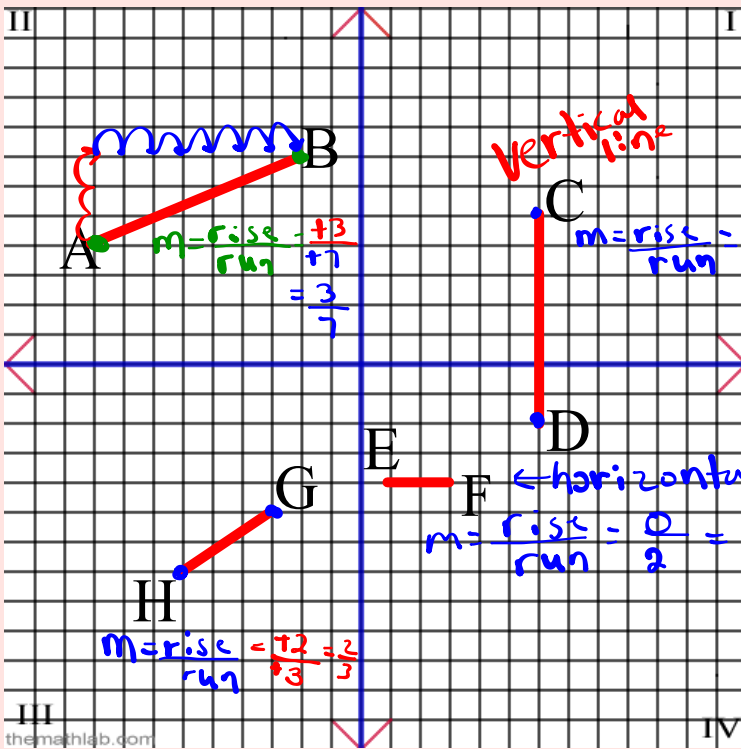
The change in  $y$  is the rise.

The change in  $x$  is the run.

$$\text{So, slope} = \frac{\text{rise}}{\text{run}}$$



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$$\text{slope} = \frac{\text{rise}}{\text{run}}$$

undefined

This is used when you can see the graph!





# Calculating slope!

given points  
of ordered pairs

~~x~~

slope →  $m = \frac{y_2 - y_1}{x_2 - x_1}$

Find the slope of a line passing through the points (2,-3) and (-5,8).  
*1st point*      *2nd point*  
 $(x_1, y_1)$        $(x_2, y_2)$   
 $(2, -3)$        $(-5, 8)$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

This is used when you are given co-ordinates.

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{8 - -3}{-5 - 2}$$

$$= \frac{8 + 3}{-5 - 2}$$

$$\frac{+11}{-7}$$

$$m = -\frac{11}{7}$$

Be careful here add the opposite (Rule for integers)

all mean the same  
 $-\frac{11}{7}$  OR  $-\frac{11}{7}$        $\frac{11}{-7}$

## YOU TRY

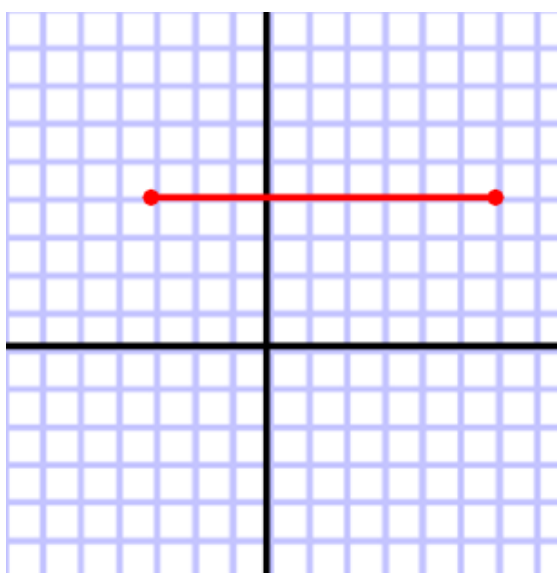
Find the slope of a line passing through the points  $(7, 5)$  and  $(8, -2)$ .

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\begin{aligned} m &= \frac{y_2 - y_1}{x_2 - x_1} \\ &= \frac{-2 - 5}{8 - 7} \\ &= \frac{-7}{1} \end{aligned}$$

# Horizontal Line

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$



Pick two points

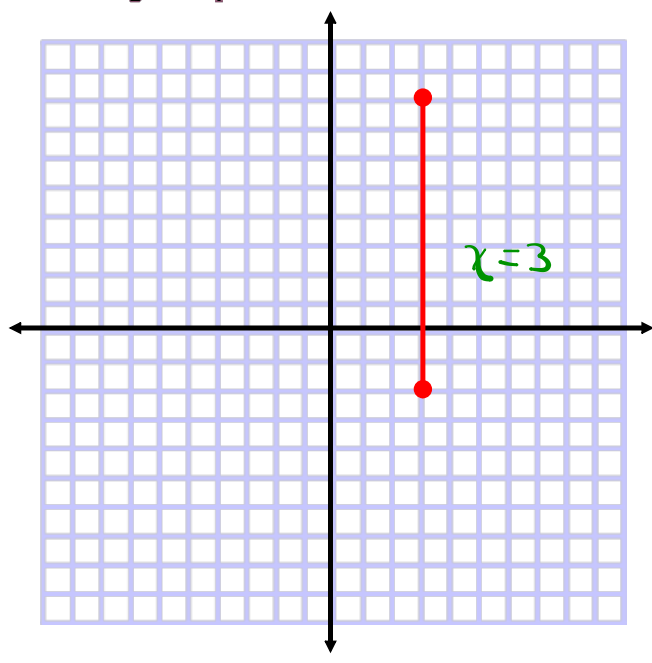
$$m = \frac{\text{rise}}{\text{run}} = \frac{0}{9} = 0$$

$m = 0$  for horizontal line

Vertical

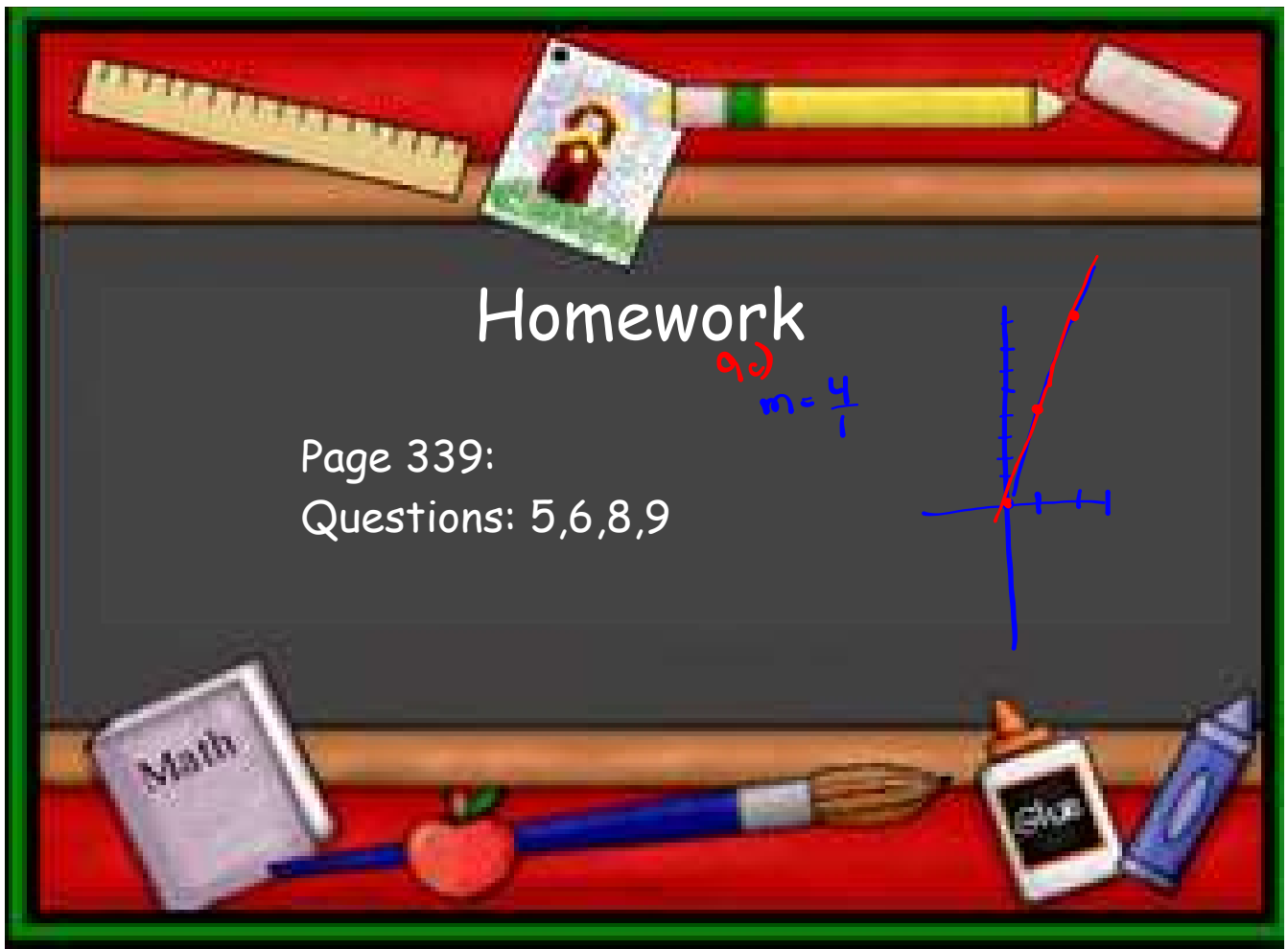
$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\text{rise}}{\text{run}} = \frac{10}{0} = \text{Undefined}$$

Always



Line



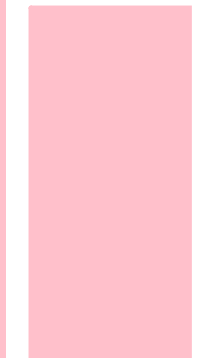


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Calculate the slope.

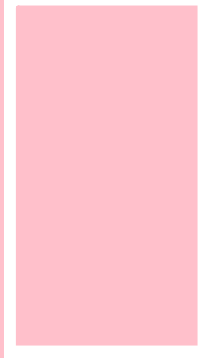
1.  $(3,5)$   $(2,8)$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$



2.  $(-9,-2)$   $(7,3)$

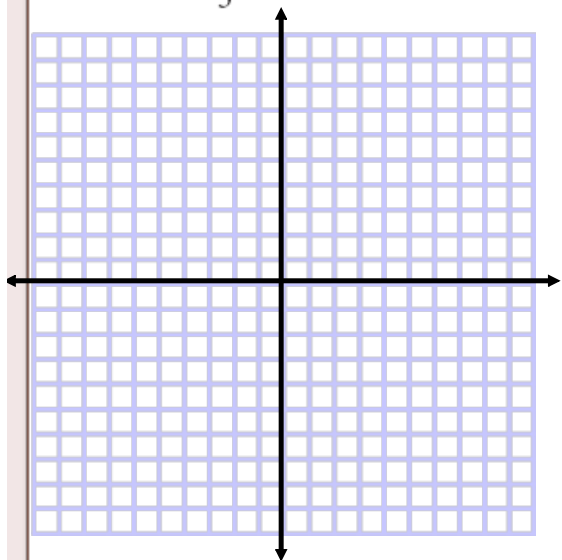
$$m = \frac{y_2 - y_1}{x_2 - x_1}$$



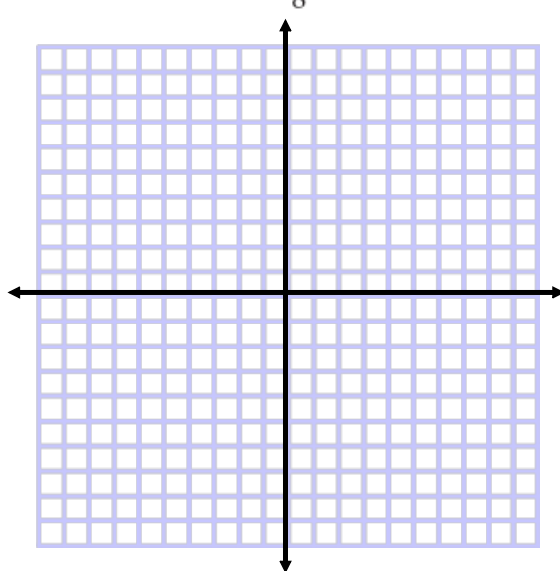
**Example 2** Drawing a Line Segment with a Given Slope

Draw a line segment with each given slope.

a)  $\frac{7}{5}$



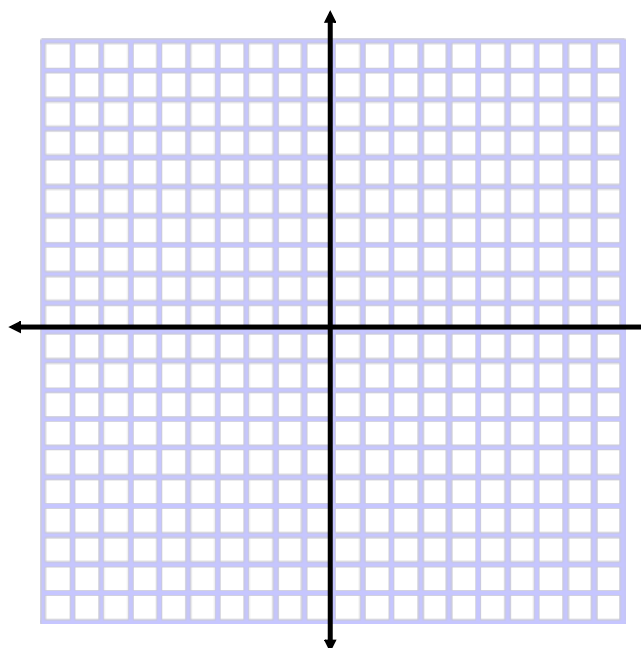
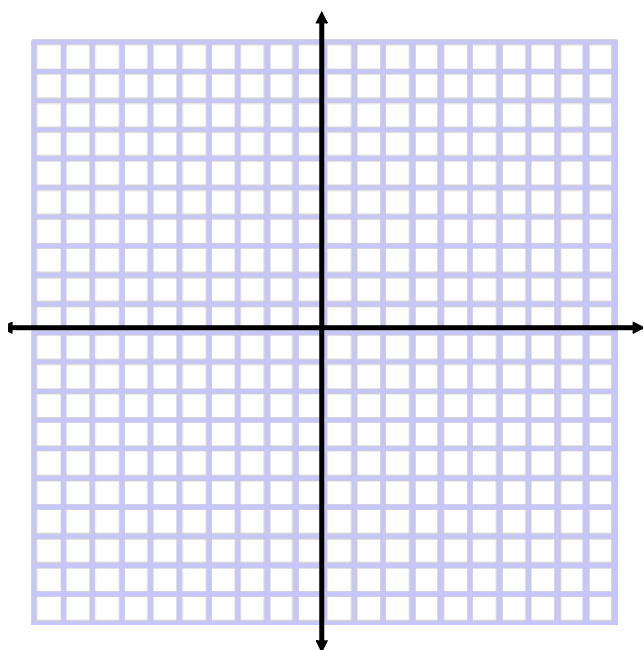
b)  $-\frac{3}{8}$



2. Draw a line segment with each slope.

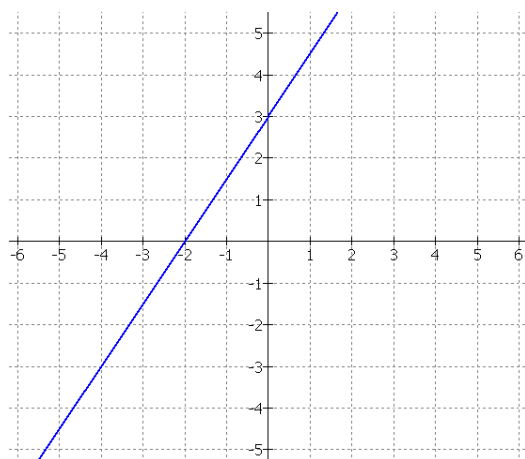
a)  $\frac{4}{9}$

b)  $-\frac{8}{3}$

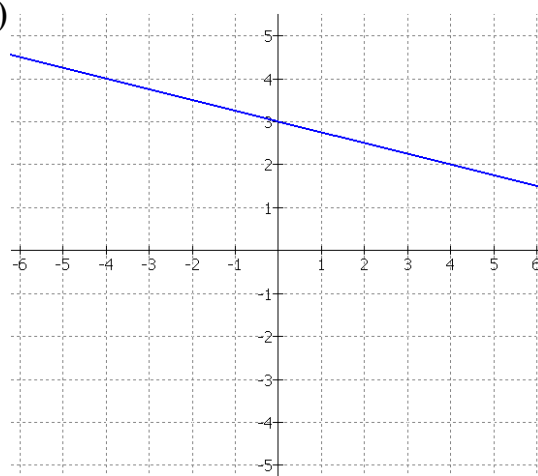


Determine the slope of each of the following lines:

(a)



(b)



Which ordered pairs should we use to make our calculation?

$$\text{slope} = \frac{\Delta y}{\Delta x}$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\text{slope} = \frac{\Delta y}{\Delta x}$$

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$