

Homework Solutions

15) $-10x + 7y = 12$

$-3x + 6y = -12$

$(-4, -4)$

16) $-3x + 4y = 2$

$-5x + 3y = 29$

$(-10, -7)$

Homework Solutions

17) $-10x - 6y = -14$

$8x + 5y = 11$

$(2, -1)$

18) $-3x - 2y = 8$

$-8x - 7y = 18$

$(-4, 2)$

Systems of Equations Word Problems



Write the following as algebraic equations involving 2 variables.

- a) The sum of 2 numbers is 50

$$x + y = 50$$

equation 1

- b) The difference between 2 numbers is 40

equation 2

$$x - y = 40$$

$$x, y$$

$$(45, 5)$$

$$\textcircled{1} \quad x + y = 50$$

$$\textcircled{2} \quad x - y = 40$$

$$\textcircled{1} + \textcircled{2} \quad 2x = 90$$

$$\frac{2x}{2} = \frac{90}{2}$$

$$x = 45$$

↓ sub into $\textcircled{1}$

$$x + y = 50$$

$$45 + y = 50$$

$$45 + y = 50 - 45$$

$$y = 5$$

c) There are a total of 35 boys and girls in the class.

equation 1

$$\textcircled{1} \quad b + g = 35$$

Eliminate

There are 5 more boys than girls

$$\textcircled{2} \quad b - g = 5$$

equation 2

$$\textcircled{1} + \textcircled{2} \quad 2b = 40$$

$$\frac{2b}{2} = \frac{40}{2}$$

$$\boxed{b = 20}$$

$$b + g = 35$$

$$20 + g = 35 - 20$$

$$\boxed{g = 15}$$

Solving Problems in 2 variables

Some problems of business and industry are solved by expressing the problems as a system of equations.

Example 1:

The sum of two numbers is thirty and their difference is 174. Find the numbers.

$$\textcircled{1} \quad x + y = 30$$

$$\textcircled{2} \quad x - y = 174$$

$$\textcircled{1} + \textcircled{2} \quad \underline{2x = 204}$$

$$\frac{2x}{2} = \frac{204}{2}$$
$$\boxed{x = 102}$$

Sub into $\textcircled{1}$

$$\textcircled{1} \quad x + y = 30$$
$$102 + y = 30 - 102$$
$$\boxed{y = -72}$$

Example 2:

When 4 times the larger of ~~2~~ numbers is added to 3 times the smaller the result is 68.
Seven times the larger less 5 times the smaller is 37. Find the numbers.

let x represent larger #
let y represent small #

$$\textcircled{1} \quad 4(x) + 3(y) = 68 \xrightarrow{\times 5} \textcircled{3} \quad 20x + 15y = 340$$

$$\textcircled{2} \quad 7x - 5y = 37 \xrightarrow{\times 3} \textcircled{4} \quad 21x - 15y = 111$$

$$\textcircled{3} + \textcircled{4} \quad \begin{array}{r} 20x + 15y = 340 \\ 21x - 15y = 111 \\ \hline 41x = 451 \\ \underline{41} \\ x = 11 \end{array}$$