

Chapter 5

Polynomials

December 1, 2017

Term--Part of an expression or series separated by a + or - sign, or parts of a sequence separated by commas.

Expression	Terms
A) $5a^3 - 2xy + 3$	$5a^3, -2xy,$ and 3
B) $\frac{p - 2q}{a^2 + b}$	$p, -2q, a^2,$ and b

$3 + 5a^3 - 2xy$
 $-2xy + 5a^3 + 3$

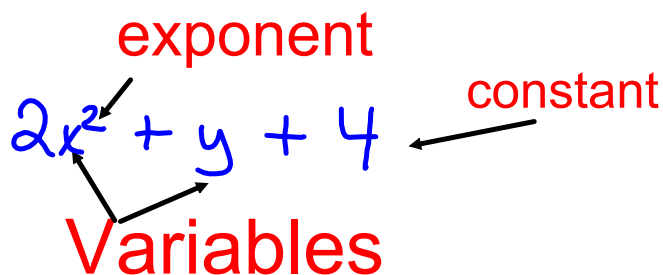
Polynomials

$$-6 + 4a$$

A polynomial is one term or the sum of terms whose variables have whole number exponents.) *different*

Expression	Polynomial? <small>[yes or no]</small>	# of terms	List the terms
A) $2a + 3$	yes	2	$2a, 3$
B) $4a - 6$	yes	2	$4a, -6$
C) $4a$	yes	1	$4a$

- constants [like 3, -20, or 1/2]
- Variables [like x , y etc]
- exponents [like the 2 in y^2] but only whole number exponents



Polynomials are combined using:

- addition [+], subtraction[-]

Term-a constant [number], variable **or** the product of a number and variable.

Examples ~~2~~, ~~y~~, ~~2xy~~, ~~2x²~~, ~~-3x~~, ~~-2~~
of a Term

constant 2, -2

Variable y

product of a number and a variable

$2xy, 2x^2, -3x$

Polynomial	How many terms	List the terms	Identify constant if there is one
A. -3	1	-3	-3
B. $4a^2$	1	$4a^2$	none
C. $-3a + 4a^3$	2	$-3a, 4a^3$	none
D. $-3xy + 2$	2	$-3xy, 2$	2
E. $-4x + 3a + 2$	3	$2, -4x, 3a$	2
F. $2x^2 + 4x - 3y + 2$	4	$2x^2, 4x, -3y, 2$	2

The degree of a term is the sum of the exponents of the **variables** in a single term. For example, the degree of $4x^2y$ is 3.

The term with the greatest exponent determines the **DEGREE** of the polynomial.

$$3x^2 - 2x^1 + 5$$

The term $-2x$ has a degree of 1

The term 5 is **constant term**. Its value does not change when the value of x changes. **A constant term has a degree of 0.**

What is the degree of the polynomial?

	(Highest exponent) Degree on variable	# Terms
a) $-3x^4$	4	1
b) $-2x^2 + 3x - 4$	2	3
c) $2x^4 + 4x^4 - 6$	4	3
d) $-3x^2 + 4x^3 - 2x + 4$	3	4
e) 4	none	1

What is not a polynomial?

If an expression has a square root of a variable \sqrt{x} , or has a variable in the denominator $(\frac{1}{x}, \frac{2}{x^2})$ it IS **NOT A POLYNOMIAL!**