

$$5p^2 + 20p - 225$$

$$5 \left(p^2 + 4p - 45 \right)$$

sign of big 9
signs diff

Simple tr:

$$5(x-5)(x+9)$$

$\frac{x}{-45}$	$\frac{+}{4}$
$-1, +45$	
$-3, +15$	
$-5, +9$	

See next page

Homework SOLUTIONS

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Questions: 10, 13, 15ab, 21ce

maybe ~~19 and 20~~

10. Copy and complete.

a) $(w + 3)(w + 2) = w^2 + \square w + 6$

MultiplyAdd

b) $(x + 5)(x + \square) = x^2 + \square x + 10$

MultiplyAdd

c) $(y + \underset{2}{\square})(y + \underset{10}{\square}) = y^2 + 12y + 20$

MultiplyAdd

+ 20

+ 12

+1, +20

+2, +10

+4, +5

13. Find and correct the errors in each expansion.

a) $(r-13)(r+4) = r(r+4) - 13(r+4)$
 $= r^2 + 4r - 13r + 52$
 $r^2 + 4r - 13r - 52$
 $r^2 - 9r - 52$

b) $(s-15)(s-5) = s(s-15) + 15(s+5)$
 $= s^2 - 15s + 15s + 75$
 $= s^2 + 75$

$$s^2 - 5s - 15s + 75$$

$$s^2 - 20s + 75$$



15. Factor. Check by expanding.

a) $12 + 13k + k^2$

$k^2 + 13k + 12$

$(k+1)(k+12)$

b) $-16 - 6g + g^2$

$g^2 - 6g - 16$

$(g-8)(g+2)$ ← ✓

c) $60 + 17y + y^2$

$y^2 + 17y + 60$

$(y \quad) (\quad)$

d) $72 - z - z^2$

$z^2 - z - 72$

19. Find an integer to replace \square so that each trinomial can be factored.
How many integers can you find each time?

a) $x^2 + \square x + 10$

b) $a^2 + \square a - 9$

c) $t^2 + \square t + 8$

$\begin{array}{c} 9 \\ 6 \end{array}$

$\frac{x}{8}$
 $\begin{array}{c} 1, 8 \\ 2, 4 \end{array}$

d) $y^2 + \square y - 12$

e) $h^2 + \square h + 18$

f) $p^2 + \square p - 16$



20. Find an integer to replace \square so that each trinomial can be factored.

How many integers can you find each time?

a) $r^2 + r + \square$

b) $h^2 - h + \square$



c) $b^2 + 2b + \square$

d) $z^2 - 2z + \square$

e) $q^2 + 3q + \square$

f) $g^2 - 3g + \square$

21. Factor.

c) $4x^2 + 4x - 48$

$$4(x^2 + x - 12)$$

$$4(x+4)(x-3)$$

a) $4y^2 - 20y - 56$

e) $-5n^2 + 40n - 35$

$$-5(n^2 - 8n + 7)$$

$$-5(n-7)(n-1)$$

$$\text{OR}$$
$$+5(n+7)(n+1)$$

b) $-3m^2 - 18m - 24$

d) $10x^2 + 80x + 120$

f) $7c^2 - 35c + 42$

Factoring Trinomials

#1

$$x^2 - 17x + 42$$

$$(x-3)(x-14)$$

$$\begin{array}{r} x \\ +42 \\ -1, 42 \\ -2, 21 \\ -3, 14 \\ -6, -7 \end{array} \quad \begin{array}{r} + \\ -17 \end{array}$$

#2

$$x^2 - 17x - 38$$

$$(x-19)(x+2)$$

$$\begin{array}{r} x \\ -38 \\ + \\ -17 \end{array}$$

#3


$$4x^2 + 5x - 6$$

New Method

What do you notice ??

DECOMPOSITION

If there is a numerical coefficient in front of x^2 , then we use a method for factoring called *DECOMPOSITION*.


$$4x^2 + 5x - 6$$

Hard Trinomials

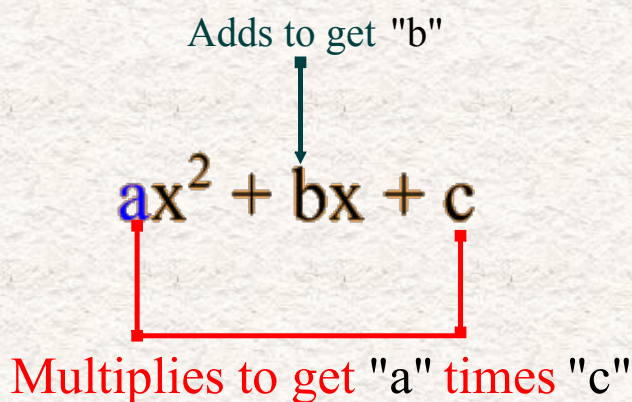
- has three terms with the form...

$$ax^2 + bx + c$$

- a hard trinomial has an "a" value not equal to 1.
- we use a method of decomposition to factor them.

DECOMPOSITION METHOD

- here's how it goes... "What two numbers?"




- once you find the two numbers, use them to break the MIDDLE TERM into two pieces (decomposition).
- then, factor by grouping.

Example

Factor $6x^2 - 11x + 3$

Solution

We are looking for two specific numbers.

What is the sum of these two numbers? 

Decompose middle term

$$6x^2 - 2x - 9x + 3$$

$$2x(3x - 1) - 3(3x - 1)$$

$$(3x - 1)(2x - 3)$$

$$\begin{array}{r} X^{+6x^3} \\ +18 \\ -1, 18 \\ -2, 9 \\ -3, 6 \end{array} \quad \begin{array}{r} + \\ -11 \end{array}$$


$$(3x - 1)(2x - 3)$$

Multiply

$(4x^2 + \underline{5x} - 6)$

$\underline{\quad} + \underline{\quad} = \text{orange box } 5$
 $\underline{4} \times \underline{-6} = \text{orange box } -24$
 $-1, 24$
 $-2, 12$
 $-3, 8 \checkmark$
 $-4, 6$

$4x^2 + 8x - 3x - 6$
 $4x(x+2) - 3(x+2)$
 $(x+2)(4x-3)$



$$|n^2 + 7n + 12$$

$$\frac{x}{+12} \quad \frac{+}{+7}$$

$$\underbrace{n^2 + 3n} + \underbrace{4n + 12}$$

$$+3, +4$$

$$n(n+3) + 4(n+3)$$

$$(n+3)(n+4)$$

Always check the following when you are asked to factor:

- 1) G.C.F (# and Letters) {if not....}
- 2) Simple Trinomial
- 3) Hard Trinomial ...

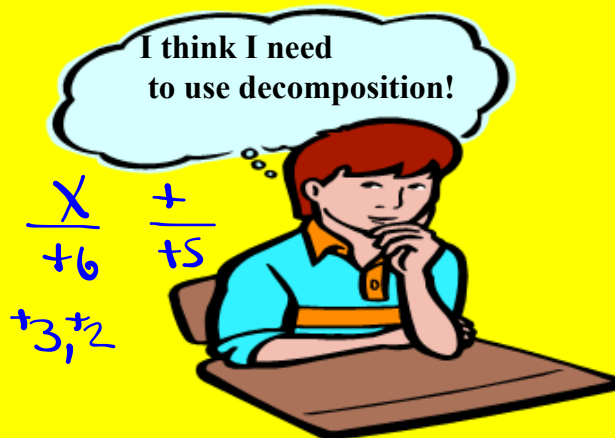
Factor Completely!

1. $2x^2 + 5x + 3$

$$\underline{2x^2 + 2x} + \underline{3x + 3}$$

$$2x(x+1) + 3(x+1)$$

$$(x+1)(2x+3)$$



Factor Completely!

$$2. \quad 10x^2 + 13x - 3$$

$$\begin{array}{r} x \\ -30 \\ -1, +30 \\ -2, +15 \\ -3, +10 \end{array} \quad \begin{array}{r} + \\ +13 \end{array}$$

$$10x^2 - 2x + 15x - 3$$

$$2x(5x-1) + 3(5x-1)$$

$$(5x-1)(2x+3)$$



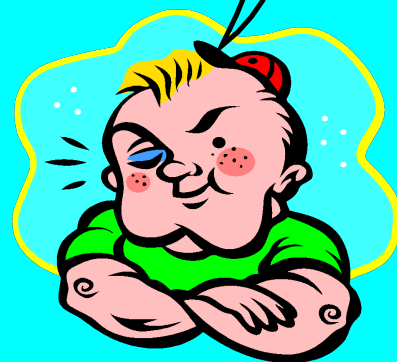
$$\star 4. 2x^2+6x+4 \star$$

$$2 (x^2 + 3x + 2)$$

Simple trinomial

$$2 (x+1)(x+2)$$

I suppose she wants me to do two types of factoring!



3.6 Polynomials of the Form $ax^2 + bx + c$

Homework

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Questions: ~~8~~, 13, ~~15~~, ~~19~~