

Warm Up



1) A line that passes through $(-7, 2)$ and $(3, -1)$

- a) Write an equation in point slope form:
- b) Write an equation in slope intercept form:
- c) State the x and y intercept

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{-1 - 2}{3 - (-7)}$$

$$m = \frac{-3}{10} \quad \text{Point } (-7, 2)$$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = \frac{-3}{10}(x - (-7))$$

$$y - 2 = \frac{-3}{10}(x + 7)$$

Slope point form

$$b) \quad y - 2 = \frac{-3}{10}x - \frac{21}{10} + \frac{2}{1} \times \frac{10}{10}$$

$$y = \frac{-3}{10}x - \frac{21}{10} + \frac{20}{10}$$

Common Denominators

$$y = \frac{-3}{10}x - \frac{1}{10}$$

$y = mx + b$ y intercept

c) x-intercept (let $y=0$)

$$y = \frac{-3}{10}x - \frac{1}{10}$$

$$10(0) = \left(\frac{-3}{10}x - \frac{1}{10}\right) \times 10$$

$$0 = \frac{-30}{10}x - \frac{10}{10}$$

$$0 = -3x - 1 + 1$$

$$\frac{1}{-3} = \frac{-3x}{-3}$$

$$\frac{-1}{3} = x$$

$$\begin{aligned} 0 &= \frac{-3}{10}x - \frac{1}{10} \\ \frac{1}{10} &= \frac{-3}{10}x \\ -30x &= 10 \\ \frac{1}{-3} &= x \\ x &= \frac{-1}{3} \end{aligned}$$

$$y = mx + b$$

$$y = \frac{-3}{10}x - \frac{1}{10}$$

or let $x=0$

$$y = \frac{-3}{10}(0) - \frac{1}{10}$$

$$y = \frac{-1}{10}$$

Homework Solutions

$$\begin{aligned}
 1) \quad & y - y_1 = m(x - x_1) \\
 & y - 8 = 2(x - (-1)) \\
 & y - 8 = 2(x + 1) \\
 & y - 8 = 2x + 2 \\
 & y - 8 + 8 = 2x + 2 + 8 \\
 & y = 2x + 10
 \end{aligned}$$

$$\begin{aligned}
 2) \quad & y - y_1 = m(x - x_1) \\
 & y - (-3) = 4(x - 6) \\
 & y + 3 = 4(x - 6) \\
 & y + 3 = 4x - 24 \\
 & y + 3 - 3 = 4x - 24 - 3 \\
 & y = 4x - 27
 \end{aligned}$$

$$\begin{aligned}
 3) \quad & y - y_1 = m(x - x_1) \\
 & y - (-6) = \frac{3}{4}(x - (-1)) \\
 & y + 6 = \frac{3}{4}(x + 1) \\
 & y + 6 = \frac{3x + 3}{4} \\
 & y + 6 - 6 = \frac{3x + 3}{4} - 6 \\
 & y = \frac{3x + 3}{4} - \frac{24}{4} \\
 & y = \frac{3x - 21}{4}
 \end{aligned}$$

$$\begin{aligned}
 4) \quad & y - y_1 = m(x - x_1) \\
 & y - 1 = -3(x - (-1)) \\
 & y - 1 = -3(x + 1) \\
 & y - 1 = -3x - 3 \\
 & y - 1 + 1 = -3x - 3 + 1 \\
 & y = -3x - 2
 \end{aligned}$$

$$\begin{aligned}
 6) \quad & m = \frac{y_2 - y_1}{x_2 - x_1} \\
 & m = \frac{1 - (-2)}{(-4) - (3)} \\
 & m = \frac{1 + 2}{(-4) - (3)} \\
 & m = \frac{3}{-7}
 \end{aligned}$$

$$\begin{aligned}
 & y - y_1 = m(x - x_1) \\
 & y - (-2) = \frac{3}{-7}(x - 3) \\
 & y + 2 = \frac{3(x - 3)}{-7} \\
 & y + 2 = \frac{-3x + 9}{7} \\
 & y + 2 - 2 = \frac{-3x + 9}{7} - 2 \\
 & y = \frac{-3x + 9}{7} - \frac{14}{7} \\
 & y = \frac{-3x - 5}{7}
 \end{aligned}$$

$$(-4, 1) \quad -\frac{3}{7}$$

$$y - 1 = -\frac{3}{7}(x + 4)$$

$$y - 1 = -\frac{3}{7}x - \frac{12}{7} + 1$$

$$y = -\frac{3}{7}x - \frac{12}{7} + \frac{7}{7}$$

$$7(y) = \left(-\frac{3}{7}x\right) - \left(\frac{5}{7}\right)$$

Standard
 $Ax + By = C$

$$7y = -3x - 5$$

$$+3x \quad 7y = \cancel{-3x} - 5$$

Standard

$$3x + 7y = -5$$

$$3x + 7y + 5 = \cancel{-5} + 5$$

General

$$3x + 7y + 5 = 0$$

6.6 General Form of the Equation for a Linear Relation



LESSON FOCUS

Relate the graph of a linear function to its equation in general form.

Make Connections

A softball team may field any combination of 9 female and male players. There must be at least one female and one male on the field at any time. What are the possible combinations for female and male players on the field?



Slope-intercept

$$y = mx + b$$

Slope-Point Equation

$$y - y_1 = m(x - x_1)$$

Linear Equations

**Slope
Intercept Form**

$$y = mx + b$$

**Point Slope
Form**

$$y - y_1 = m(x - x_1)$$

Two other forms of Linear Equations

Standard

$$Ax + By = C$$

- Where A, B and C are integers

Example:

$$2x + 7y = 10$$

$$Ax + By = C$$

General

$$Ax + By + C = 0$$

General Form of the Equation of a Linear Relation

$Ax + By + C = 0$ is the general form of the equation of a line, where A is a whole number, and B and C are integers.

Example:

$$2x + 7y - 10 = 0$$

$$Ax + By + C$$

Point - Slope to General Form

Method 1: distribute through

$$y - 3 = \frac{2}{5}(x + 6)$$

$$y - 3 = \frac{2x}{5} + \frac{12}{5}$$

$$y - 3 = \frac{2x}{5} + \frac{12}{5} + \frac{3}{1}$$

$$y = \frac{2}{5}x + \frac{12}{5} + \frac{15}{5}$$

$$y = \frac{2}{5}x + \frac{27}{5} \quad \begin{array}{l} \text{slope} \\ \text{intercept} \\ \text{form} \end{array}$$

$$(5)y = \frac{2}{5}(5)x + \frac{27}{5}(5)$$

$$5y = 2x + 27$$

$$5y - 2x = 27 \quad \begin{array}{l} \text{Standard} \\ \text{form} \end{array}$$

$$5y - 2x = 27$$

$$5y - 2x - 27 = 0 \quad \begin{array}{l} \text{General} \\ \text{form} \end{array}$$

$$y - 3 = \frac{2x}{5} + \frac{12}{5}$$

$$5y - 15 = 2x + 12$$

$$5y = 2x + 27$$

Point - Slope to General Form

Method 2: Get rid of denominator by multiplying each side by denominator

$$5 \cdot [y - 3] = \left[\frac{2}{5} (x + 6) \right] \cdot 5$$

$$5y - 15 = 2(x + 6)$$

$$5y - 15 = 2x + 12$$

$$5y - \cancel{15} = 2x + 12 + 15$$

$$5y = 2x + 27$$

$$-2x + 5y = 27$$

$$-2x + 5y = 27 - 27$$

$$-2x + 5y - 27 = 0$$

You try

Point - Slope to General Form

$$7x[y + 6] = \left[\frac{-3}{7} (x - 2) \right] x7$$

$$7(y+6) = -3(x-2)$$

$$7y + 42 = -3x + 6$$

$$7y + \cancel{42} = -3x + \underbrace{6 - 42}$$

$$7y = -3x - 36 - 7y$$

$$0 = -3x - 7y - 36$$

$$3x + 7y + 36 = 0$$

Slope Intercept to

General Form

$$a) \quad y = \left[-\frac{2}{3}x + 4 \right]$$

$$y = -\frac{2}{3}x + 4$$

$$3y = -2x + 12$$

$$0 = -2x - 3y + 12$$

General Form
 $Ax + By + C = 0$

Slope Intercept
 $y = mx + b$

$$7x - 2y + 18 = 0$$

(Handwritten: -2y is crossed out with a blue slash, and +2y is written next to the 0)

step 1) Locate y and take it to the side so it is positive

$$\frac{7x + 18}{2} = \cancel{2}y$$

(Handwritten: 2y is crossed out with a red slash)

$$\frac{7}{2}x + \frac{18}{2} = y$$

(Handwritten: "Reduce" is written below the fraction 18/2)

$$\frac{7}{2}x + 9 = y$$

(Handwritten: The final equation is enclosed in a red cloud-like border)

Homework

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Questions: 4, 5, 6, ~~7~~, ~~8~~, 12, 18, ^ab

^q_b ^q_o

$$y = mx + b \quad \text{slope intercept}$$

$$y - y_1 = m(x - x_1) \quad \text{slope point}$$

$$Ax + By = C \quad \text{Standard}$$

$$Ax + By + C = 0 \quad \text{General}$$

Test TUESDAY