

1(a) $4x - 7y = 6$
 $2x + y = 12$

① $4x - 7y = 6$
 ② $\times 7$ $14x + 7y = 84$

① + ② $18x = 90$
 $x = 5$

Sub $x = 5$
 $4(5) - 7y = 6$
 $20 - 7y = 6$
 $-7y = -14$
 $y = 2$

$(5, 2)$

(b) ① $6x - 5y = -3$
 ② $5x + 3y = 19$

① $\times 3$ $18x - 15y = -9$
 ② $\times 5$ $25x + 15y = 95$

① + ② $43x = 86$
 $x = 2$

Sub $x = 2$
 $6(2) - 5y = -3$
 $12 - 5y = -3$
 $-5y = -15$
 $y = 3$

$(2, 3)$

(c) $3(x+4) - 4(y+1) = 7$ $x - 9 = y$
 $3x + 12 - 4y - 4 = 7$ $x - y = 9$
 $3x - 4y + 8 = 7$
 $3x - 4y = -1$

① $3x - 4y = -1$
 ② $x - y = 9$

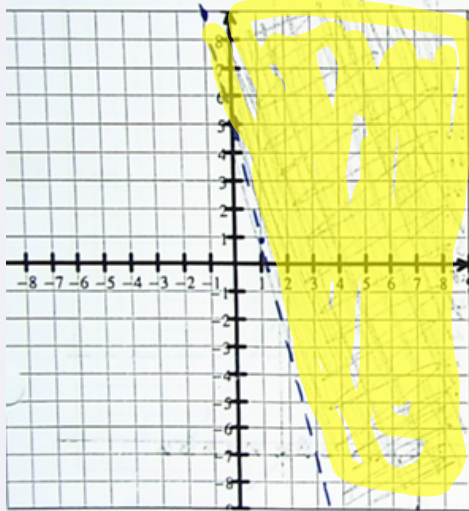
① $3x - 4y = -1$
 ② $\times 3$ $3x - 3y = 27$

① - ② $-y = -28$
 $y = 28$

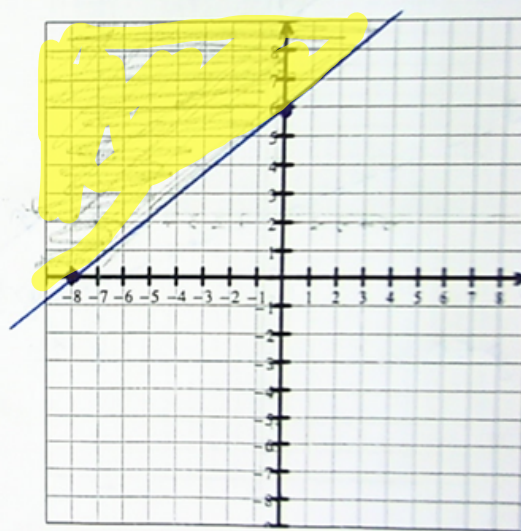
Sub $y = 28$ $x - 28 = 9$
 $x = 37$

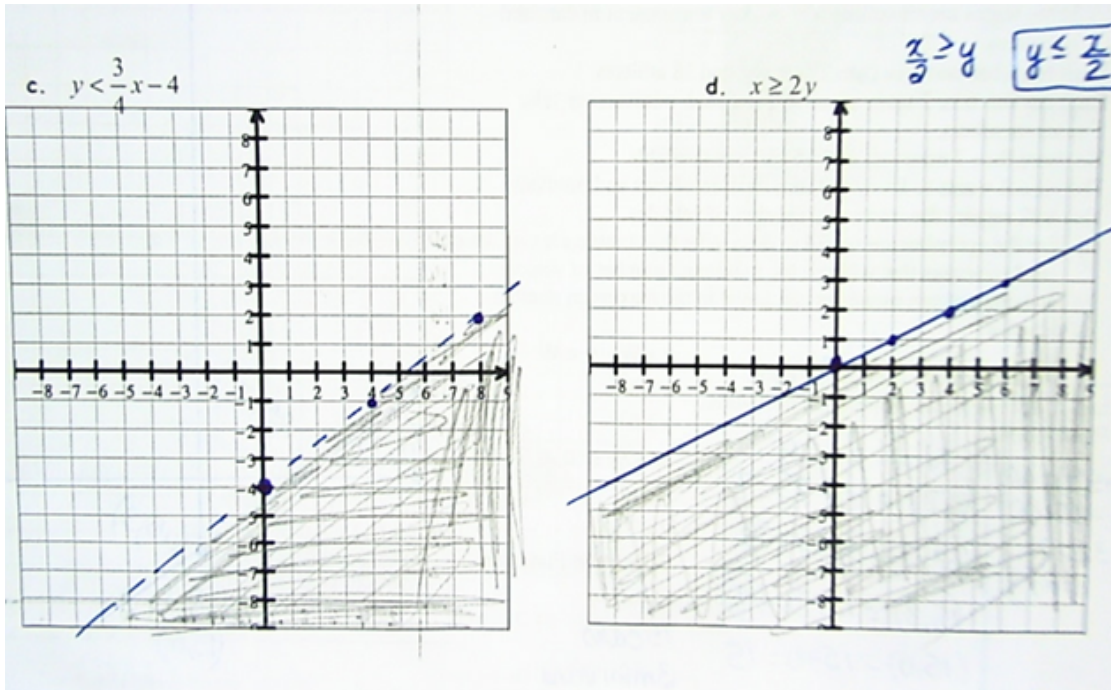
$(37, 28)$

2. a. $y > -4x + 5$



b. $3x - 4y \leq -24$





3. Given the following constraints, graph each:

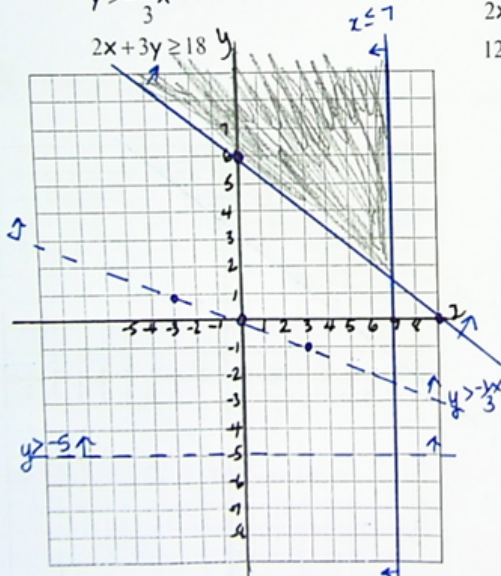
a. $x \in \mathbb{R}, y \in \mathbb{R}$

$x \leq 7$

$y > -5$

$y > -\frac{1}{3}x$

$2x + 3y \geq 18$



b. $x \geq 0$

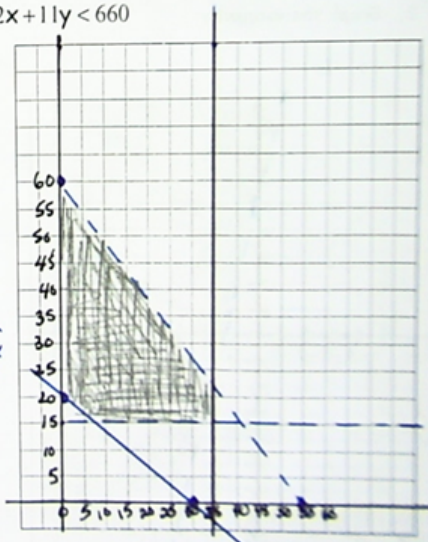
$y \geq 0$

$x \leq 35$

$y > 15$

$2x + 3y \geq 60$

$12x + 11y < 660$



4. Three teams are travelling to a hockey tournament in cars and minivans.
- Each team has no more than 2 coaches and 18 athletes.
 - Each car can take 3 team members, and each minivan can take 5 team members.
 - No more than 7 minivans and 15 cars are available.
- The school wants to know the combination of cars and minivans that will require the maximum number of vehicles.
- Use the optimization model to determine the combination of cars and minivans that will use the maximum number of vehicles.
 - How many team members can travel in the maximum number of vehicles?

Let x represent the number of cars.
 Let y represent the number of minivans.

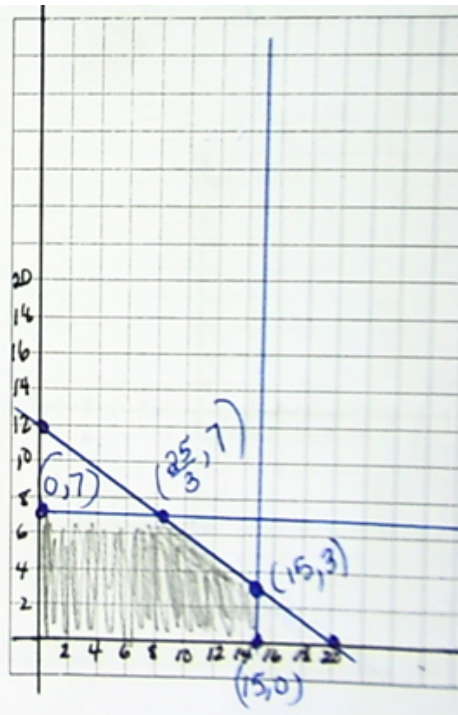
Restrictions:

$$\begin{aligned} 3x + 5(7) &= 60 \\ 3x + 35 &= 60 \\ 3x &= 25 \\ x &= \frac{25}{3} \end{aligned}$$

$$\begin{aligned} N &= x + y \\ (0, 7) &= 0 + 7 = 7 \\ (\frac{25}{3}, 7) &= \frac{25}{3} + 7 = \frac{46}{3} \\ (15, 3) &= 15 + 3 = 18 \\ (15, 0) &= 15 + 0 = 15 \end{aligned}$$

$$\begin{aligned} x \in W \quad y \in W \\ x \geq 0 \\ y \geq 0 \\ 3x + 5y \leq 60 \\ x \leq 15 \\ y \leq 7 \end{aligned}$$

Objective Function
 $N = x + y$
 15 cars
 3 minivans



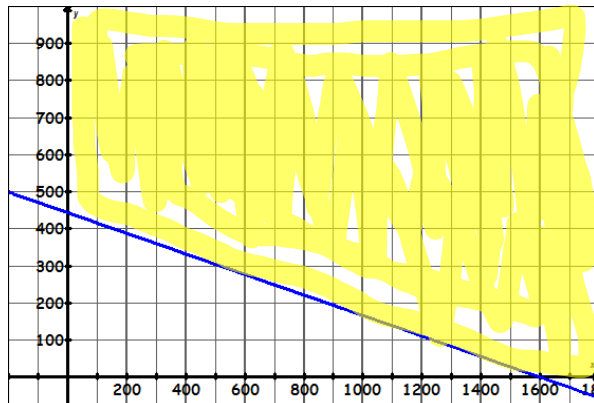
Ans: 15 cars, 3 minivans

this point is not justified because you cannot have 25/3 cars....

5. $x = \text{school friends}$
 $y = \text{karate friends}$
 $x + y \leq 460$
 $x \geq 2y$

b. $x = \text{\# salami}$
 $y = \text{\# cheese}$
 $x + y \leq 820$
 $3x \geq 2y$

17. $x = \text{\# bouquets}$
 $y = \text{\# tickets}$
 $5x + 18y \geq 8000$



8. $x = \# \text{ hot dogs}$
 $y = \# \text{ hamburgers}$
 $x + y \leq 250$
 $x \leq 200$
 $y \leq 120$
 $P = 3x + 5y$

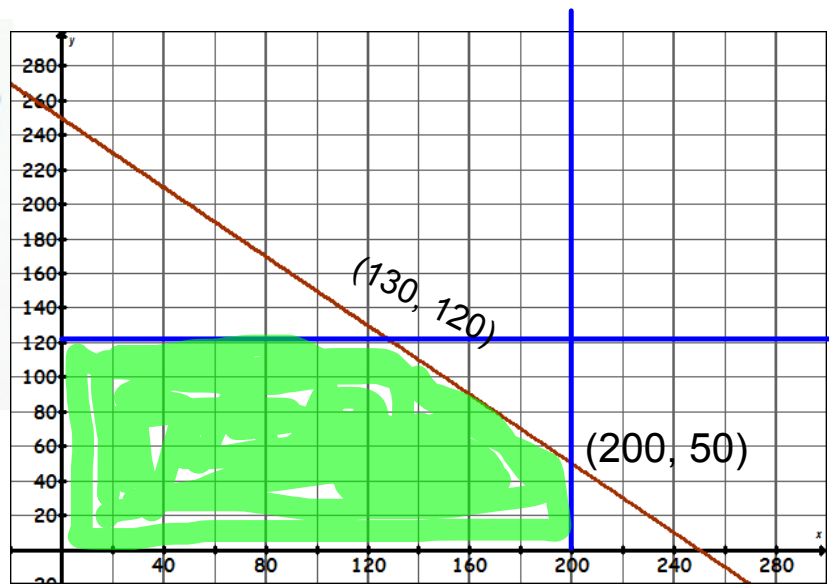
$(0, 0) \quad P = 0$

$(0, 120) \quad P = 600$

$(130, 120) \quad P = 990 \text{ max}$

$(200, 50) \quad P = 850$

$(200, 0) \quad P = 600$



9. $x = \# \text{ hot dogs}$
 $y = \# \text{ sausages}$
 $x + y \leq 400$
 $y \geq 2x$

$$P = 2.50x + 3.50y$$

$$P = 2.50x + 3.50y$$

$$(0, 0) = 0$$

$$(400, 0) = 1000$$

$$\left(\frac{400}{3} + \frac{800}{3}\right) = \frac{3800}{3} = 1266.\bar{6} \text{ max}$$

